Late Stages of Stellar Evolution

Low to Intermediate Mass Stars

Introduction

Stars evolve because of two (irreversible) processes:

Nuclear burning (in the core)
Mass loss (from the surface)

Massive stars (M > 9 M_o) lose mass during most of their lifes, and finally explode as supernovae.
Low and intermediate mass stars (M < 9 M_o) only lose

large amounts of mass towards the end of their evolution, and end up as White Dwarfs.

 Without mass loss, stars with masses as low as 4 M_o would explode as supernovae.

Relevance of Lower Mass Stars

- Stars that end up as WDs may seem less spectacular than those that become SNe, but they are important in the lifecycle of gas/dust in galaxies.
 - Most stars are low mass stars:
 - The initial mass function of stars can be approximated with the Salpter function: $\frac{dN}{dM} \propto M^{-2.35}$
 - Using this we see that >90% of stars have a mass between 0.8 and 8 M_{\odot} .

The lower mass limit is set by the lifetime of stars:

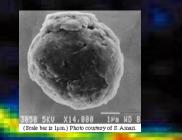
 $t_{\rm evol} \propto M^{-2.5}$

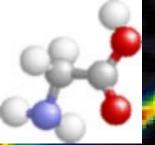
• Stars with a mass of 0.8 M_{\odot} take longer than 14 Gyr to evolve off the Main Sequence.

The Life Cycle of Gas & Dust

- Stars form from the interstellar gas, which to a large extent comes from previous generations of stars. This is known as the life cycle of gas & dust.
 - Although lower mass stars do not enrich the ISM as much as SNe, they still contribute substantially (and dominate the budget of certain elements).
- Lower mass stars are also the main producers of dust grains in galaxies, both Si-based and C-based.
 - The complex chemistry in their circumstellar envelopes allows the formation of complex (organic even)

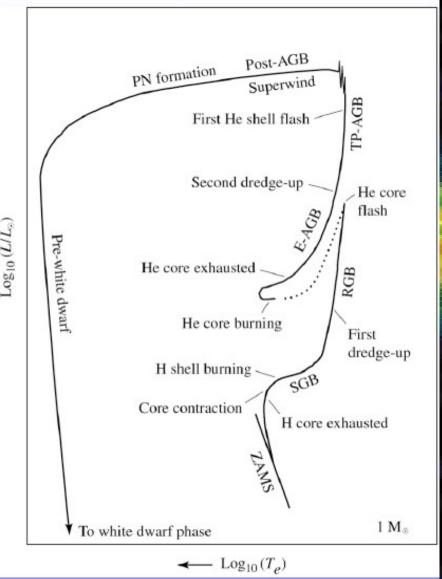
molecules.





Evolution across the HR-Diagram

- After the MS, our stars evolve through 6 phases:
 - Sub-Giant Branch
 - Red Giant Branch (RGB) phase.
 - Horizontal Branch (HB) phase.
 - Asymptotic Giant Branch (AGB) phase.
 - Planetary Nebula (PN) phase.
 - White Dwarf (WD) phase.



Course Contents

- Review of Stellar Evolution
- Evolution on the AGB
 - Thermal pulses, nucleosynthesis and dredge-up Pulsation
- Mass loss
- Circumstellar Envelope
- Post-AGB Evolution

Basic Stellar Evolution

Equations:

Mass conservation:

dM

$$\frac{dM_r}{dr} = 4\pi r^2 \rho$$
Hydrostatic equilibrium:

$$\frac{dp}{dr} = -\frac{GM_r \rho}{r^2}$$
Energy production:

$$\frac{dL_r}{dr} = 4\pi r^2 \rho \epsilon$$

Energy transport:

 $\frac{\mathrm{d}T_r}{\mathrm{d}r} = \begin{cases} -\frac{3}{4ac} \frac{\bar{\kappa}\rho}{T^3} \frac{L_r}{4\pi r^2} & \text{if } \frac{\mathrm{d}\ln P}{\mathrm{d}\ln T} > \gamma/(\gamma - 1) \text{ (radiative diffusion)} \\ -\left(1 - \frac{1}{\gamma}\right) \frac{\mu m_{\mathrm{H}}}{k_{\mathrm{B}}} \frac{GM_r}{r^2} & \text{if } \frac{\mathrm{d}\ln P}{\mathrm{d}\ln T} < \gamma/(\gamma - 1) \text{ (adiabatic convection)} \end{cases}$

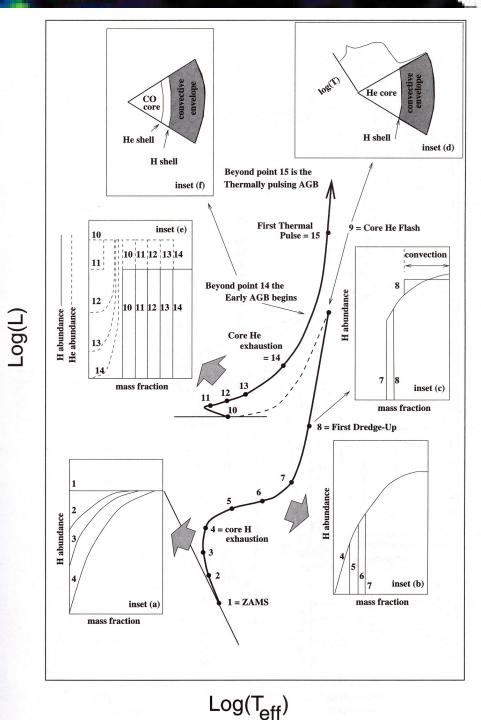
combined with

Equation of state: $p = p(\rho, T, \text{composition})$ Nuclear reactions: $\epsilon = \epsilon(\rho, T, \text{composition})$

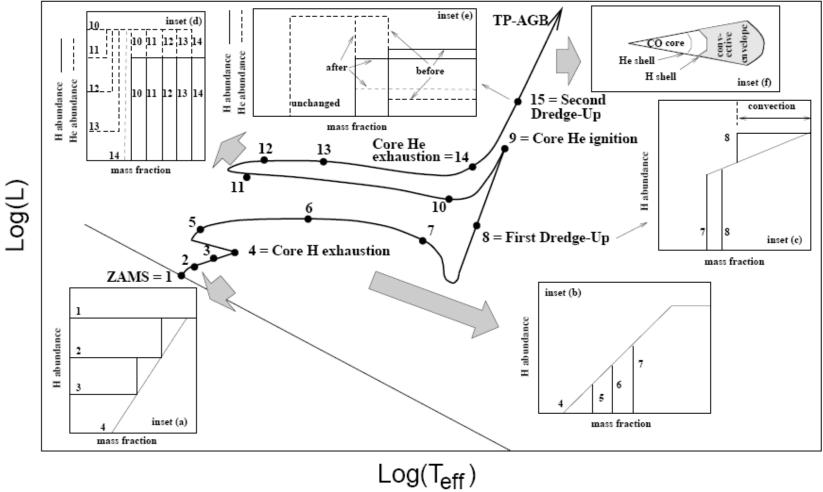
Opacity: $\bar{\kappa} = \bar{\kappa}(\rho, T, \text{composition})$

$1 M_{\odot}$ Star

- 1-4: Core H-burning
- 4-8: H-shell burning
 8: Convection, 1st dredge-up
- 9: He-core flash
- 9-14: Core He-burning14- : AGB







Some Mass Limits

Main Sequence: M_{ZAMS} $\begin{cases} < 1.3 M_{\odot} & \text{pp-chain dominates} \\ > 1.3 M_{\odot} & \text{CNO-cycle dominates} \end{cases}$

 $\text{RGB: } M_{\text{ZAMS}} \begin{cases} < 2.3 M_{\odot} & \text{electron-degenerate He-core} \\ > 2.3 M_{\odot} & \text{non-degenerate He-core} \end{cases}$

 $M_{\rm ZAMS} < 0.6 M_{\odot}$ He-burning never starts

 $M_{\rm ZAMS} \begin{cases} < 9 M_{\odot} & {
m electron-degenerate C/O \ core} \\ > 9 M_{\odot} & {
m non-degenerate C/O \ core} \end{cases}$

Shells Sources

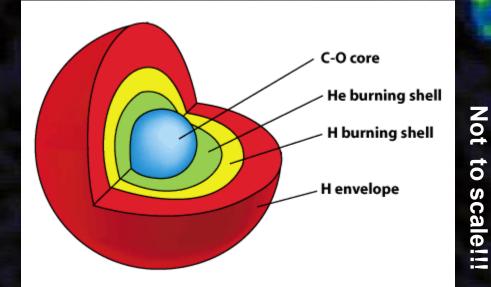
- The three rules of thumb for active shell sources: Associated with a density jump (due to composition difference between core and shell)
 - Position fixed in time (due to thermal feedback). For example r_{shell}=0.03R_o throughout most of the post-MS evolution of a 1 M_o star.
 - Shells mirror the expansion/contraction of their interiors.

Core contraction (Active Shell) Envelope expansion Core expansion (Active Shell) Envelope contraction

Stellar Evolution on AGB

Once on the AGB, all stars have a similar structure;

- C/O core
- He-shell
- Intershell region
- H-shell
- H-envelope



Their evolution is therefore also similar, although still mass-dependent.

The evolution is dominated by occasional activity of the He-shell: thermal pulses.

Early AGB

- The period before the first thermal pulse is known as the early AGB (E-AGB).
 - Stars with M > 4 M_{\odot} lose their active H-shell during this period, and the convective envelope can reach down and mix up processed material: Second Dredge Up.
 - Both 1st and 2nd Dredge-Up bring up CNO-processed material: ⁴He↑ ¹²C↓ ¹³C↑ ¹⁴N↑

At the end of the E-AGB all stars have an active H-shell and an inactive, but growing He-shell.

Thermally Pulsing AGB

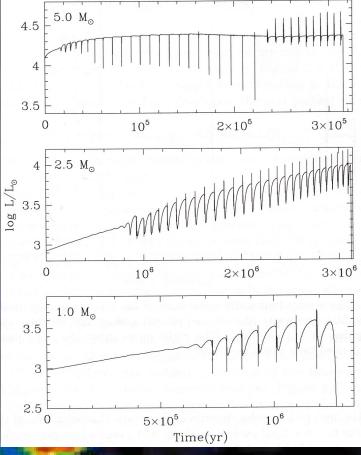
- The rest of the AGB is known as the TP-AGB, as the evolution is dominated by a series of TPs: short outbursts of the He-shell, separated by longer periods of H-shell activity.
- At the same time the star starts to lose material from its surface, with rates of the order $10^{-7} M_{\odot}/yr$.
- The luminosity of these stars ranges from 10^3 to $10^4 L_{\odot}$, so they consume something like $10^{-8} M_{\odot}$ /yr in nuclear fusion.
 - The conclusion is that mass loss dominates the evolution on the AGB!

AGB Evolution

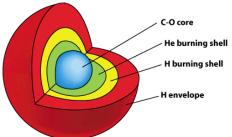
Time Scales

Luminosity Evolution

| $M_{\rm i}$ | $M_{ m f}$ | $M_{\mathrm bol}$ | $t_{\rm MS}$ | $t_{\rm EAGB}$ | $t_{\rm EAGB}$ | t_{TPAGB} | t_{TPAGB} | |
|-------------------|------------|-------------------|--------------|----------------|----------------|----------------------|----------------------|--|
| [M _☉] | | | [Gyr] | [Myr] | t_{MS} [%] | [Myr] | $t_{\rm MS}$ [%] | |
| | and the | - united | 2 | Z=0.016 | | | | |
| 1.0 | 0.57 | -4.0 | 11.3 | 12 | 0.16 | 0.50 | 0.004 | |
| 1.5 | 0.60 | -4.5 | 2.7 | 9.2 | 0.34 | 0.83 | 0.03 | |
| 2.0 | 0.63 | -4.9 | 1.2 | 7.9 | 0.66 | 1.20 | 0.10 | |
| 2.5 | 0.67 | -5.1 | 0.62 | 1.1 | 0.18 | 2.20 | 0.35 | |
| 3.5 | 0.75 | -5.7 | 0.23 | 2.8 | 1.2 | 0.43 | 0.19 | |
| 5.0 | 0.89 | -6.2 | 0.10 | 1.2 | 1.2 | 0.26 | 0.27 | |
| 19 | | | 2 | Z=0.004 | 19 June - | | | |
| 1.0 | 0.59 | -4.5 | 6.7 | 8.0 | 0.12 | 0.87 | 0.01 | |
| 1.5 | 0.64 | -4.9 | 2.1 | 6.3 | 0.30 | 0.97 | 0.05 | |
| 2.0 | 0.67 | -5.2 | 0.89 | 6.7 | 0.75 | 1.60 | 0.18 | |
| 2.5 | 0.69 | -5.5 | 0.46 | 5.2 | 1.1 | 1.30 | 0.27 | |
| 3.5 | 0.85 | -6.0 | 0.18 | 2.2 | 1.2 | 0.25 | 0.14 | |
| 5.0 | 0.94 | -6.5 | 0.08 | 0.6 | 7.3 | 0.31 | 0.39 | |

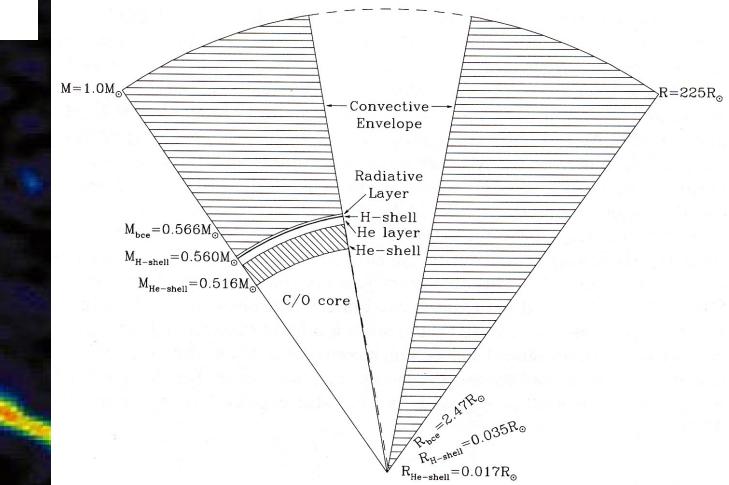


Internal Structure



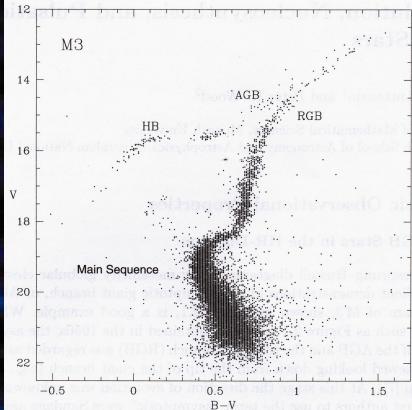
Not to scale!

To scale: very inhomogeneous!



History

- The name Asymptotic Giant Branch was introduced by Sandage & Walker (1966) to describe the observed bifurcation of the Red Giant Branch in HR-diagrams of Globular Clusters:
- Nowadays we use the term AGB for the evolutionary phase when stars become Red Giants for the second time



Thermal Pulses

- The He-core flash is a run-away process because the core is supported by the pressure of degenerate electrons, decoupling the pressure from the temperature. The He-shell in AGB stars is non-degenerate. Why then does the ignition of the He-shell lead to a thermal run-away?
 - The process was first discovered by Schwarzschild & Härm (1965) in their stellar evolution calculations. They also identified the cause:
 - Temperature dependence of the 3α process (∝ T⁴⁰).
 Small width of the shell region.

Gravothermal Specific Heat

- When a certain amount of heat is added to a pocket of gas, its temperature will change according to: dT = 1 dq
- Under isolated circumstances C the specific heat depends only on the gas properties.
- If in addition we require that the gas is part of a system in hydrostatic equilibrium, we obtain instead

$$C_* = C_p \left(1 - \nabla_{\mathrm{ad}} \frac{4\delta}{4\alpha - 3} \right) \quad \rho \propto p^{\alpha} T^{-\delta} \quad \nabla_{\mathrm{ad}} = \left(\frac{\mathrm{d} \ln p}{\mathrm{d} \ln T} \right)_{S}$$

 $\mathrm{d}t$

 $C \, \mathrm{d}t$

For a monatomic gas ∇_{ad} =0.4, α = δ =1, so C_* =-0.6 C_p <0.

- Adding heat brings down the temperature!
- Explanation: upon heating, the gas pocket will expand, pushing the upper layers out, doing work, losing energy.

Adding Energy Production & Opacity

 A more complete picture requires that we take into account the energy production rate ε and the energy transport (proportional to the opacity κ):

 $\kappa \propto \rho^p T^q$

This gives an expression:

 $\epsilon \propto \rho^{\lambda} T^{\nu}$

$$\frac{\mathrm{d}T}{\mathrm{d}t} = \frac{K}{C_*} \frac{\mathrm{d}T}{T}$$

$$K = \frac{L}{M} \left[(\nu + q - 4) + \frac{\delta}{4\alpha - 3} (3\lambda + 3p + 4) \right]$$

 For negative feedback K and C_{*} need to have opposite signs, for positive, the same.

Feedback and Stability

- For a stable situation we need negative feedback: a small temperature increase will lead to higher energy production due to nuclear processes. If this leads to an even higher temperature, we have a run-away process.
 For the pp-chain: v=4, λ=1, for Kramer's opacity q=-3.5, p=1, so *K*>0 and C_{*}<0, and the situation is stable.
 - For 3α in a degenerate core: v=40, λ =2, making K still positive, but now α =3/5, δ =0, so C_{*}>0, and we have positive feedback, and a thermal run-away (until the equation of state is changed).

Shell Sources

- If we want to apply this to shell sources, we have to realize that they have a much smaller volume than a spherical core region.
 - A small expansion of a shell region will lead to a drop in the density, but will not consume much energy in pushing away the outer layers.

$$dV = \frac{3}{r}Vdr$$

$$dV = \frac{1}{D}VdD = \frac{r}{D}\frac{V}{r}dD$$

$$C_* = C_p\left(1 - \nabla_{\rm ad}\frac{4\delta}{4\alpha - 3}\right)$$

$$C_*^{\rm shell} = C_p\left(1 - \nabla_{\rm ad}\frac{4\delta}{4\alpha - r/D}\right)$$

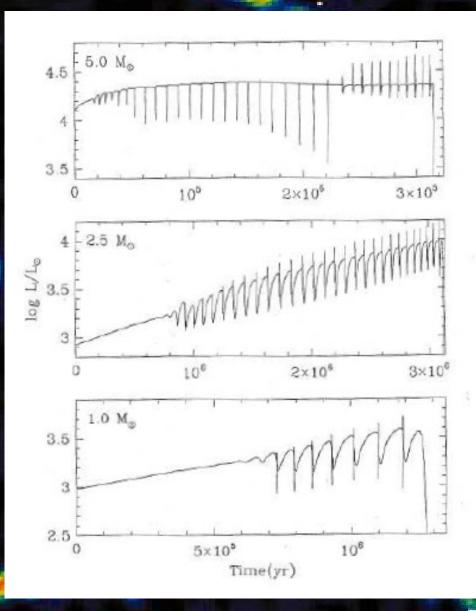
If D<r/4 then C, will still be positive! Unstable!</p>

Interpulse Times

The time between thermal pulses depends on the mass of the star.
 Numerical modelling shows

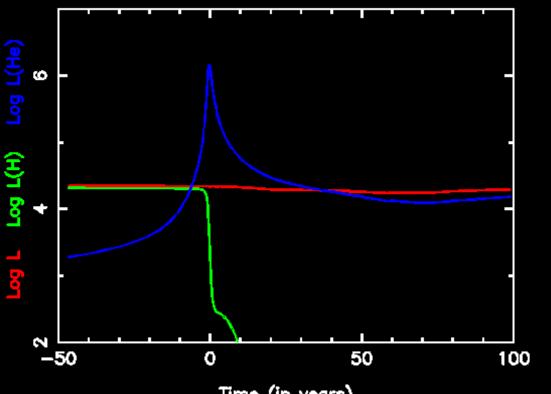
 $\log \tau_{\rm p} = 4.5(1.678 - \frac{M_{\rm core}}{M_{\odot}}) \qquad ({\rm years})$

- For 1 M_{\odot} with $M_c=0.6 M_{\odot}$: 70,000 years For 5 M_{\odot} with $M_c=1.0 M_{\odot}$: 1,100 years
- Peak luminosity: 10⁹ L_o.



What Happens During a TP

He-luminosity \bullet goes up many order of magnitude. **H-luminosity** goes down (Hshell extinguished). Total luminosity remains almost constant



M=5 Z=0.02

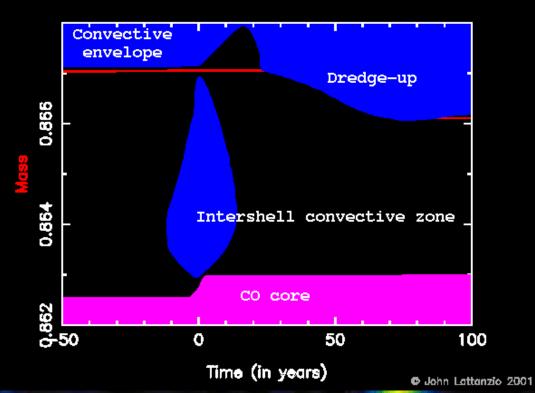
Time (in years)

[🛛] John Lattanzio 2001

Interior Structure During TP

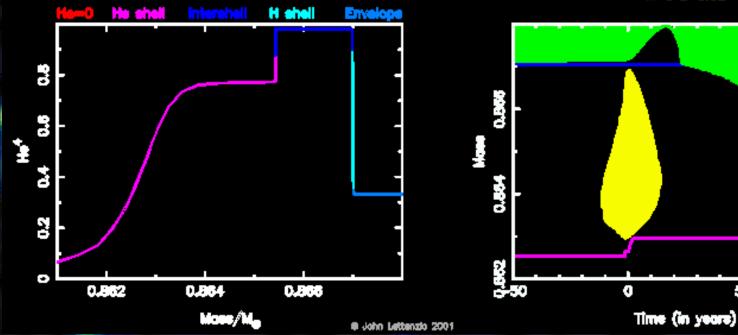
- Blue areas: convective.
- C/O core grows rapidly
 Convective envelope pushed out.
- Intershell convective zone develops.
- After end of pulse, convective zone moves back in.

M=5 Z=0.02



Animated TP Evolution: ⁴He

M=6 2=02



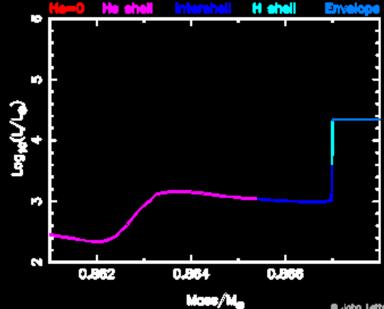
M=5 Z=0.02



100

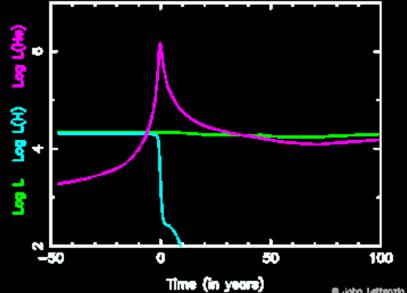
50

Animated TP Evolution: L





M=5 Z=0.02



John Lettenzio 2001

John Lettenzio 2001

Anatomy of a TP

- "Off": He-shell is inactive, Hshell is active.
- "On": He-shell ignites, 10⁸ L_o. Convective zone develops in ISR. Lasts 10-100 years. "**Power-down**": L_{He} declines, expansion of ISR extinguishes H-shell. Overall L drops. Lasts 10-100 years. "Dredge-up": Convective envelope moves in, mixing up processed material. Lasts 10-100 years.

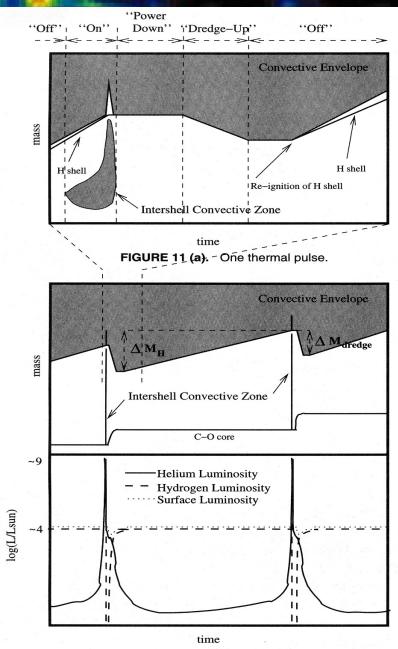
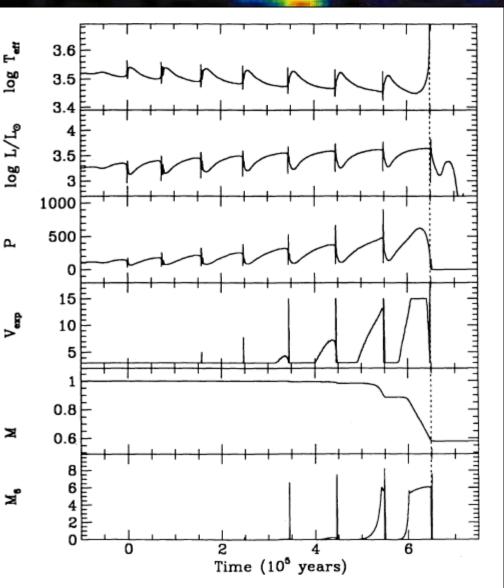


FIGURE 11 (b). Two consecutive thermal pulses

Evolutionary Calculations 1 M_o

Evolution of a 1 M_☉ star on the TP-AGB.
(Y,Z)=(0.25,0.008).
8 TPs.
Total TP-AGB lifetime: 650,000 years.

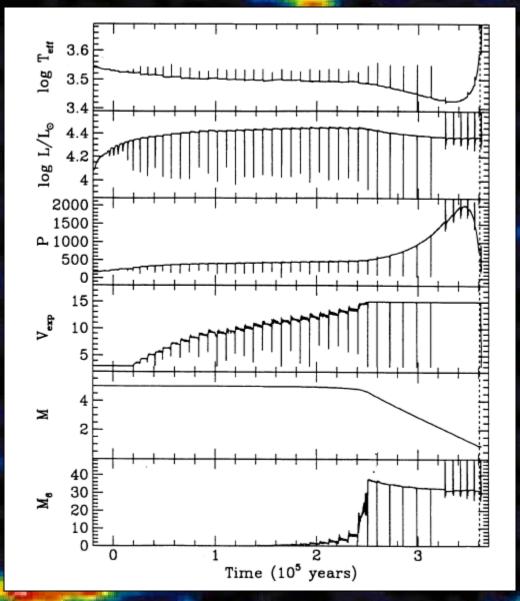
From Vassiliadis & Wood (1993).



Evolutionary Calculations 5 M_o

Evolution of a 5 M_☉ star on the TP-AGB.
(Y,Z)=(0.25,0.008).
~40 TPs.
Total TP-AGB lifetime: 360,000 years.

From Vassiliadis & Wood (1993).



Core Mass – Luminosity Relation

- The luminosity during the "off" phase keeps going up as the star evolves along the TP-AGB.
 - This is connected to the growth of the core mass:

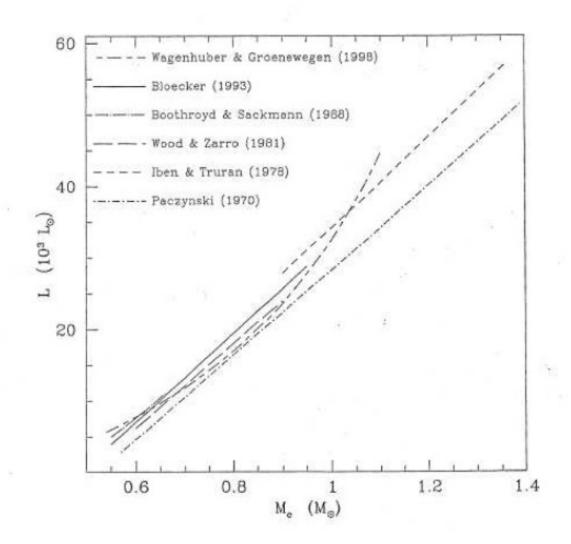
 $L_{\rm AGB} = 5.9 \times 10^4 (M_{\rm c} - 0.52)$ L_{\odot}

 The relation is due to the fact that the envelope is so extended that it becomes irrelevant for the energy producing region.

L-M_c relations exist for all giant phases, but on RGB: $L \propto M_c^8$. On the AGB this becomes $L \propto M_c$ because the higher luminosity leads to a domination of radiation pressure.

L-M_c Relations

Paczynski's relation was theoretically derived. Later L-M relations followed from stellar evolution calculations or 'synthetic evolution calculations', fitted to observations.



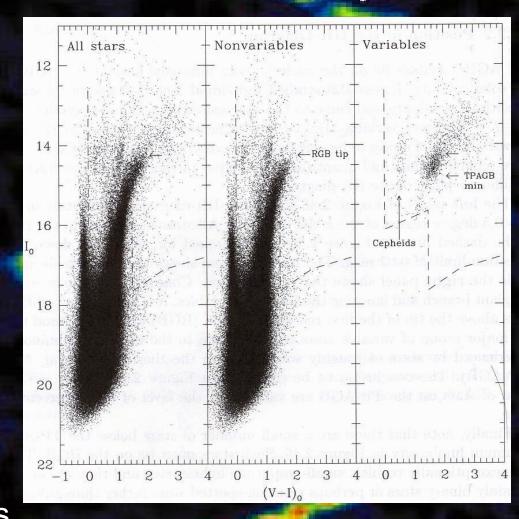
Luminosities Limits

AGB

 $L_{min} = 2800 L_{\odot}$ $L_{max} = 51000 L_{\odot}$

RGB: _ L_{max}= 2900 L_☉

Tip of the RGB is a useful concept for studying populations in other galaxies, but confusion with AGB stars may occur.



Luminosity - Colour Diagram

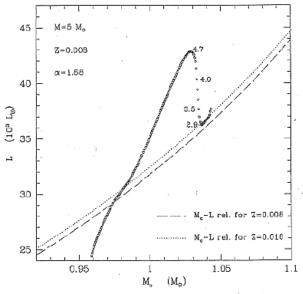
Life Times

TABLE 1 LIFETIMES OF MAJOR EVOLUTIONARY PHASES

| М | | - | - | - | | | | | τ_{FGB-C} | τ_{AGB} | τ _{tpagb} | τ_{AGB} |
|-------------------|-------|-------------------------|----------------------------|-------------------------------------|--------------------------|---------------------------|----------------------------|-------------------|------------------|--------------------|--------------------|------------------|
| (M _☉) | Ζ | τ _{MS} (yr) | τ _{FGB-C} (yr) | ^τ _{FGB} (yr) | τ _{нев} (yr) | τ _{EAGB} (yr) | τ _{традв} (уг) | τ_{AGB} (yr) | $\tau_{\rm HeB}$ | τ _{FGB-C} | τ_{eagb} | $\tau_{\rm HeB}$ |
| 1.0 | 0.016 | 1.125E + 10 | 5.786E+07 | 3.563E+09 | 1.416E + 08 | 1.209E+07 | 4.946E+05 | 1.258E+07 | 0.409 | 0.218 | 0.041 | 0.089 |
| 1.5 | 0.016 | 2.742E + 09 | 5.197E+07 | 7.570E+08 | 1.359E+08 | 9.191E+06 | 8.266E + 05 | 1.002E + 07 | 0.373 | 0.193 | 0.090 | 0.038 |
| 2.0 | 0.016 | 1.236E + 09 | 5.454E+07 | 1.648E+08 | 1.509E+08 | 7.933E+06 | 1.175E + 06 | 9.108E+06 | 0.361 | 0.167 | 0.148 | 0.060 |
| 2.5 | 0.016 | 6.192E + 08 | 1.429E + 08 | 4.283E+07 | 2.805E + 08 | 1.084E + 07 | 2.184E + 06 | 1.303E + 07 | 0.051 | 0.911 | 0.201 | 0.046 |
| 3.5 | 0.016 | 2.307E + 08 | 1.669E + 06 | 1.110E + 07 | 9.142E + 07 | 2.793E+06 | 4.270E + 05 | 3.220E+06 | 0.018 | 1.929 | 0.153 | 0.035 |
| 5.0 | 0.016 | 9.560E+07 | 3.638E+05 | 2.578E + 06 | 2.353E+07 | 1.145E + 06 | 2.624E + 05 | 1.408E + 06 | 0.015 | 3.869 | 0.229 | 0.060 |
| 0.945 | 0.008 | 1.052E + 10 | 6.094E+07 | 3.038E+09 | 1.356E+08 | 1.057E+07 | 5.704E+05 | 1.114E + 07 | 0.449 | 0.183 | 0.054 | 0.082 |
| 1.0 | 0.008 | 8.129E + 09 | 4.860E+07 | 2.776E+09 | 1.336E + 08 | 9.600E+06 | 6.502E + 05 | 1.025E + 07 | 0.364 | 0.211 | 0.068 | 0.077 |
| 1.5 | 0.008 | 2.461E + 09 | 3.450E+07 | 5.140E+08 | 1.304E + 08 | 7.783E+06 | 9.385E + 06 | 8.721E + 06 | 0.265 | 0.253 | 0.121 | 0.067 |
| 2.0 | 0.008 | 1.018E + 09 | 4.458E+07 | 1.286E + 08 | 1.520E + 08 | 1.340E + 07 | 1.339E + 06 | 1.474E + 07 | 0.293 | 0.331 | 0.100 | 0.097 |
| 2.5 | 0.008 | 5.170E+08 | 9.028E+06 | 3.355E+07 | 2.209E + 08 | 1.035E + 07 | 1.827E + 06 | 1.217E + 07 | 0.041 | 1.349 | 0.177 | 0.055 |
| 3.5 | 0.008 | 2.009E + 08 | 1.100E + 06 | 9.042E+06 | 6.388E+07 | 3.032E + 06 | 3.509E+05 | 3.383E+06 | 0.017 | 3.075 | 0.116 | 0.053 |
| 5.0 | 0.008 | 8.567E + 07 | 2.496E+05 | 2.426E + 06 | 2.161E + 07 | 8.036E+05 | 3.601E+05 | 1.150E+06 | 0.012 | 4.662 | 0.448 | 0.053 |
| 0.89 | 0.004 | 1.096E + 10 | 6.276E+07 | 2.617E+09 | 1.294E+08 | 1.127E + 07 | 7.711E+05 | 1.204E + 07 | 0.485 | 0.192 | 0.068 | 0.093 |
| 1.0 | 0.004 | 6.650E + 09 | 5.872E+07 | 2.111E + 09 | 1.279E + 08 | 8.008E+06 | 8.684E+05 | 8.875E + 06 | 0.459 | 0.151 | 0.108 | 0.069 |
| 1.5 | 0.004 | 2.088E + 09 | 3.650E+07 | 4.202E + 08 | 1.268E + 08 | 6.302E + 06 | 9.667E+05 | 7.269E + 06 | 0.288 | 0.199 | 0.153 | 0.057 |
| 2.0 | 0.004 | 8.930E+08 | 3.693E+07 | 1.082E + 08 | 1.539E + 08 | 6.705E + 06 | 1.559E + 06 | 8.264E+06 | 0.240 | 0.224 | 0.233 | 0.054 |
| 2.5 | 0.004 | 4.604E + 08 | 5.953E+06 | 2.745E + 07 | 1.669E + 08 | 5.149E + 06 | 1.248E + 06 | 6.397E + 06 | 0.036 | 1.075 | 0.242 | 0.038 |
| 3.5 | 0.004 | 1.844E + 08 | 7.070E+05 | 6.868E+06 | 5.355E + 07 | 2.150E + 06 | 2.524E + 05 | 2.402E + 06 | 0.013 | 3.398 | 0.117 | 0.045 |
| 5.0 | 0.004 | 8.058E+07 | 1.759E+05 | 2.180E + 06 | 1.864E + 07 | 5.924E+05 | 3.123E+05 | 9.205E+05 | 0.009 | 5.143 | 0.527 | 0.049 |
| 1.0 | 0.001 | 5.737E+09 | 3.436E+07 | 1.344E+09 | 1.211E + 08 | 7.737E+06 | 1.357E+06 | 9.094E+06 | 0.284 | 0.265 | 0.175 | 0.075 |
| 1.5 | 0.001 | 1.603E + 09 | 3.633E+07 | 3.606E+08 | 1.222E + 08 | 4.962E + 06 | 1.127E + 06 | 6.088E + 06 | 0.297 | 0.168 | 0.227 | 0.050 |

Hot Bottom Burning

- This process happens in the more massive AGB stars (>5 M_☉, for solar metallicity Z=Z_☉, lower for lower metallicity).
 - It involves the base of the convective zone being involved in H-burning.
- HBB breaks the L-M_c relation, so the higher mass stars do not follow this relation. The observational evidence for this process comes from certain abundance variations.
- As well as the lack of high mass C-stars (see later).

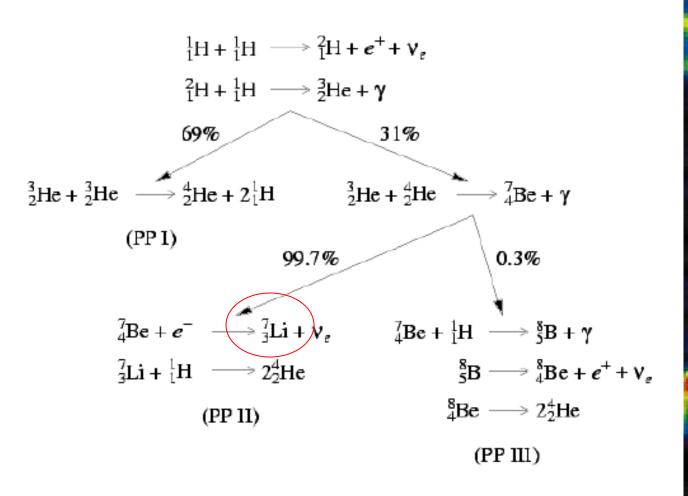


HBB: Abundance Effects

- Since the H-burning occurs at the base of the convective envelope, it leads to changes in the surface abundances. Partly these are similar to the effects of the 1st and 2nd dredge-up, ⁴He↑ ¹²C↓ ¹³C↑ ¹⁴N↑
 - The reduction of ¹²C influences the formation of C-stars (see below).

However, also partial products can now enter the stellar envelope. The most interesting one is ⁷Li, which is an intermediate product of the pp-chain. Stars with increased ⁷Li have been found in both the MW and the Magellanic Clouds. The cosmic abundance of ⁷Li is important because it connects to big bang nucleosynthesis.

PP Chain



Third Dredge-Up

- As the convective envelope gets pushed out during a TP, and later moves back in again, formerly intershell material may end up in the stellar envelope. This is known as the 3rd Dredge-Up.
 - The difference with the other dredge-up events is that this material has been involved in He-burning, so the types of isotopes that are dredged up are very different. The most notable of these are
 - ¹²C

- s-process elements

3DUP Efficiency

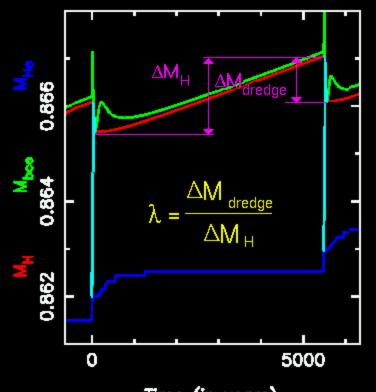
The efficiency of the 3rd dredge-up is parametrized

via

 $\lambda = \frac{\Delta M_{\rm dredge-up}}{\Delta M_{\rm c}}$

This efficiency is not well known, but falls in the range 0.3 – 1.0.
It can be calibrated with measured abundances in AGB star populations.

M=5 Z=0.02



Time (in years) _{© John Lattanzio 2001}

Formation of Carbon Stars

- The most dramatic effect of the 3DUP is the formation of Carbon stars.
 - Since the early days of stellar spectroscopy (1860s, A. Secchi) a group of red stars with spectra dominated by lines of carbon molecules, has been known. This is peculiar since usually C/O < 1.
 - Only in the 1970s it was shown that the 3DUP can bring so much C that the abundance ratio C/O>1.
 - This requires a minimum number of TPs, so there is a minimum mass, \sim 1.5 M $_{\odot}$.
- HBB can turn the ¹²C in the envelope into ¹⁴N, so there is also a maximum mass, ~5 M_☉.

Surface Abundance Changes: 2.5 M_o

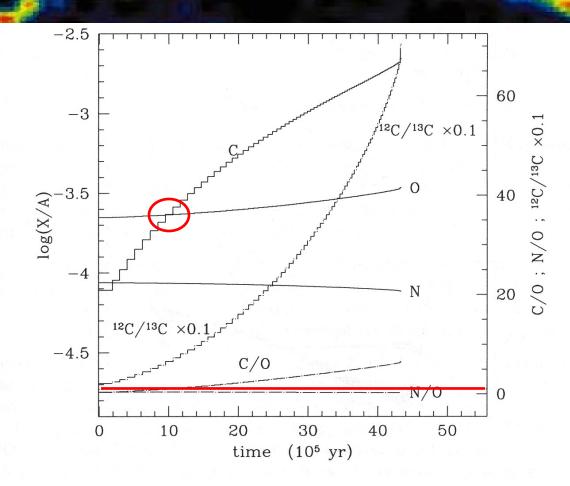
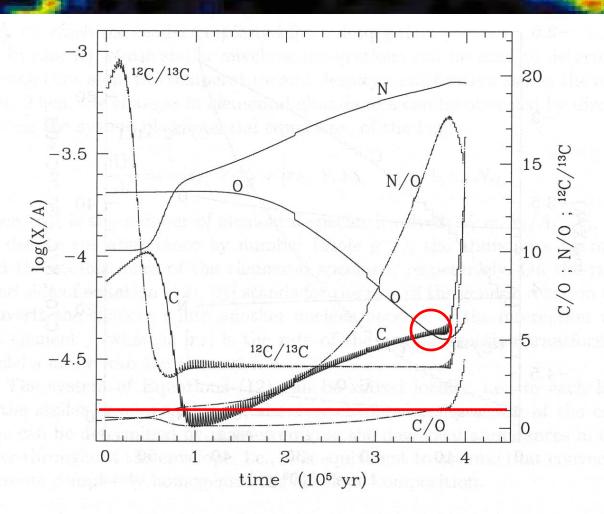
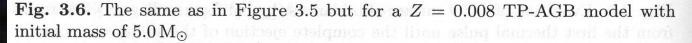


Fig. 3.5. Evolution of CNO surface abundances (by number, mole gr⁻¹) and ratios from the first thermal pulse until the complete ejection of the stellar envelope for Z = 0.008 TP-AGB model with initial mass of $2.5 M_{\odot}$. The efficiency parameter for the third dredge-up is assumed to be $\lambda = 0.5$; the mixing-length parameter is $\alpha = 2.0$. Based on synthetic calculations by [63]

Surface Abundance Changes: 5 M_o





The s-process

- Spectra of AGB stars also can show increased abundances of elements heavier than Fe: Zr, Ti, Tc.
- Nuclear burning does not produce elements heavier than Fe/Ni, since these have the highest binding energy per nucleon.
- These elements can only form through neutron capture.
- If the neutron flux is low, unstable nuclei will decay before capturing another neutron: slow neutron capture or s-process. Produces most stable isotopes.

Decay through β decay or inverse β decay:

 $^{210}\text{Bi} \rightarrow ^{210}\text{Po} + e^- + \bar{\nu}_e$

$$\rightarrow^{13} \mathrm{N} \longrightarrow^{13} \mathrm{C} + e^+ + \nu_e$$

Stepping through the Isotopes

| | | | | | | at reserves to | | | 1 12682 C | 1733 (1737 - 1 | 10000 | N |
|---|----------------|---|-----------------------|--|-----------------|----------------|-----------------|-------------------|------------------|------------------|-------------------|--------------------|
| | Se68 | Se69 | Se70 | Se71 | Se72 | Se73 | Se74 | Se75 | Se76 | Se77 | Se78 | Se79 |
| | 35,5 8 | 27.4 s (3/2+) | 41.1 m 0+ | 4.54 m 3/2-5/2- | 8.40 d 0+ | 7.15 h 9/2+ | 0+ | 119.779 d 5/2+ | 0+ | all. | | 1. DE6 y |
| | EC | ECp | EC | EC | EC | ec * | 0.89 | EC | 9.36 | 7.63 | 23.78 | ₩ B- |
| H | TAXING MALES | 000000000000000000000000000000000000000 | and the second second | 111 Contraction of the local sectors of the local s | | 141 C | | White- | | | Contract Contract | |
| 1 | As67 42.5 s | As68 151.6 x | As69 15.2 m | As70 52.6 m | As71 65.28 h | As72 26.0 h | As73 80.30 d | As74 17.77 d | As75 | As76 129778 d | As77 38.83 h | As78 90.7 m |
| | (5/2+) | 3+ | 5/2+ | 4(+) | 5/2+ | 2. | 3/2+ | 2 | 32 | | 3/2+ | 2. |
| | EC | EC | EC | EC | EC | EC | EC | EC.B | 100 | β. | p. | β- |
| | Ge66 | Ge67 | Ge68 | Ge69 | Ge70 | Ge71 | Ge72 | Ge73 | Ge74 | Ge75 | Ge76 | Ge77 |
| | 2.26 h 0+ | 18.9 m 1/2+ | 270,8 d 0+ | 39,05 h 5/2- | (Helle | 11.43 d | (r+ | | | 82.78 m | 0+ | 11.30 h 7/2+ |
| | and the second | | | 1.1.1.1 | | \$ | 30 | # | 1.1.1.1.1 | * | 11112 | * |
| | EC | EC | EC | EC | 21,23 | EC | 27.66 | 7.73 | 35,94 | ħ. | 7.44 | p |
| | Ga65 15.2 m | Ga66 9.49 h | Ga67 3.2612 d | Ga68 67.629 m | Ga69 | Ga70 2h14 m | Ga71 | Ga72 | Ga73 4.86 h | Ga74 8.12 m | Ga75 120 s | Ga76 32.6 s |
| | 3/2- | 0+ | 3/2- | 1+ | 3/2 | 2014.00 | × _ | Parto n | 3/2- | (3-) | 3/2- | (2+.3+) |
| | FC | EC | EC | EC | 60.108 | EC.5 | 39.892 | * | R. | * | 14. | R. |
| | Zn64 | Zn65 | Zn66 | Zn67 | Zn68 | Zn69 | Zn70 | Zn71 | Z.n72 | Zn73 | Zn74 | Zn75 |
| | 2004 | 244.26 d | 2,1100 | Zno/ | 2000 | 4.4 m | 14 y | 2.45 m | 46.5 h | 23.5 \$ | 95.6 5 | 10.2 s |
| | 0.+ | 5/2+ | 0. | 14 | -04 | - J. | | | 0.4 | (1/2)= | 0+ | (7/24) |
| | 48.6 | EC | 27.9 | 4.1 | 18.8 | þ- | 0.6 | ß | β- | β- | ₿. | |
| | Cu63 | Cu64 | Cu65 | Cu66 | Cu67 | Cu68 | Cu69 | Cu70 | Cu71 | Cu72 | Cu73 | Cu74 |
| | 3/2 | 11,000 | N | 3098 m | 61.83 h 3/2- | 31.1 8 | 2.85 m 3/2- | 4.5 s (1+) | 19.5 s (3/2-) | 6.6 s (1+) | 3.9 s | 1.594 s (1+.3+) |
| | | | | 23 | JA 24 | 1+ 8 | 342- | * | 10:2+7 | (1+) | iii | (Terster) |
| | | EC.B | 30.83 | β- | β- | ĝr- | ₽ | В | β | 1P | Þ. | B/ |
| | Ni62 | Ni63 | Ni64 | Ni65 26172 h | Ni66 54.6 h | Ni67 21 s | Ni68 19 s | Ni69 11.4.5 | Ni70 | Ni71 1.86 s | Ni72 2.1 s | Ni73 0.90 s |
| | 0+ | 1/2- | | 2001/20 | 04 | (1/2-) | 04 | 11.45 | 0.4 | 1.80 \$ | 0+ | 0.90 8 |
| | 3.634 | B | 0.926 | 8- | 8 | ße | B | B | | B | 8 | B |
| - | 0.004 | | 11.760 | M/ | W | | I.W. | 11/ | | LW_ | 1 H | 140 |

Limit of the s-process

 The s-process cannot produce elements heavier than Pb (Z=82) since at Pb there is a closed loop in the decay scheme:

 $\begin{array}{c} ^{209}\mathrm{Bi}+n \rightarrow ^{210}\mathrm{Bi}+\gamma \\ ^{210}\mathrm{Bi} \rightarrow ^{210}\mathrm{Po}+e^-+\bar{\nu}_e \\ ^{210}\mathrm{Po} \rightarrow ^{206}\mathrm{Pb}+^4\mathrm{He} \\ \end{array}$ $\begin{array}{c} ^{206}\mathrm{Pb}+3n \rightarrow ^{209}\mathrm{Pb} \\ ^{209}\mathrm{Pb} \rightarrow ^{209}\mathrm{Bi}+e^-+\bar{\nu}_e \end{array}$

Heavier elements require the r-process (operating in SN explosions).

Spectroscopic Evidence

- AGB stars can show clear signs of s-process elements: ZrO, TiO. Stars which show these lines particularly prominently get a special spectroscopic classification: S-stars.
 - The most convincing evidence for the s-process in AGB stars is the detection of Tc lines. Tc (Z=43) does not have any stable isotopes. The stablest isotope is 99 Tc with a half life of 2×10⁵ years.

As s-process elements have the same origin as the increase in the C abundance, it is thought that there is an evolutionary sequence $M \rightarrow S \rightarrow C$.

Neutron Source

- Although the evidence for the operation of the s-process is convincing, the process itself is not fully understood.
- The problem lies with the source of neutrons which is needed for the s-process.

Best candidates:

$$^{13}\text{C} + ^{4}\text{He} \rightarrow ^{16}\text{O} + n$$

 $^{22}\text{Ne} + ^{4}\text{He} \rightarrow ^{25}\text{Mg} + n$

← Only in higher mass stars

To make ¹³C we need protons, but only just enough!!

 ${}^{12}\mathrm{C} + p \rightarrow {}^{13}\mathrm{N} + \gamma \rightarrow {}^{13}\mathrm{C} + e^+ + \nu_e$

 $^{13}\mathrm{C} + p \rightarrow ^{14}\mathrm{N} + \gamma$

← and gone it is!!!

The ¹³C Pocket

 Two consecutive TPs needed to get the s-process elements out.

