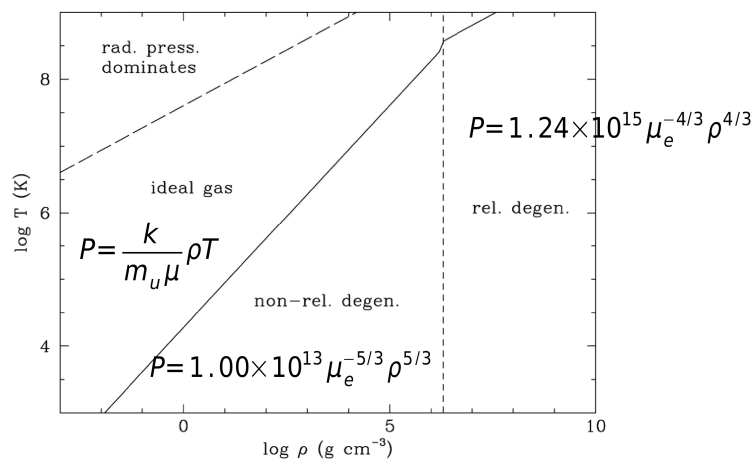


Outline of massive stars & supernovae

- Physics of massive stars
- Structure and evolution up to core collapse
- Core collapse, explosion
- Observational aspects of supernovae
- Circumstellar interaction of SNe
- Thermonuclear SNe = Type Ia SNe
- Gamma-ray bursts

Equation of state



Difference between massive and low mass stellar evolution = core evolution

$$P \approx \frac{k}{\mu_e m_p} \rho T + K_\gamma \left(\frac{\rho}{\mu_e} \right)^\gamma$$

$$\frac{dP}{dr} = -\frac{Gm(r)\rho}{r^2} \Rightarrow P_c \approx \frac{GM_c \rho_c}{R_c}$$

$$P_c \approx f GM_c^{2/3} \rho_c^{4/3} \quad f=0.364 \quad \gamma=4/3$$

$$\frac{k}{\mu_e m_p} T_c \approx f GM_c^{2/3} \rho_c^{1/3} - K_\gamma \rho_c^{\gamma-1} \mu_e^{-\gamma}$$

Low density: perfect gas

$$kT_c \approx f G \mu_e m_p M_c^{2/3} \rho_c^{1/3}$$

High density: ER degenerate $\gamma=4/3$

$$M_{Ch} \approx \left(\frac{K_{4/3}}{fG} \right)^{3/2} \mu_e^{-2} = 5.85 \mu_e^{-2}$$

Chandrasekhar mass

$$\frac{k}{m_p} T_c \approx \left(\frac{\rho_c}{\mu_e} \right)^{1/3} \left[K_{4/3} \left(\frac{M_c}{M_{Ch}} \right)^{2/3} - K_\gamma \left(\frac{\rho_c}{\mu_e} \right)^{\gamma-4/3} \right]$$

If $\gamma > 4/3$ then this has a max.

I. $M_c < M_{Ch}$ i.e., low mass stars: Gas NR $\gamma=5/3$

$$\frac{k}{m_p} T_c \approx K_{4/3} \left(\frac{\rho_c}{\mu_e} \right)^{1/3} \left(\frac{M_c}{M_{Ch}} \right)^{1/3} - K_{5/3} \left(\frac{\rho_c}{\mu_e} \right)^{2/3}$$

Temperature max at

$$\frac{\rho_{c,max}}{\mu_e} = \left(\frac{K_{4/3}}{2K_{5/3}} \right)^3 \left(\frac{M_c}{M_{Ch}} \right)^2$$

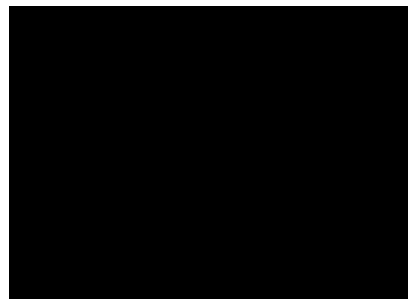
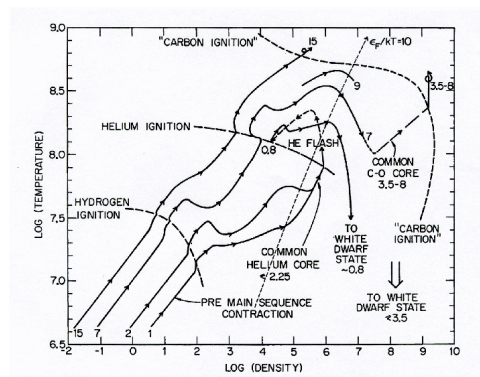
where

$$T_{c,max} = \frac{m_p K_{4/3}^2}{4 k K_{5/3}} \left(\frac{M_c}{M_{Ch}} \right)^{4/3} \approx 4.7 \times 10^8 \left(\frac{M_c}{M_{Ch}} \right)^{4/3} \text{ K}$$

II. $M_c > M_{Ch}$ i.e., high mass stars: Gas ER $\gamma=4/3+\epsilon$ $\epsilon \ll 1$

$$T_c \propto \left(\frac{\rho_c}{\mu_e} \right)^{1/3}$$

Core temperature rises monotonically

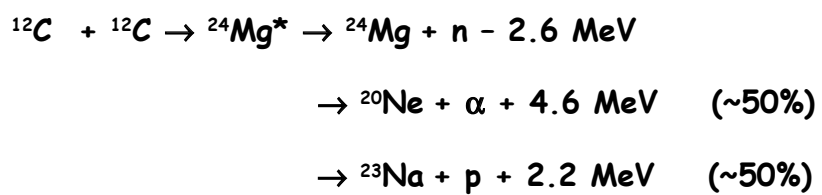


Conclusion

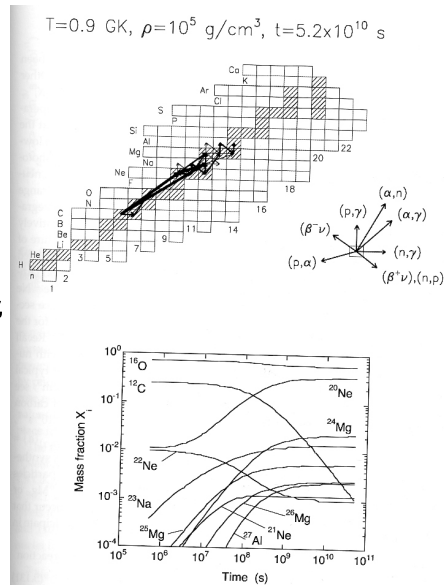
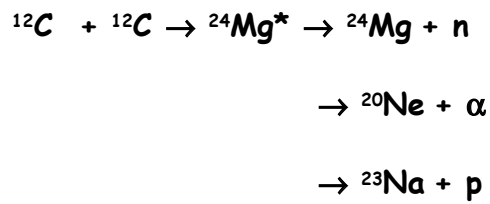
Main difference between low and high mass evolution:
Low mass stars ($M < 8-10 M_{\odot}$) never reach high enough
temperature to ignite carbon

Stellar nucleosynthesis

Carbon burning $T \sim (0.6-1.2) \times 10^9 \text{ K}$

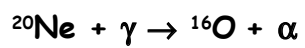


$$dQ/dt \propto T^{29}$$

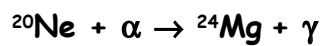
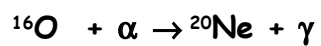


Neon burning $T \sim 1.5 \times 10^9 \text{ K}$

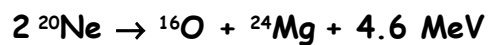
First



Then



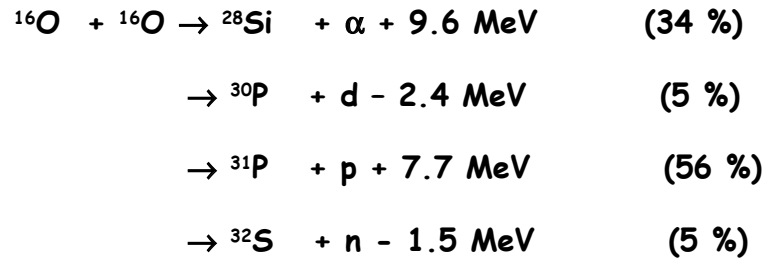
In summary,



$$dQ/dt \propto T^{50}$$

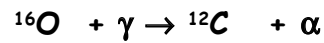
Oxygen burning $T \sim 2 \times 10^9 \text{ K}$

I. Hydrostatic O-burning: Fusion dominates



But, ${}^{31}\text{P} + \alpha \rightarrow {}^{28}\text{Si} + \gamma$ $dQ/dt \propto T^{33}$

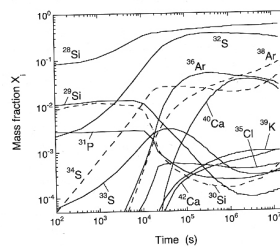
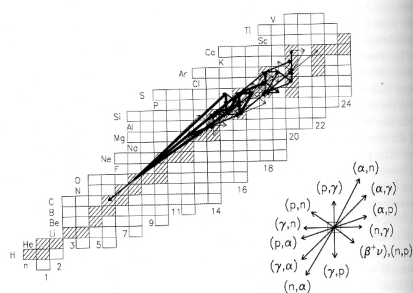
II. Explosive O-burning: Photodisintegration dominates



Main products:

${}^{28}\text{Si}$ and ${}^{32}\text{S}$

$T = 2.2 \text{ GK}$, $\rho = 3 \times 10^6 \text{ g/cm}^3$, $t = 1.4 \times 10^{-7} \text{ s}$



Silicon burning $T \sim 3.5 \times 10^9 \text{ K}$

I. Photodisintegration. Si melting



II. Creates α particles

These are used to build heavier α elements



Quasi equilibrium between forward and backward reactions

If run to **nuclear statistical equilibrium (NSE)** end-result will be iron peak elements

$$dQ/dt \propto T^{49}$$

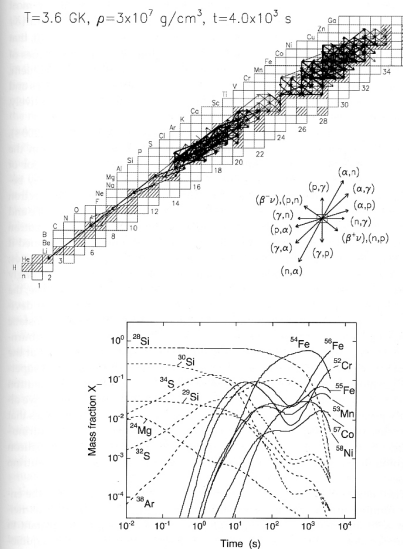


Fig. 5.52 Time-integrated net abundance flows (top) and abundance evolutions (bottom) for a constant temperature and density of $T = 3.6 \text{ GK}$ and $\rho = 3 \times 10^7 \text{ g/cm}^3$, respectively. Such conditions are typical of core silicon burning in stars with an initial mass of $M = 25 M_{\odot}$ and with initial solar metallicity. The reaction network is solved numerically

until the silicon fuel is exhausted ($X_{\text{Si}} < 0.001$ after $\approx 4000 \text{ s}$). The arrows in the top part have the same meaning as in Fig. 5.44. The abundance flows in the top part of the figure reflect the existence of two quasiequilibrium clusters in the $A = 25\text{--}40$ and $A = 46\text{--}64$ mass ranges.

Saha: Ionization equilibrium

$$n_i + \gamma \leftrightarrow n_{i+1} + e^-$$

$$\frac{n_{i+1} n_e}{n_i} = \frac{G_{i+1} g_e}{G_i} \frac{(2\pi m k T)^{3/2}}{h^3} e^{-\chi_i / k T} \quad m = \frac{m_e m_{i+1}}{m_e + m_{i+1}}$$

Nuclear Statistical Equilibrium (NSE)

Remove (add) a neutron

$$n_{Z,A} + \gamma \leftrightarrow n_{Z,A-1} + n$$

$$\frac{n_{Z,A-1} n_n}{n_{Z,A}} = \frac{2G_{Z,A-1}}{G_{Z,A}} \frac{(2\pi m_{Z,A-1} m_n k T)^{3/2}}{h^3 m_{Z,A}^{3/2}} e^{-Q_n / k T}$$

$$Q_n = (m_{Z,A-1} + m_n - m_{Z,A}) c^2$$

$$\frac{n_{Z,A-1} n_n}{n_{Z,A}} = \frac{2G_{Z,A-1}}{G_{Z,A}} \left(\frac{A-1}{A} \right)^{3/2} \theta e^{-Q_n / k T}$$

$$\theta = (2\pi m_n k T)^{3/2} / h^3$$

Remove (add) a proton

$$n_{Z,A-1} + \gamma \leftrightarrow n_{Z-1,A-2} + p$$

$$\frac{n_{Z-1,A-1} n_n}{n_{Z,A-1}} = \frac{2G_{Z-1,A-2}}{G_{Z,A-1}} \left(\frac{A-2}{A-1} \right)^{3/2} \theta e^{-Q_p / k T}$$

$$Q_p = (m_{Z-1,A-2} + m_p - m_{Z,A-1}) c^2$$

Continue!

$$n_{Z,A} = G_{Z,A} \frac{A^{3/2} n_p^Z n_n^{A-Z}}{2^A} \theta^{1-A} e^{Q_{Z,A}/kT}$$

$$Q_{Z,A} = (Zm_p + (A-Z)m_n - m_{Z,A})c^2$$

$$\theta = (2\pi m_n kT)^{3/2} / h^3$$

+ Number conservation!

$$n_e = \sum_i Z_i n_{Z_i, A_i} \quad \rho = m_u \sum_i A_i n_{Z_i, A_i}$$

Define

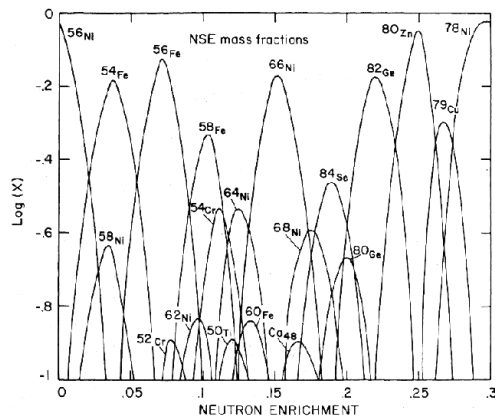
$$X_i = \frac{n_i A_i m_u}{\rho} \quad Y_e = \frac{n_e m_u}{\rho}$$

$$\sum_i X_i = 1 \quad Y_e = \sum_i Z_i \frac{X_i}{A_i}$$

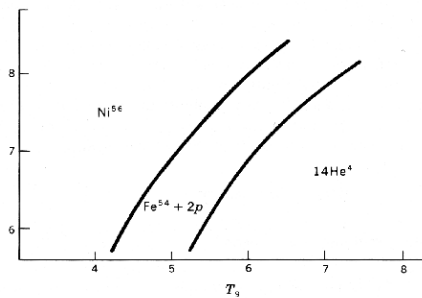
Neutron excess

$$\eta = \frac{n_n - n_p}{n_n + n_p} = 1 - 2Y_e$$

Rule: The most tightly bound nucleus for a given neutron excess is favored. For $\eta=0$ the most ^{56}Ni (28 n + 28 p, doubly magic) is most bound. For $\eta=0.07$ ^{56}Fe [(30 - 26)/56=0.071]

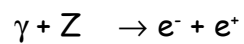
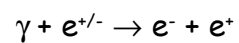


Photodisintegration

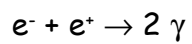


Neutrino cooling

$T \sim m_e c^2/k \sim 5 \times 10^9 \text{ K}$ electron/positron pair creation



Most often



Sometimes, weak interaction

$$e^+ + e^- \rightarrow \nu_e + \bar{\nu}_e$$

$$\sigma \approx 10^{-44} \left(\frac{E}{m_e c^2} \right)^2 \text{ cm}^2$$

Pair production

$$\varepsilon \approx 4.9 \times 10^{18} T_9^3 e^{-11.86/T_9} \quad T < 10^9$$

$$\varepsilon \approx 4.5 \times 10^{15} T_9^9 \quad T > 3 \times 10^9$$

Plasma neutrino cooling

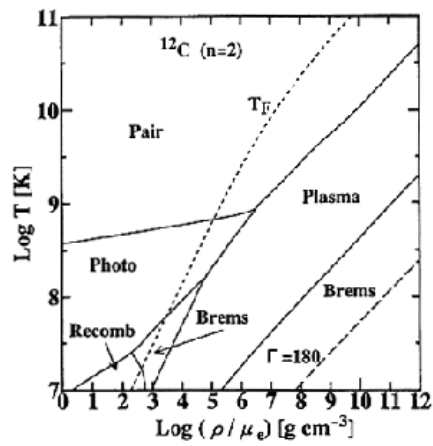
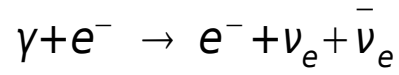
Dispersion relation for a photon in a plasma

$$\omega^2 = k^2 c^2 + \omega_{pl}^2$$
$$\omega_{pl} = \left(\frac{4\pi n_e e^2}{m_e} \right)^{1/2} = 5.6 \times 10^4 n_e^{1/2} \quad \text{Hz}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

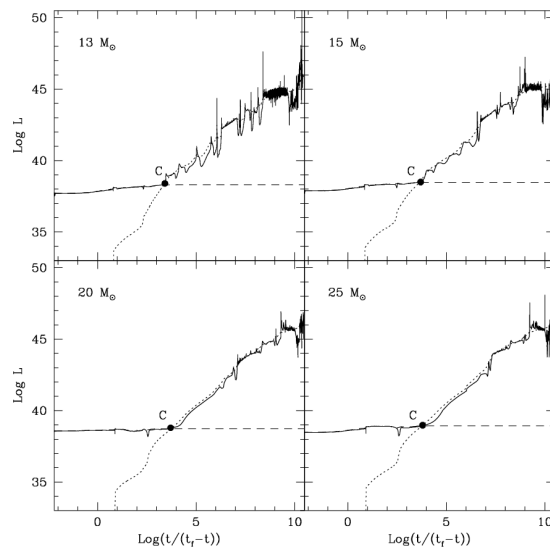
The photon behaves if it had a mass which can be used for pair production of neutrinos

Photo neutrino



Pair most important
for massive stars
Plasma for lower masses

Neutrino vs photon luminosity



Carbon burning and
later dominated by
neutrino cooling!!

$$\tau_i = \frac{Y_i q_i}{\epsilon_i}$$

Table 3: **Estimates of the duration of the advanced burning stages**

Burning stage	$q_i/10^{17}$ erg g ⁻¹	Y_i	T_i 10 ⁹ K	$\rho/10^6$ g cm ⁻³	ϵ_i erg g ⁻¹ s ⁻¹	τ_i s
C	4.0	0.2	0.7	0.3	7.1×10^5	3.6×10^3 yrs
Ne	1.1	0.7	1.4	2.7	3.0×10^9	0.81 yrs
O	5.0	0.2	1.9	6.9	3.5×10^{10}	30 days
Si	1.9	0.5	3.4	39.3	2.4×10^{12}	0.5 days

15 M_⊙

Table 1: **Burning stages for a 15 M_⊙ star (WHW02)**

Fuel	Ashes	T 10 ⁸ K	ρ g cm ⁻³	M M _⊙	L 10 ³ L _⊙	R R _⊙	τ yrs
H	He, N	0.35	5.8	14.9	28.0	6.75	1.1×10^7
He	C,O	1.8	1.4×10^3	14.3	41.3	461.	2.0×10^6
C	Ne, Mg, O	8.3	2.4×10^5	12.6	83.3	803.	2.0×10^3
Ne	O, Mg, Si	16.3	7.2×10^6	12.6	86.5	821.	0.73
O	Si, S	19.4	6.7×10^6	12.6	86.6	821.	2.6
Si	Ni	33.4	4.3×10^7	12.6	86.5	821.	18 days

25 M_⊙

Table 2: **Same as above for a 25 M_⊙ star**

Fuel	Ashes	T 10 ⁸ K	ρ g cm ⁻³	M M _⊙	L 10 ³ L _⊙	R R _⊙	τ yrs
H	He	0.38	3.8	24.5	110.	9.2	6.7×10^6
He	C,O	2.0	7.6×10^2	19.6	182.	1030.	8.4×10^5
C	Ne, Mg	8.4	1.3×10^5	12.5	245.	1390.	5.2×10^2
Ne	O, Mg	15.7	4.0×10^6	12.5	246.	1400.	0.89
O	Si, S	20.9	3.6×10^6	12.5	246.	1400.	0.40
Si	Ni	36.5	3.0×10^7	12.5	246.	1400.	0.73 days

Mass loss I

Early type stars: O-B stars

Radiatively driven winds by UV radiation

UV resonance lines Most important Fe III-V

$$v_w \approx 1000 - 3000 \text{ km s}^{-1} \quad dM/dt \approx 10^{-7} - 10^{-6} M_{\odot} \text{ yr}^{-1}$$

Mass loss II

Red supergiants

Dust driven winds + pulsations (?)

$$v_w \approx 10 - 50 \text{ km s}^{-1} \quad dM/dt \approx 10^{-6} - 10^{-4} M_{\odot} \text{ yr}^{-1}$$

superwinds connected to pulsations (?)

$$dM/dt \approx 10^{-4} - 10^{-3} M_{\odot} \text{ yr}^{-1} \quad \text{duration} < 10^4 \text{ yrs}$$

Wolf-Rayet stars (post-MS stars No H left!)

Pulsations (?) + radiatively driven winds by UV radiation

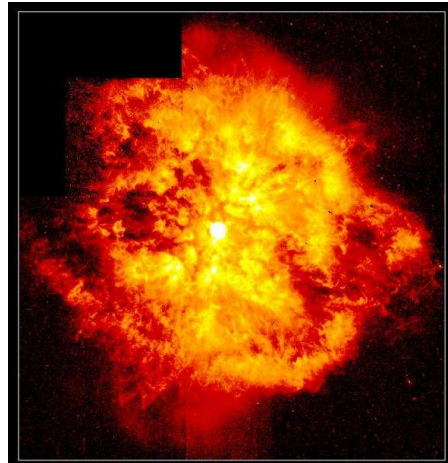
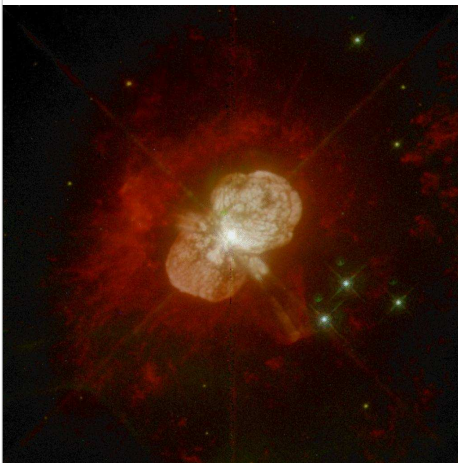
UV resonance lines

Most important Fe III-V

$$v_w \approx 1000 - 3000 \text{ km s}^{-1} \quad dM/dt \approx 10^{-6} - 10^{-5} M_{\odot} \text{ yr}^{-1}$$

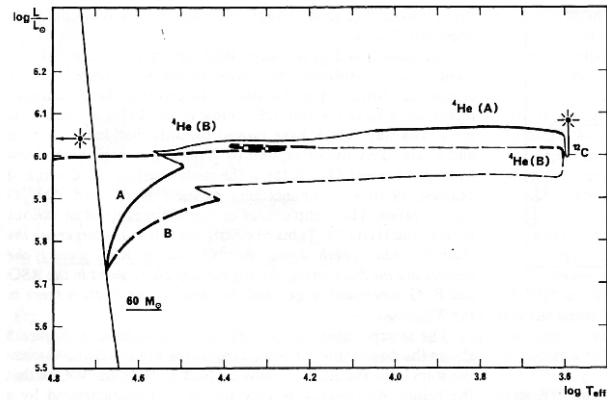
$$\tau_{OB} \sim 10^6 \text{ yrs} \quad \tau_{RSG} \sim 10^5 \text{ yrs} \quad \tau_{WR} \sim 10^5 \text{ yrs}$$

several $M_{\odot}$ lost!



η Carinae LBV $M \sim 100 M_{\odot}$ WR 124 Wolf-Rayet star $M \sim 40 M_{\odot}$

$60 M_{\odot}$



Without mass loss: $O \rightarrow BSG, LBV \rightarrow RSG \rightarrow SN$

With: $O \rightarrow BSG \rightarrow RSG \rightarrow WR \rightarrow SN$

$M > 60 M_{\odot}$ $O \rightarrow LBV \rightarrow WR \rightarrow SN$

Rotation

On MS $v \sim 200 \text{ km s}^{-1}$

Break-up velocity:

$$\frac{V^2}{R} \approx \frac{GM}{R} \Rightarrow V_c \approx \left(\frac{GM}{R} \right)^{1/2}$$

I. Rotation $\rightarrow$ circulation $\rightarrow$ mixing

II. Rotation $\rightarrow$ flattening of star

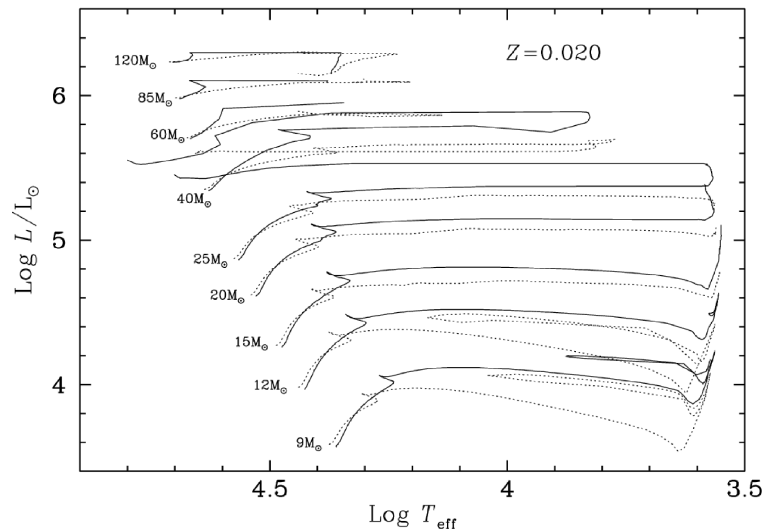
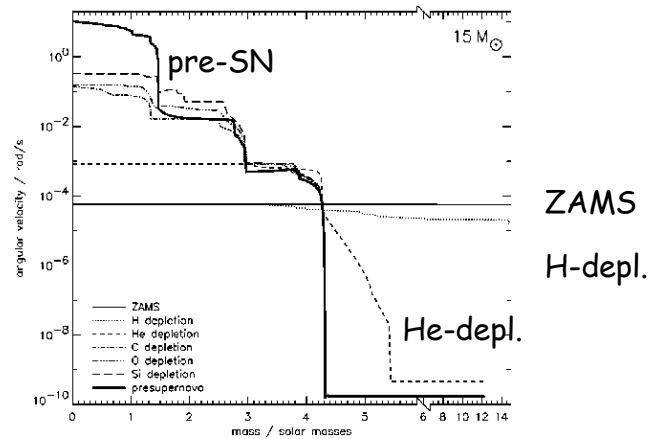
Flux follows grav. potential surfaces (von Zeipel's theorem)

$\Rightarrow$ star more luminous at poles $\Rightarrow$ more mass loss in polar directions

III. On MS solid body rotation

If angular momentum is conserved $\Omega \propto R^{-2}$

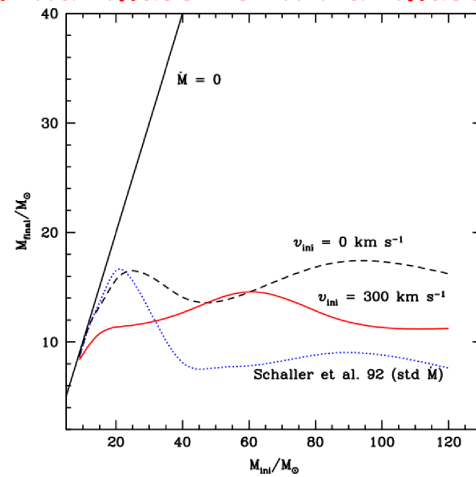
core contracts $\Rightarrow$ spin-up H-envelope expands $\Rightarrow$ slow down



No rotation: $M(\text{WR}) \sim 37 M_{\odot}$

With rotation: $M(\text{WR}) \sim 22 M_{\odot}$

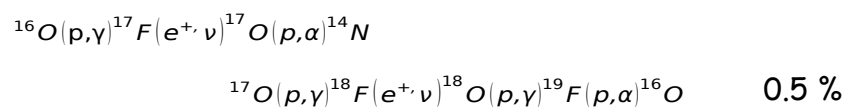
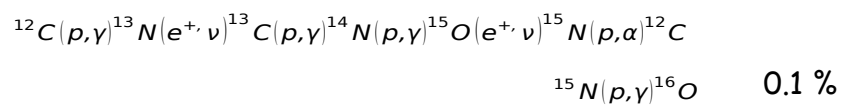
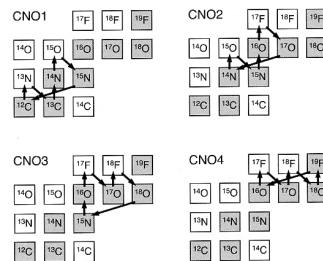
Final mass vs initial mass



Final mass independent of initial mass for large M !!

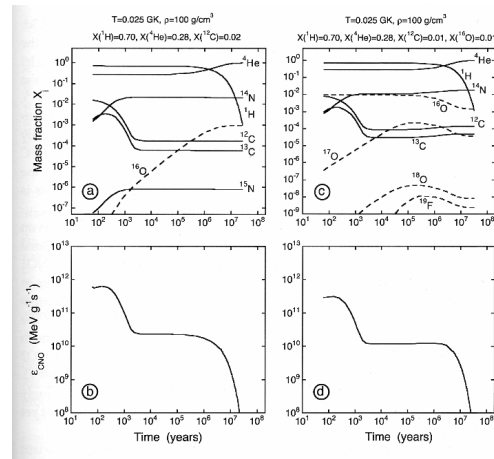
Mainly H-envelope lost. Core mass less affected $\Rightarrow L \sim \text{same}$

CNO burning in massive stars

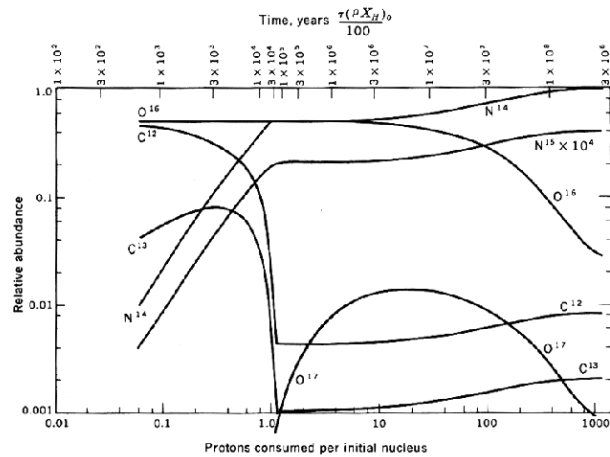


C converted to N and if running long enough also O to N

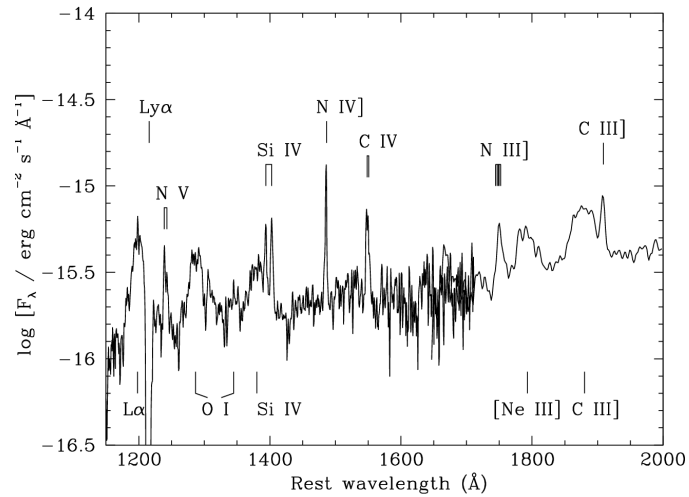
CNO burning in massive stars



C converted to N and if running long enough also O to N



SN 1998S Type IIn

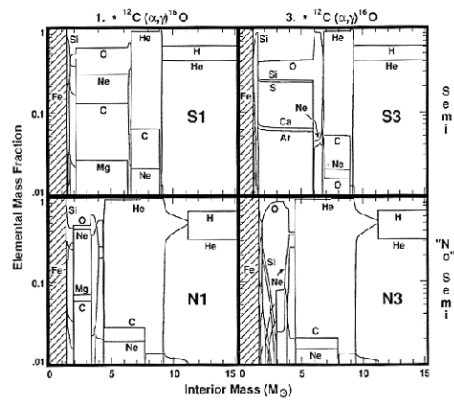


$\text{N/C} \sim 6$ (Sun $\text{N/C} \sim 1/4$)

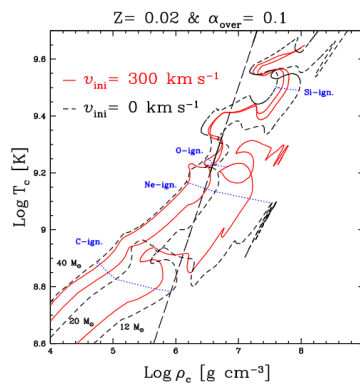
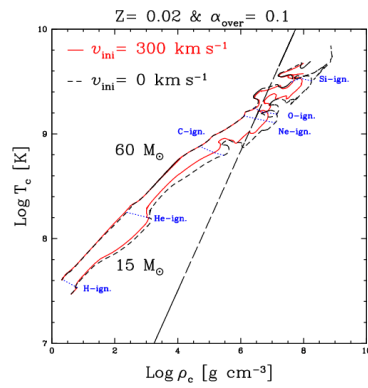
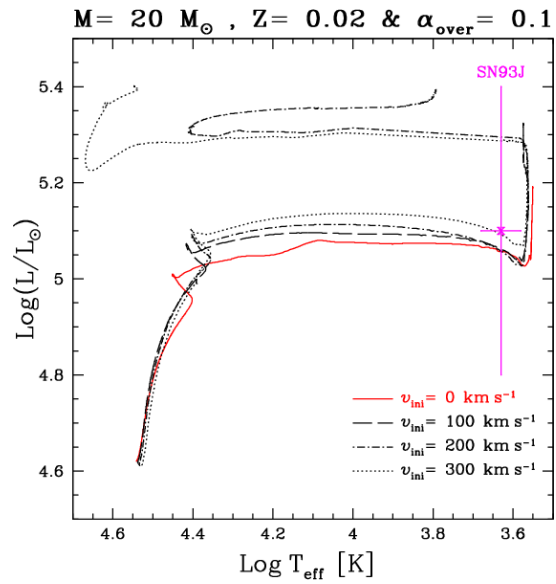
Uncertainties in nuclear reaction rates

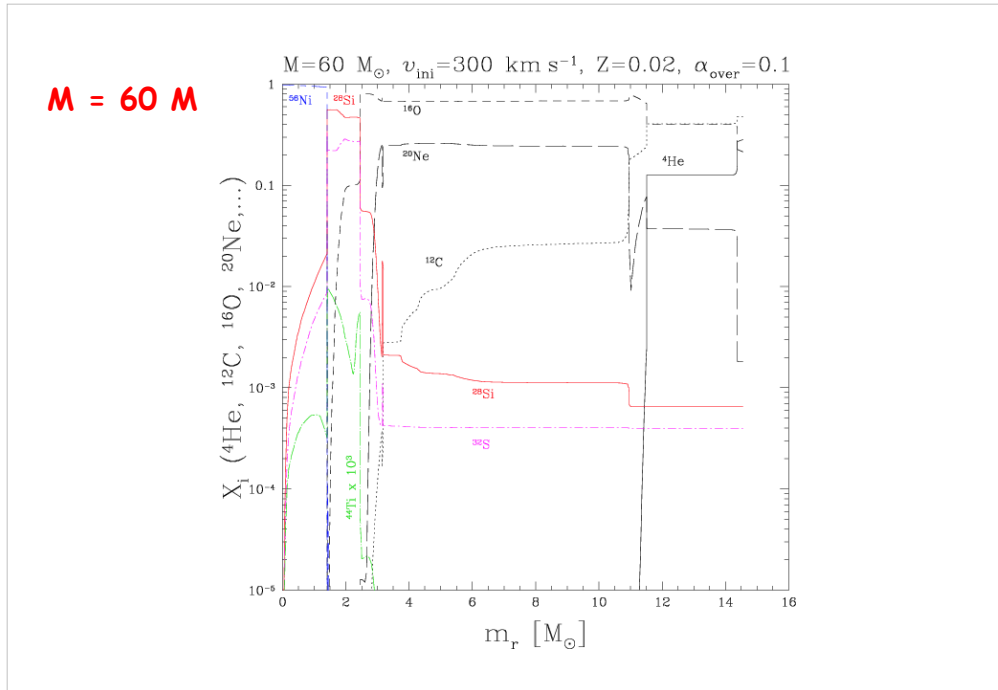
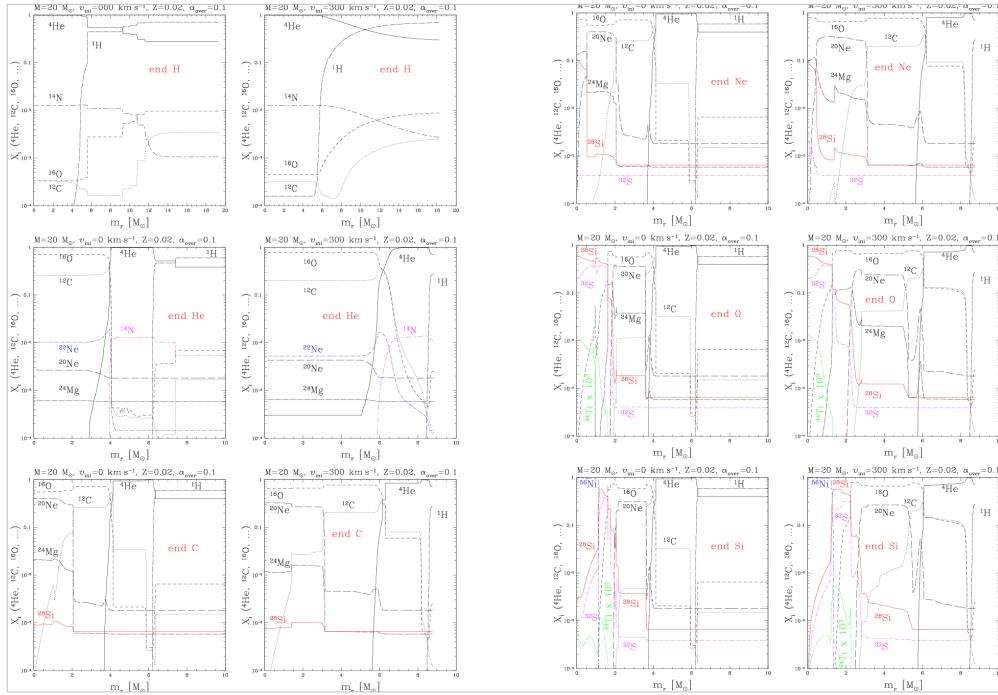
$^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ uncertain by factor of ~ 3

affects C/O and whole evolution after He burning



Example: 20 M





Pre-SN structure

