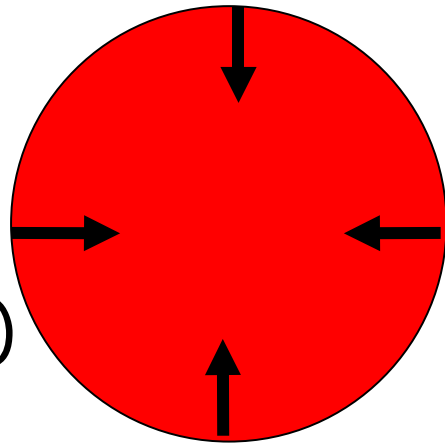


Collapse
(only core
inner $\sim 1.5 M_{\odot}$)
Free-fall



1000 km

$10^{10} \text{ g cm}^{-3}$

Core collapse triggered by
K-captures, photodissociation

Bounce
Shock wave

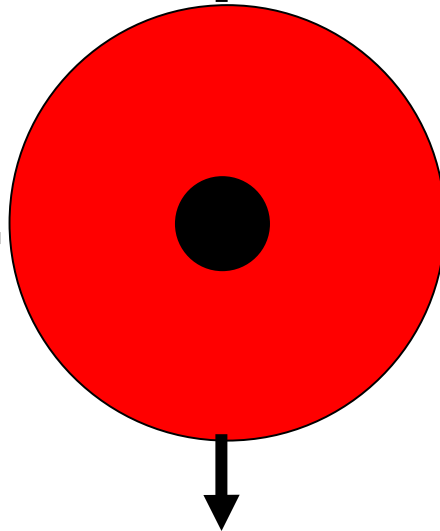


30 km
nuclear dens.
 $\sim 10^{14} \text{ g cm}^{-3}$

Nuclear
repulsion

Explosion

$V \sim 10^4 \text{ km s}^{-1}$



Collapse time scale

$$\tau_{coll} \approx \frac{R}{V_{ff}} \approx 10^{-3} \left(\frac{\rho}{10^{12} \text{ g cm}^{-3}} \right)^{-1/2} \text{ s}$$

Neutrino scattering

elastic scattering of free nucleons

$$\nu + n \rightarrow \nu + n$$

$$\nu + p \rightarrow \nu + p$$

elastic scattering against nuclei (NC)

$$\nu + (Z,A) \rightarrow \nu + (Z,A)$$

inelastic scattering

$$\nu + e \rightarrow \nu + e$$

Free nucleon scattering

$$\sigma = \frac{1}{4} \sigma_0 \left(\frac{E_\nu}{m_e c^2} \right)^2$$

$$\sigma_0 = 1.76 \times 10^{-44} \quad \text{cm}^2$$

Coherent scattering off bound nucleons

$$\sigma = \frac{1}{16} \sigma_0 \left(\frac{E_\nu}{m_e c^2} \right)^2 A^2 \left[1 - \frac{Z}{A} + \frac{Z}{A} (4 \sin^2 \theta_W - 1) \right]^2$$

$$\sin^2 \theta_W = 0.23 \approx 0.25$$

$$\sigma_\nu \approx \frac{1}{64} \sigma_0 \left(\frac{E_\nu}{m_e c^2} \right)^2 A^2$$

Mean free path

$$\lambda_\nu \approx 1.0 \times 10^8 \left[\frac{N^2}{6A} X_{\text{bound}} + X_{\text{nucleon}} \right]^{-1} \rho_{12}^{-1} E_{\text{MeV}}^{-2} \quad \text{cm}$$

Mean free path

$$\lambda_{\nu} = 2 \times 10^5 \left(\frac{E_{\nu}}{10 \text{ MeV}} \right)^{-2} \rho_{12}^{-1} \quad \text{cm}$$

diffusion time scale (random walk)

$$t_{diff} \approx \frac{\Delta R^2}{3 \lambda_{\nu} c}$$

more exactly for spherical geometry

$$t_{diff} \approx \frac{3 R^2}{\pi^2 \lambda_{\nu} c}$$

$$t_{diff} \approx 3.9 \times 10^{-3} \left(\frac{E_{\nu}}{10 \text{ MeV}} \right)^2 \rho_{12}^{1/3} \quad \text{s}$$

$$t_{diff} \approx 3.9 \times 10^{-3} \left(\frac{E_\nu}{10 \text{ MeV}} \right)^2 \rho_{12}^{1/3} \quad \text{s}$$

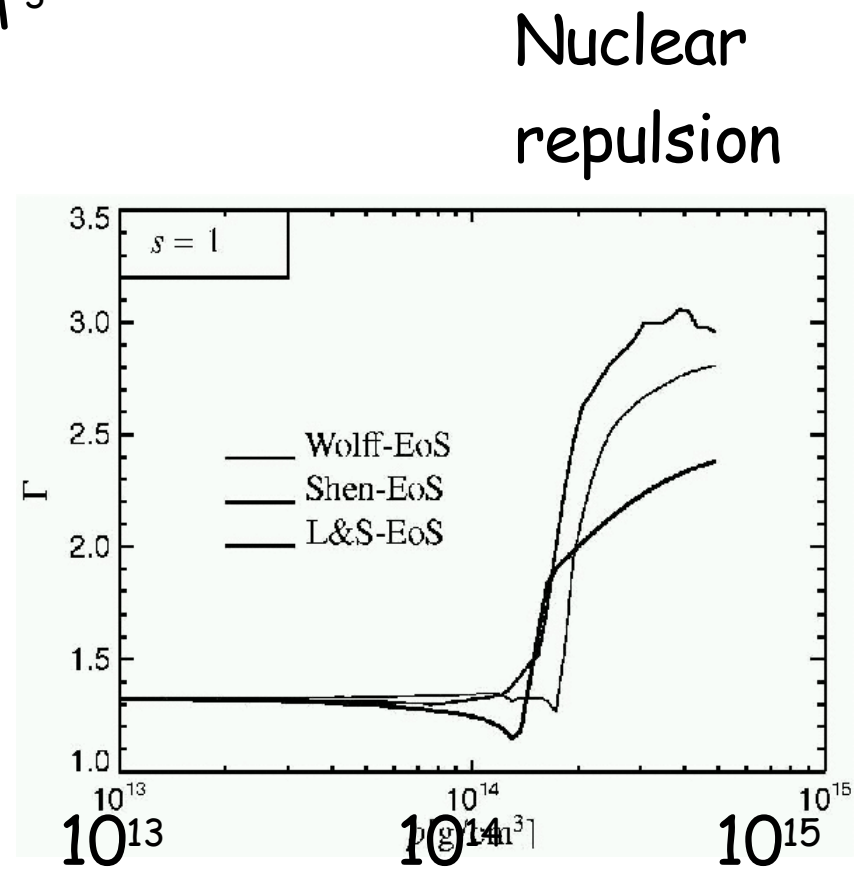
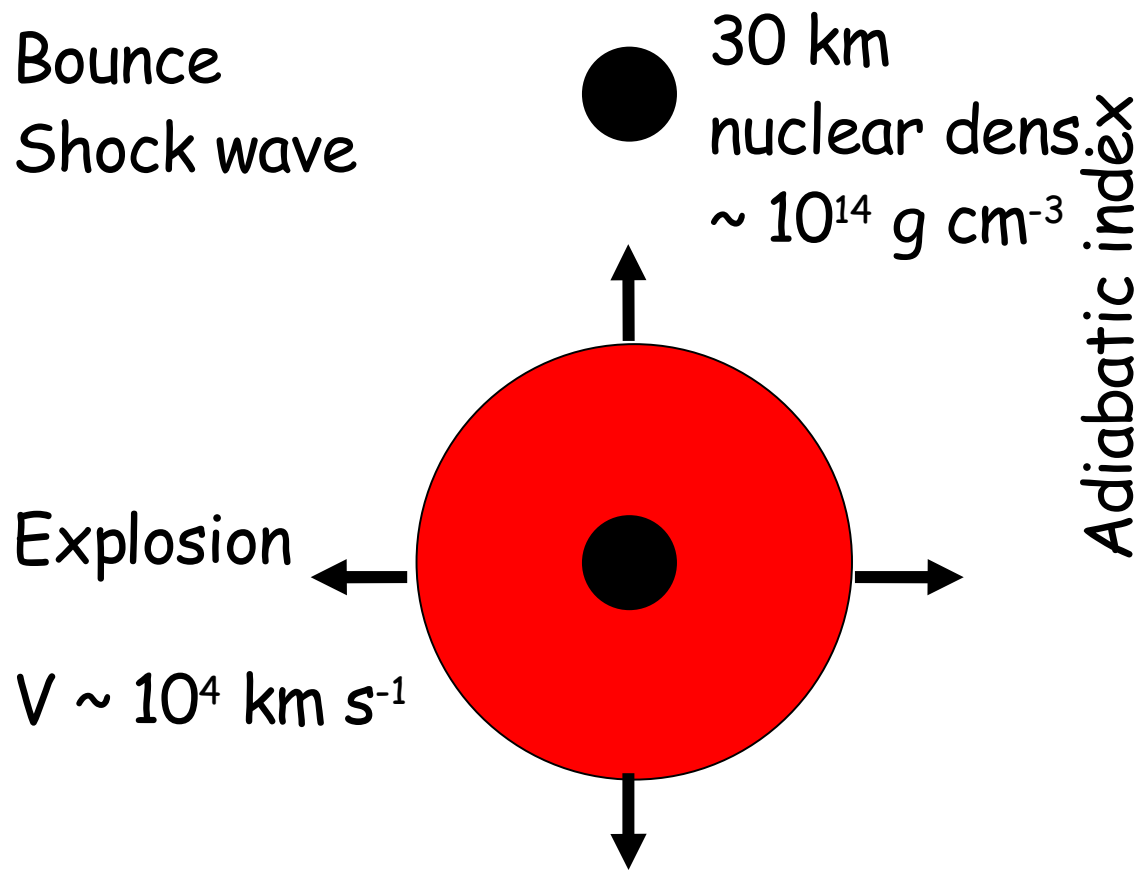
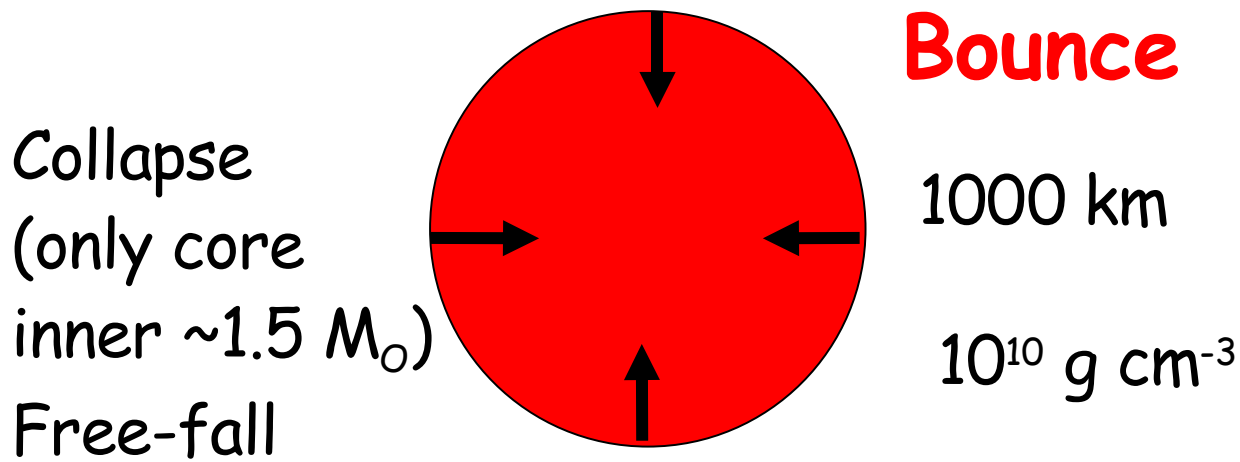
Typical ν energy

$$E_\nu \approx E_F = 36.8 \rho_{12}^{1/3} \text{ MeV} \quad \text{MeV}$$

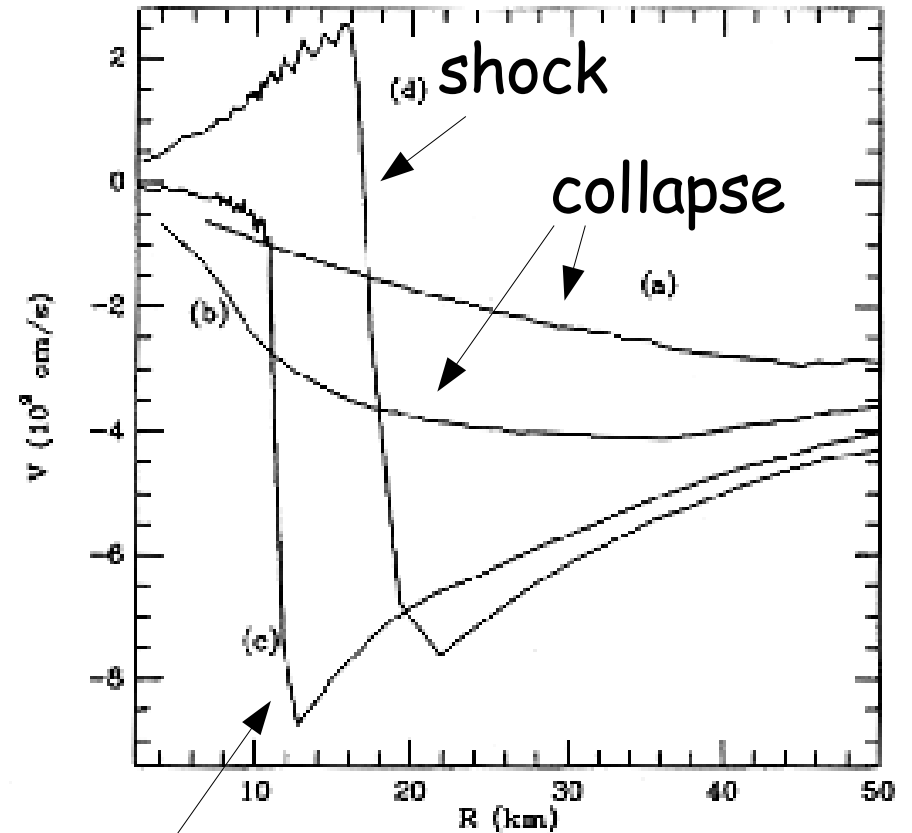
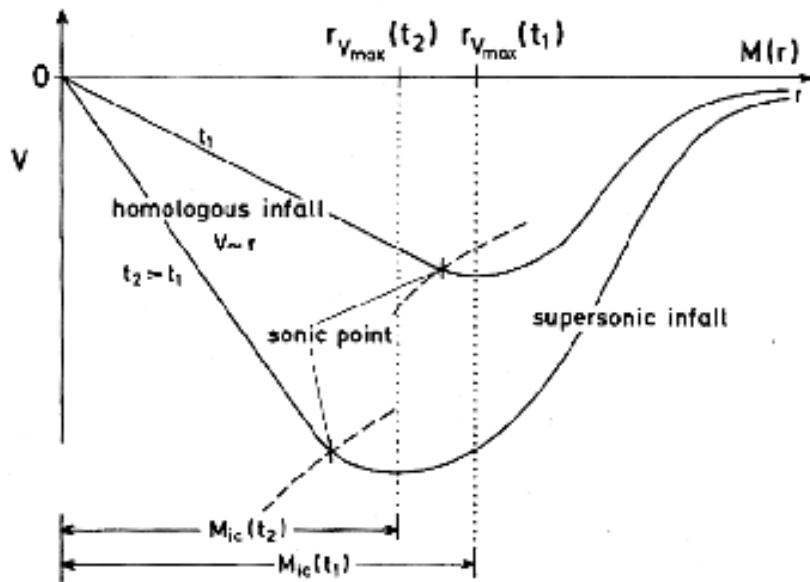
$$t_{diff} \approx 5.2 \times 10^{-2} \rho_{12} \quad \text{s}$$

$$\frac{t_{diff}}{t_{dyn}} \approx 40 \rho_{12}^{3/2}$$

ν :s will be trapped in collapsing core above $\sim 10^{11} \text{ g cm}^{-3}$!
Collapse adiabatic above trapping density $\gamma \sim 4/3$



Collapse



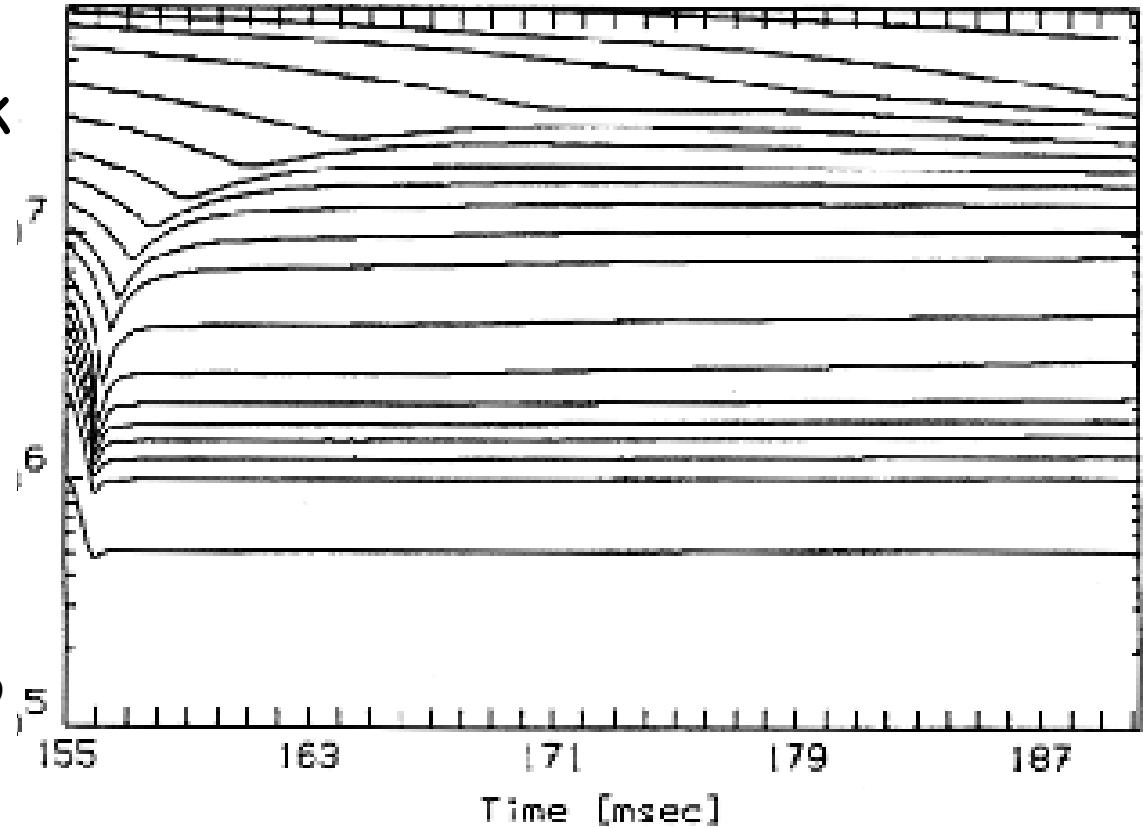
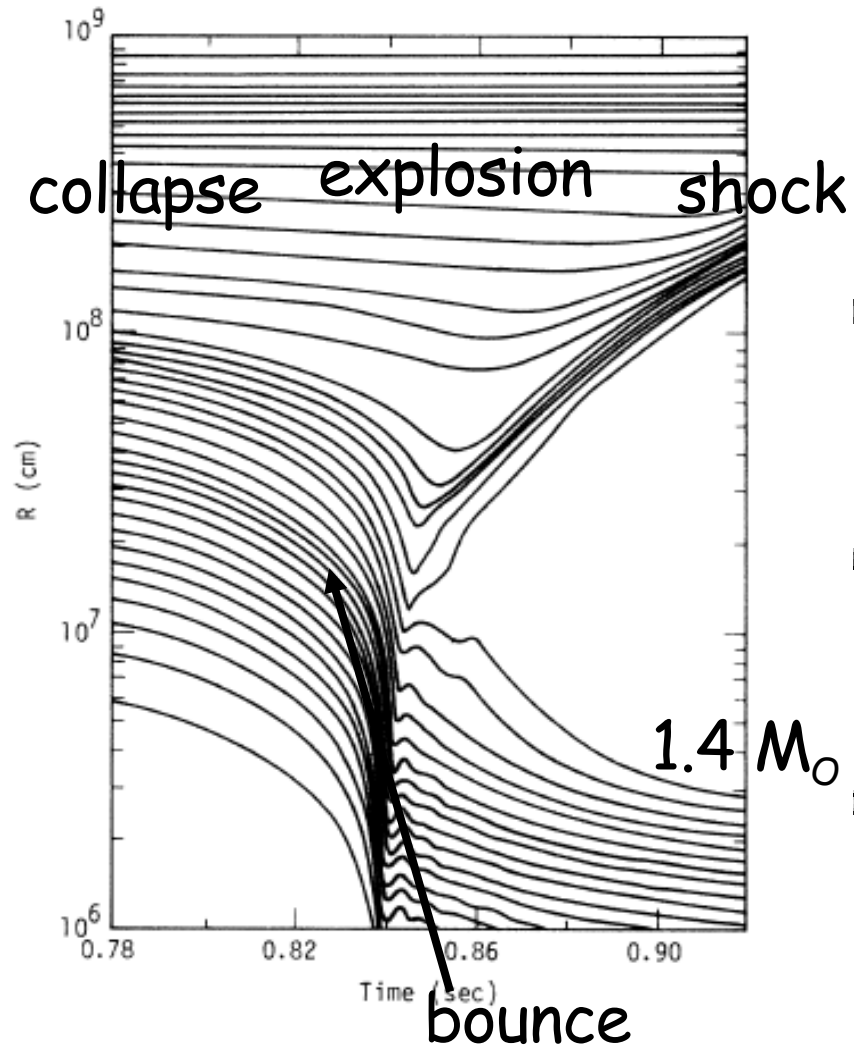
Before bounce:
Homologous inside sonic radius

bounce

Wilson 1974

Explosion?

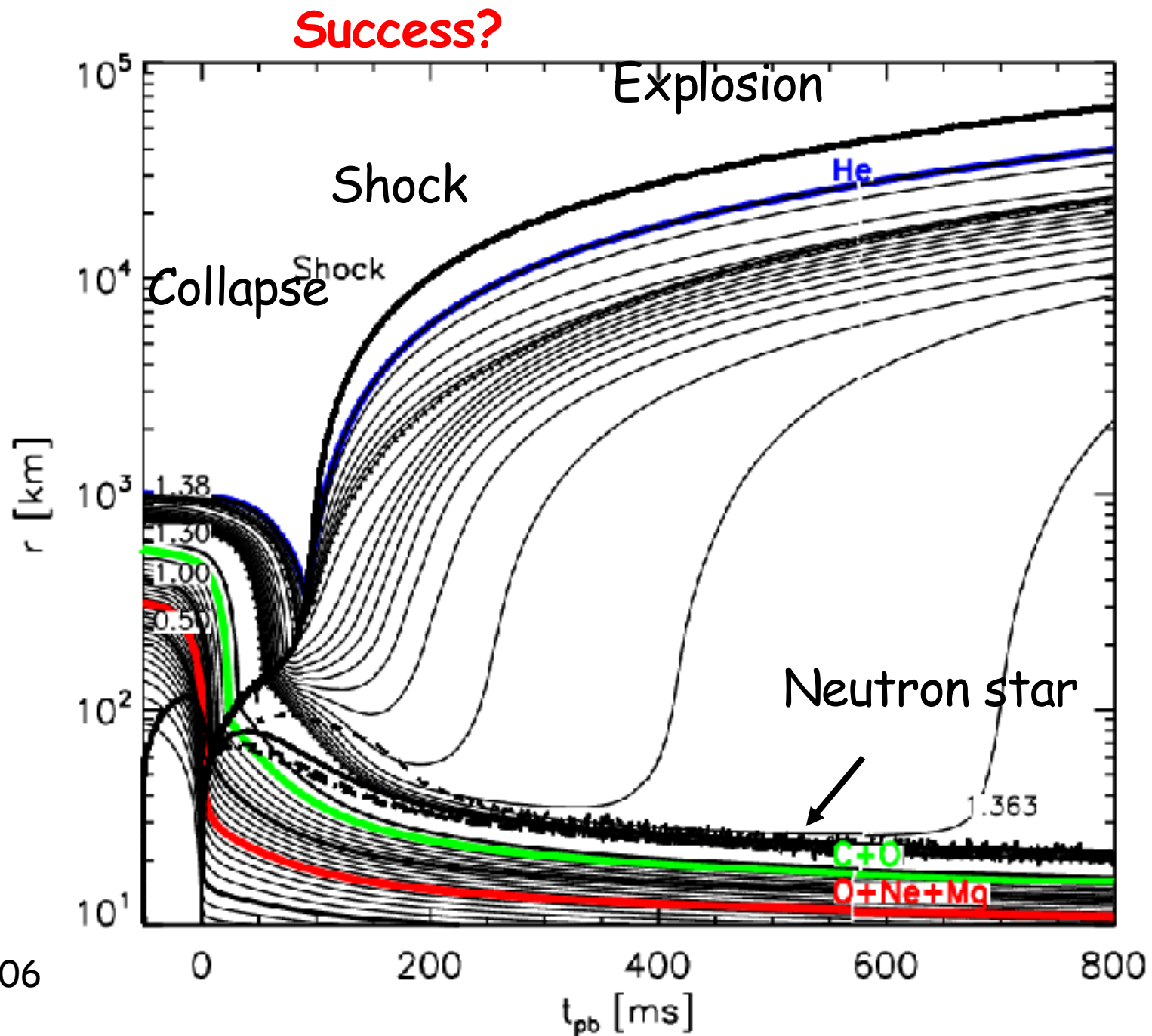
Hillebrandt 1981



All lacking some essential physics! (neutrino transport, EOS, 2/3D....)

Progenitor

$11 M_{\odot}$

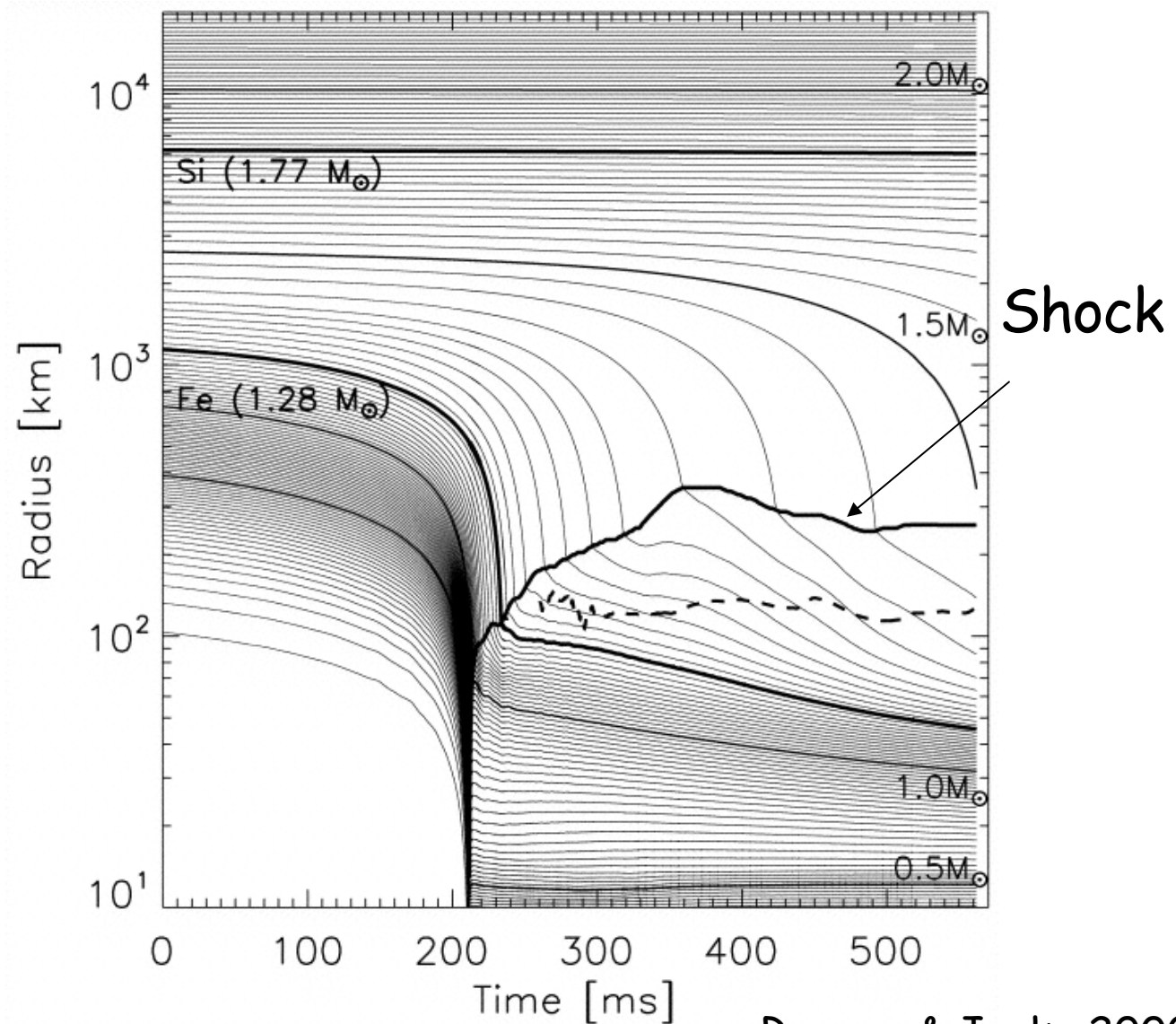


Kitaura et al 2006

Black holes in most cases!

Photodissociation of Fe
 $^{56}\text{Fe} + \gamma \rightarrow 13\alpha + 4n$
 ν -losses

Except for low mass
stars ($< 12 M_{\odot}$) shock
stalls and collapse continues



Rampp & Janka 2000

Total energy = binding energy of neutron star

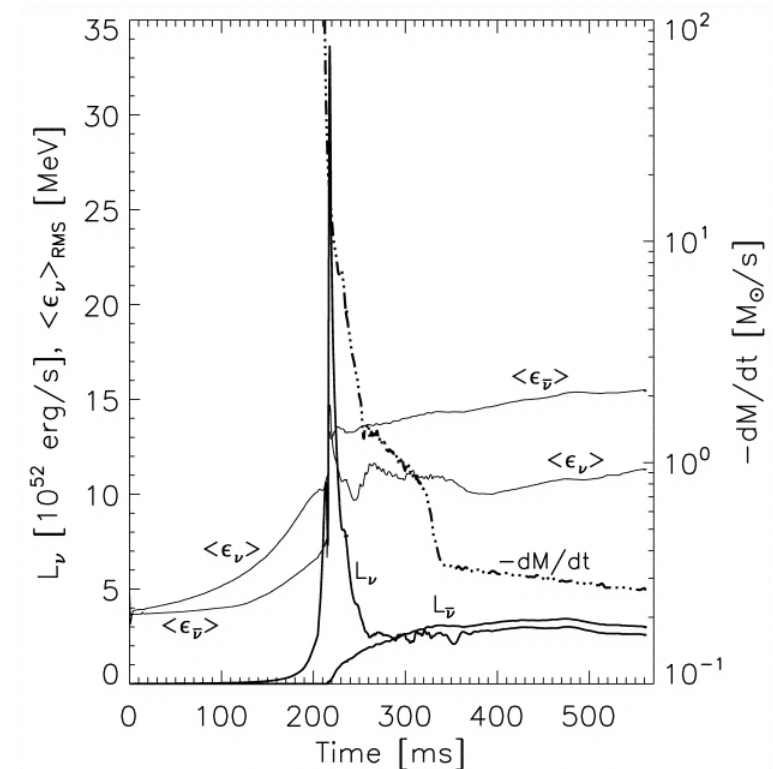
$$E \approx \frac{GM_{core}^2}{R_n} \approx 3 \times 10^{53} \quad \text{ergs}$$

Release time scale $\approx$ ν diffusion time scale

$$\tau_{diff} \approx 5 \left(\frac{\rho}{\rho_{nuclear}} \right) \quad \text{s}$$

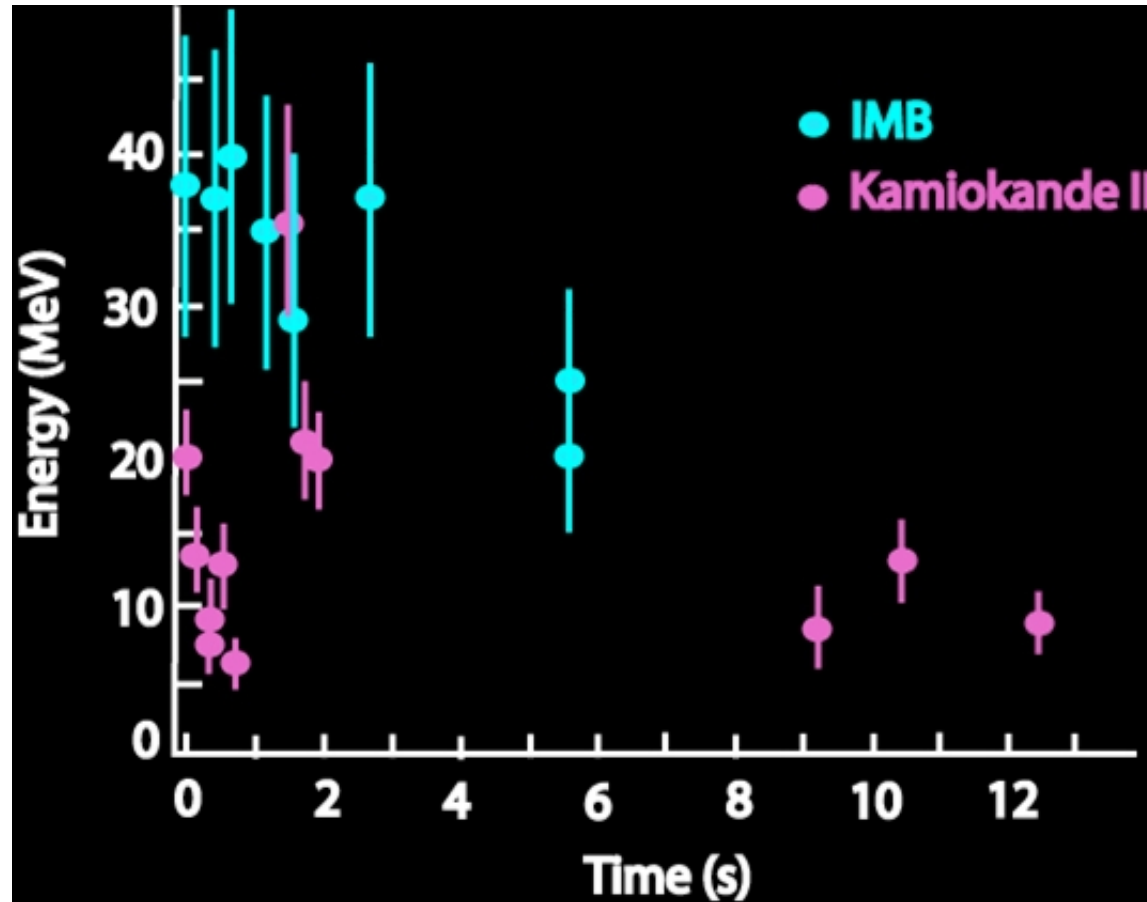
Mean energy 10-15 MeV

Trapping equilibrium creation of
all neutrino species



Neutrinos

$$\bar{\nu}_e + p \rightarrow e^+ + n$$



Also ~5 vs from
Baksan

$E(\bar{\nu}_e) \sim 6 \times 10^{52}$ ergs. Equal amounts of all 6 ν :s $\Rightarrow$
 $E_{\text{tot}} \sim (3-4) \times 10^{53}$ ergs $\tau \sim 5$ s Mean energy ~ 15 MeV

A history of failures....

1965 Colgate & White neutrino heating

1970-1980 Arnett, Bethe, Brown, Wilson

EOS, neutrino transport prompt explosion. No!

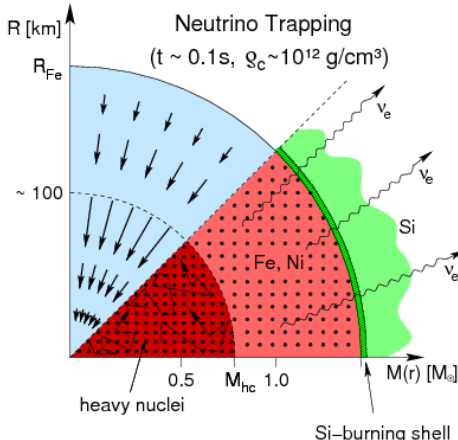
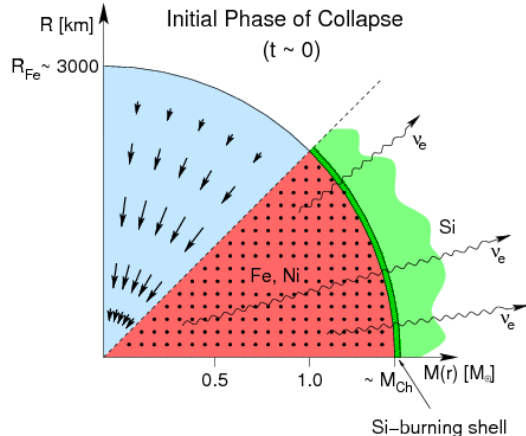
198? J. Wilson Late neutrino heating

Woosley, Nomoto: progenitor models: Fe core mass.....

1990 Janka, Burrows... neutrino convection 2D, 3D

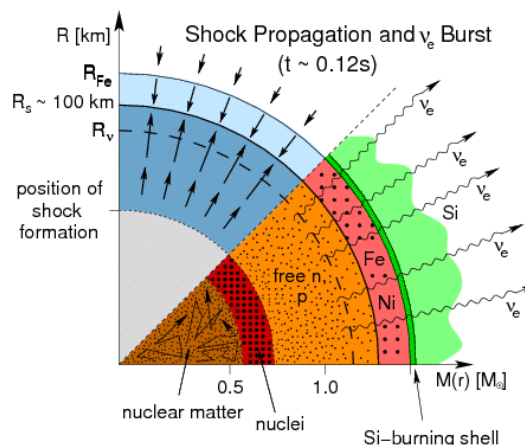
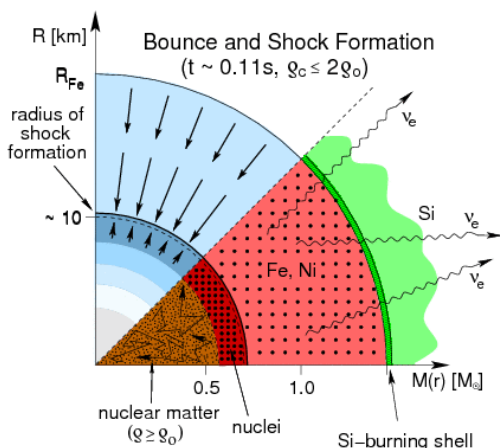
2000 - Large scale instabilities, rotation, 2D, 3D.....

collapse

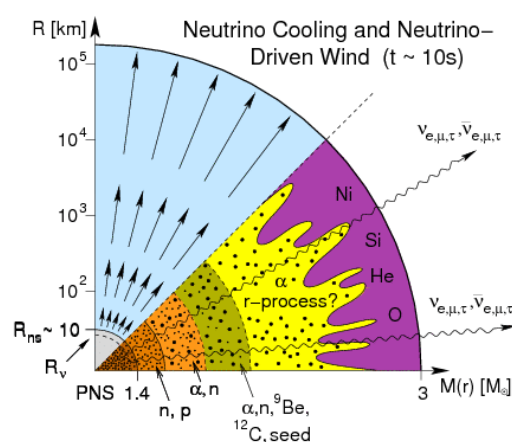
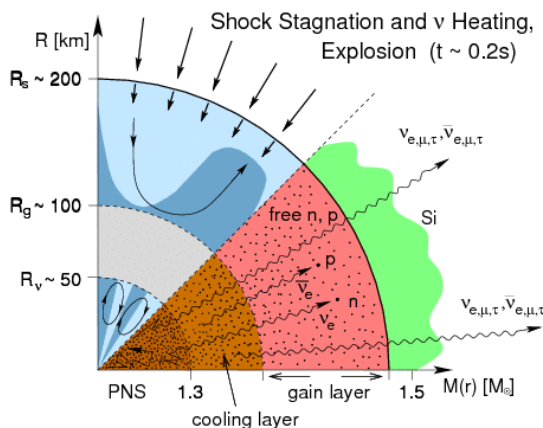


ν -trapping

bounce
shock



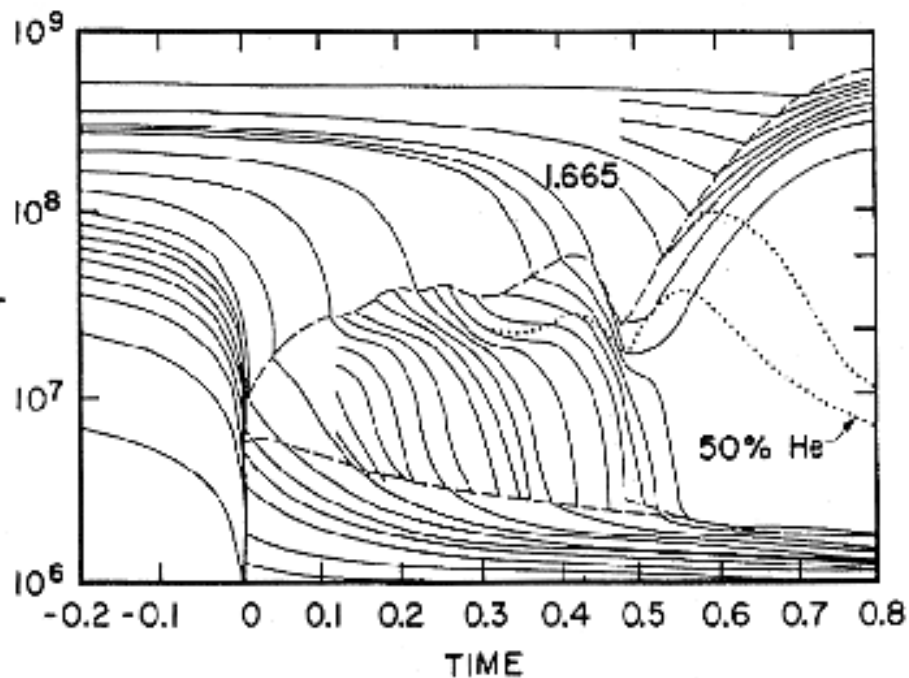
ν -heating



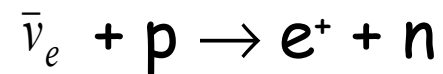
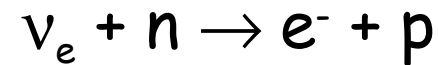
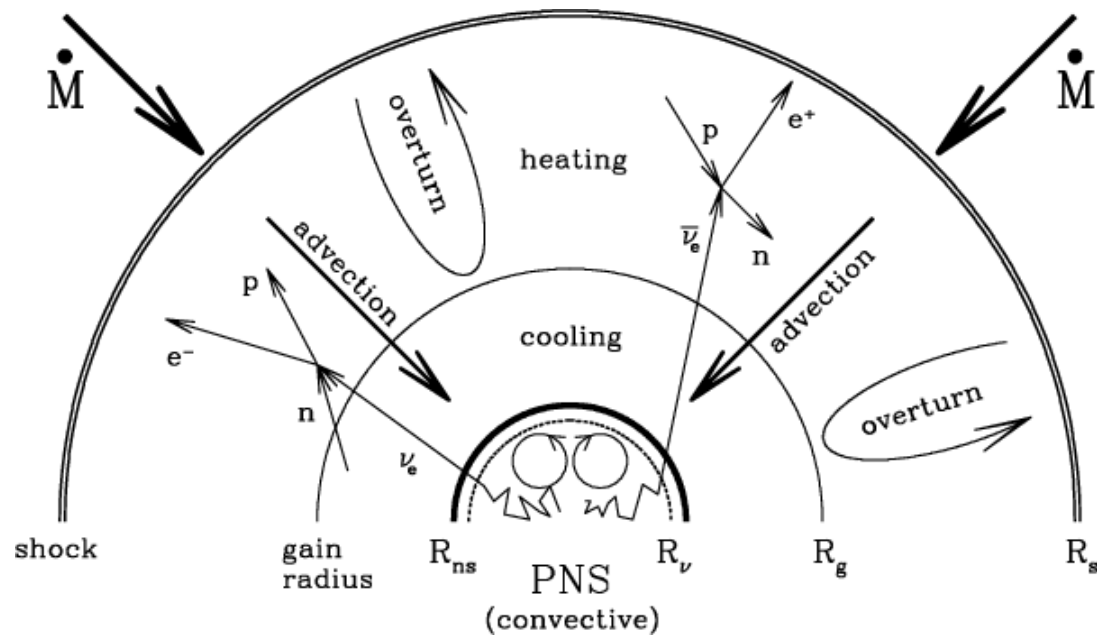
Explosion,
 ν driven wind

Janka et al 2006

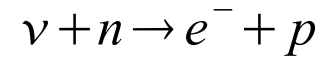
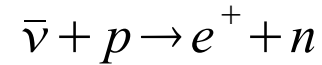
Delayed neutrino heating?



J. Wilson + H. Bethe 1985



Neutrino heating



Heating rate

$$H_{\nu}(r) = \frac{4\pi}{(ch)^3} \int c \sigma(E_{\nu}) E_{\nu} W(r) f(E_{\nu}) E_{\nu}^2 dE_{\nu}$$

$$f(E_{\nu}) = \frac{1}{e^{E_{\nu}/kT_{\nu}} + 1}$$

Dilution factor

$$W(r) = \frac{1}{2} [1 - \sqrt{1 - (R_{\nu}/r)^2}]$$



radius of 'neutrinosphere'

For cooling we need

$$\sigma_{e^- + p \rightarrow \nu + n}$$

Detailed balance

$$\sigma_{i \rightarrow f} g_i p_i^2 = \sigma_{f \rightarrow i} g_f p_f^2$$

$$g_\nu = 1 \quad g_e = 2 \quad p_\nu = E_\nu / c \quad p_e \approx E_e / c$$

$$E_\nu^2 \sigma_{\nu + n \rightarrow e^- + p} = 2 E_e^2 \sigma_{e^- + p \rightarrow \nu + n}$$

Earlier

$$\sigma_{\nu + n \rightarrow e^- + p} = \frac{1}{4} \sigma_0 \left(\frac{E_\nu}{m_e c^2} \right)^2$$

$\Rightarrow$

$$\sigma_{e^- + p \rightarrow \nu + n} = \frac{1}{8} \sigma_0 \left(\frac{E_e}{m_e c^2} \right)^2$$

$\dot{}$
 $\dot{}$
 $\dot{}$

Cooling rate

$$C_{\nu}(r)=\frac{\pi \sigma_0 c}{2(c h)^3} \int E^5 f(E) dE$$

$$C_{\nu}(r)=\frac{31 \pi^7}{252} \frac{m_e^4 c^6}{h^3} \sigma_0 \left(\frac{k T}{m_e c^2} \right)^6$$

$\dot{}$

$$H_{\nu}(r)=\frac{31 \pi^7}{252} \frac{m_e^4 c^6}{h^3} \sigma_0 \left[W(r) T_{\nu}^6 - \frac{1}{2} T^6 \right]$$

Net neutrino heating rate

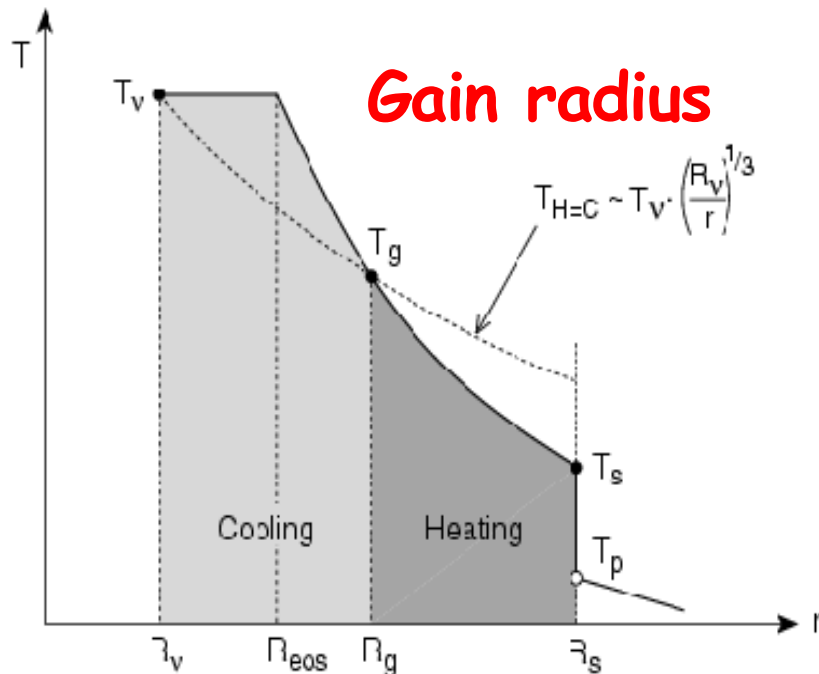
$$H_{\nu}(r) = \frac{31 \pi^7}{252} \frac{m^4 c^6}{h^3} \sigma_0 [W(r) T_{\nu}^6 - \frac{1}{2} T^6]$$

Temperature of nucleons set by energy loss due to photodiss.

$$\frac{G M m_p}{r} = E_{bind} + \frac{3}{2} k T$$

Fe to α -particles ~ 2 MeV/nucleon

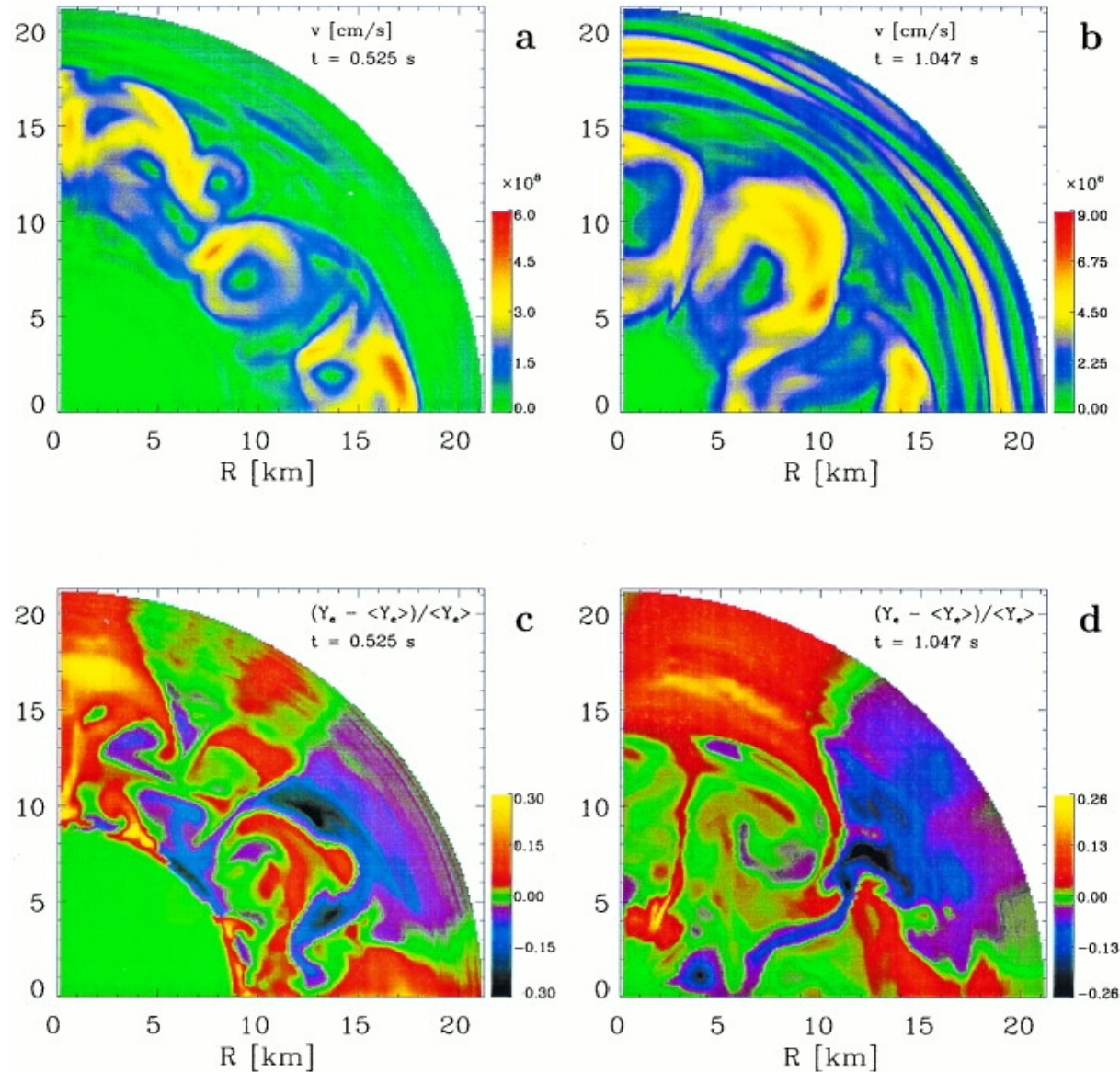
$$T \approx \frac{15}{r_7} - 1.3 \text{ MeV}$$

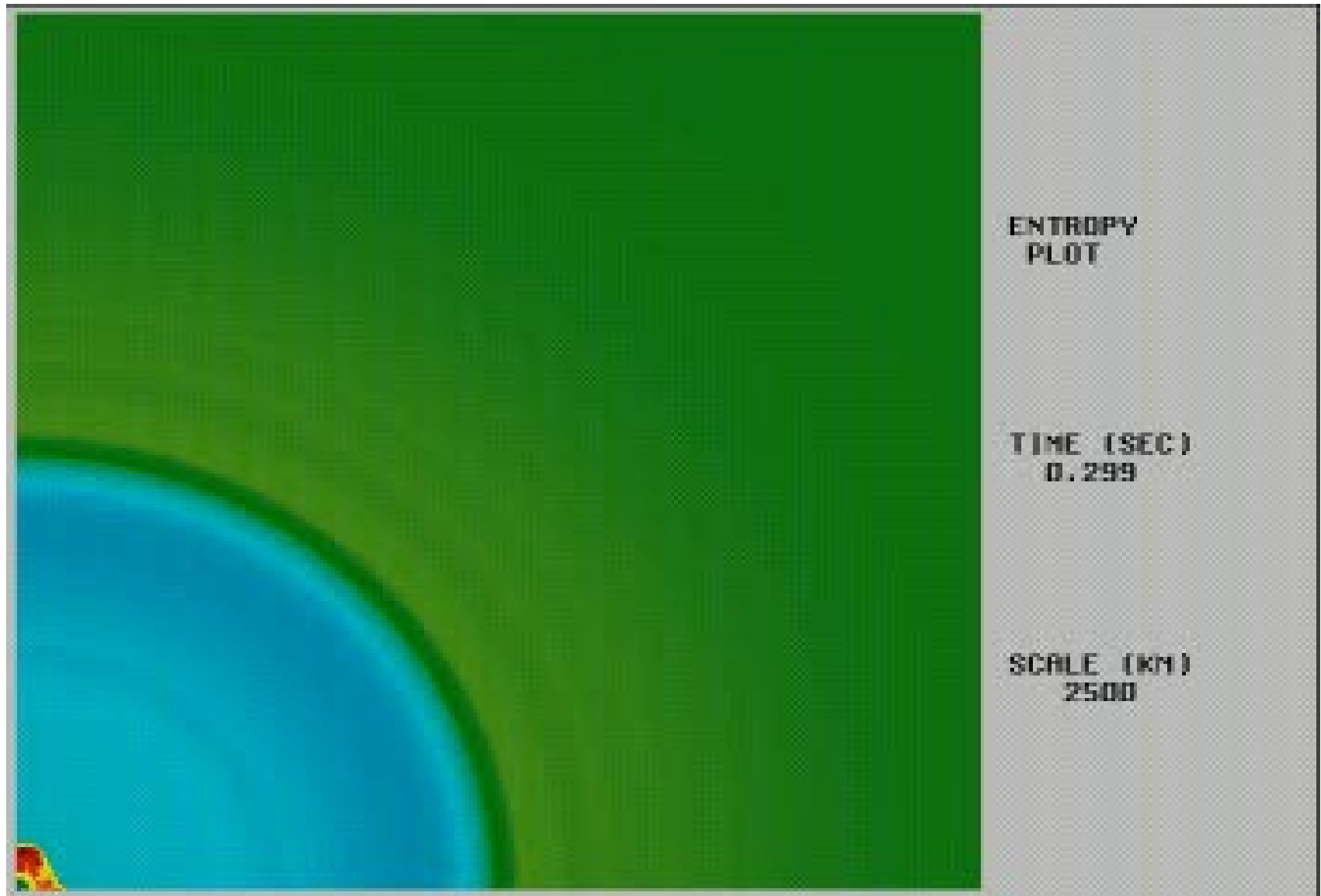


$$W \approx \frac{1}{2} \left(\frac{R_v}{r} \right)^2$$

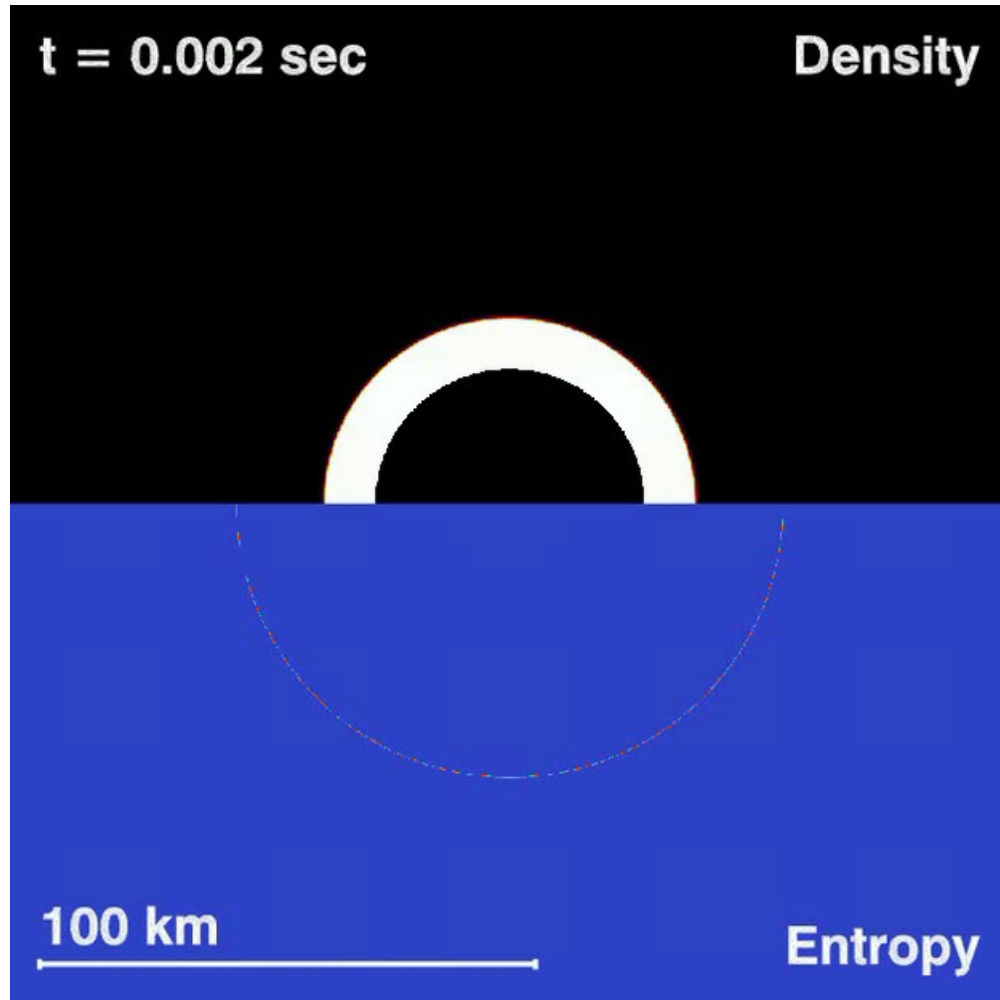
$$T_{H=C} \approx T_v \left(\frac{R_v}{r} \right)^{1/3}$$

Convection in proto neutron star increases neutrino flux





A. Burrows



Latest ingredient: Large scale shock instabilities

Accretion shock
unstable to large
scale modes

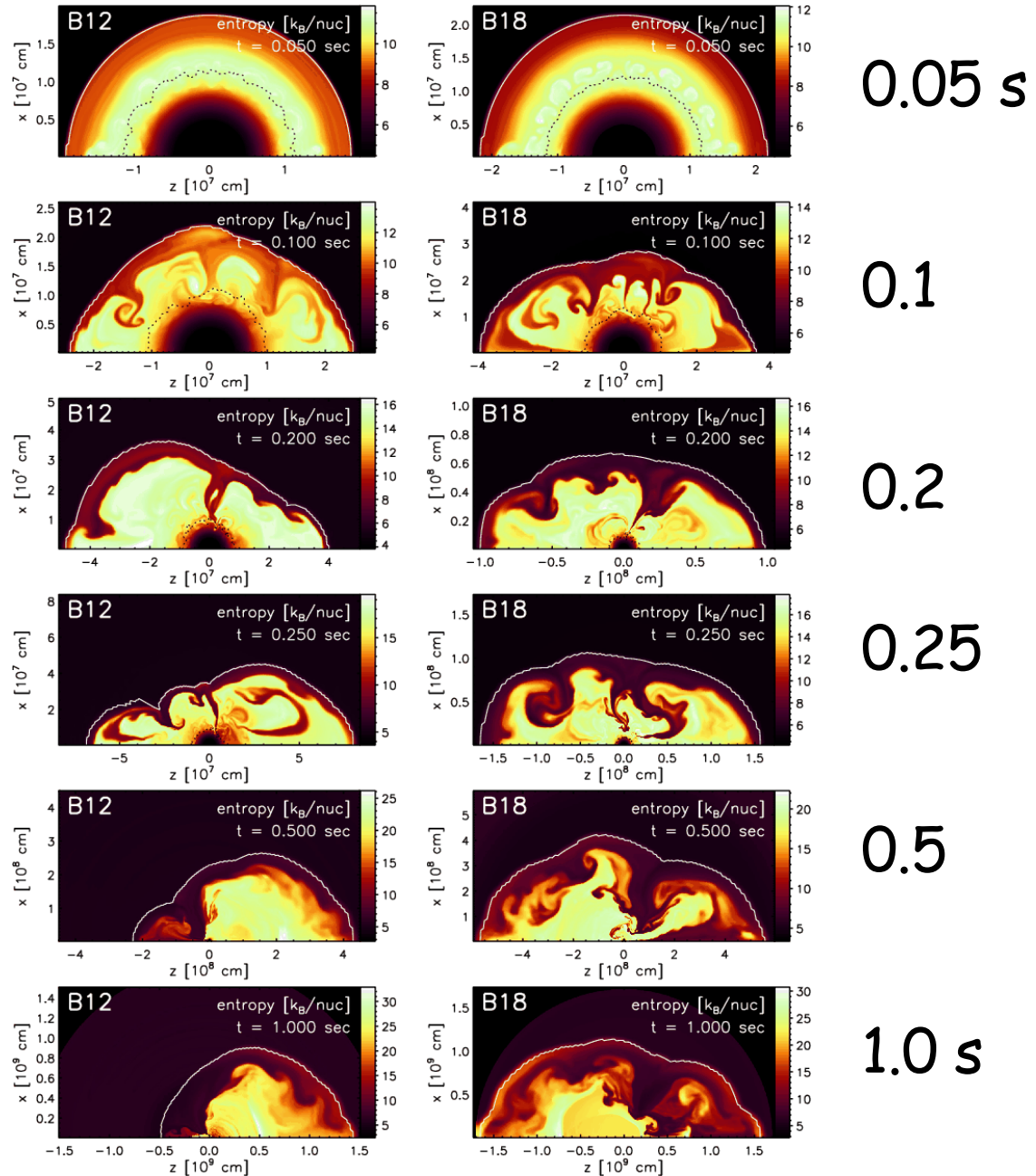
$l=1,2$

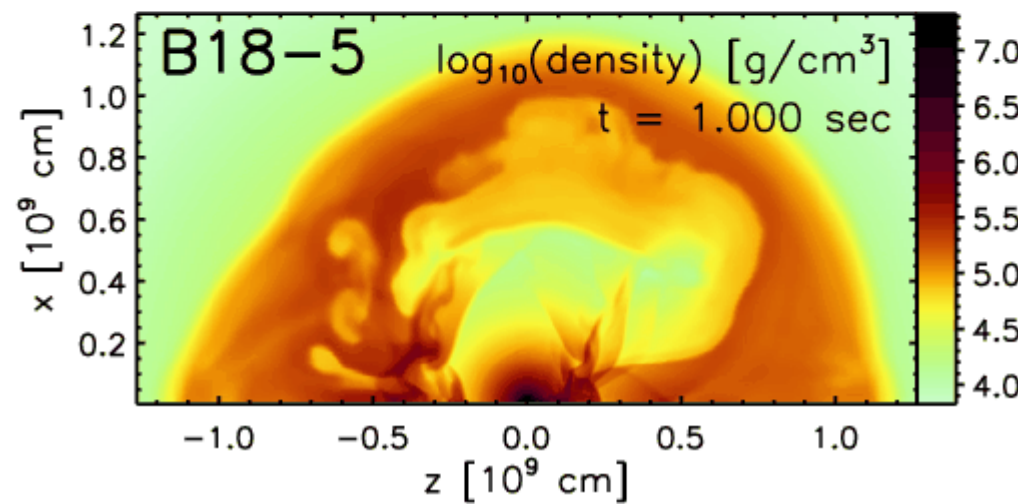
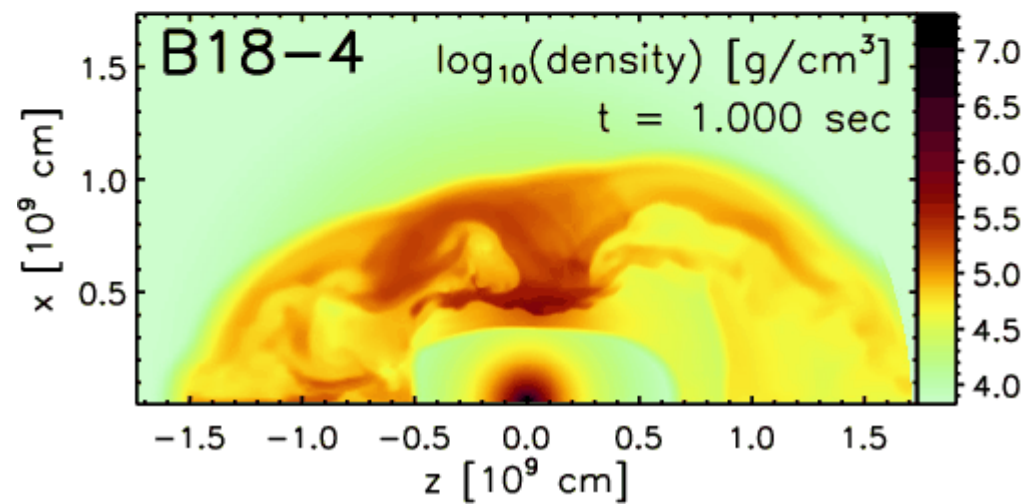
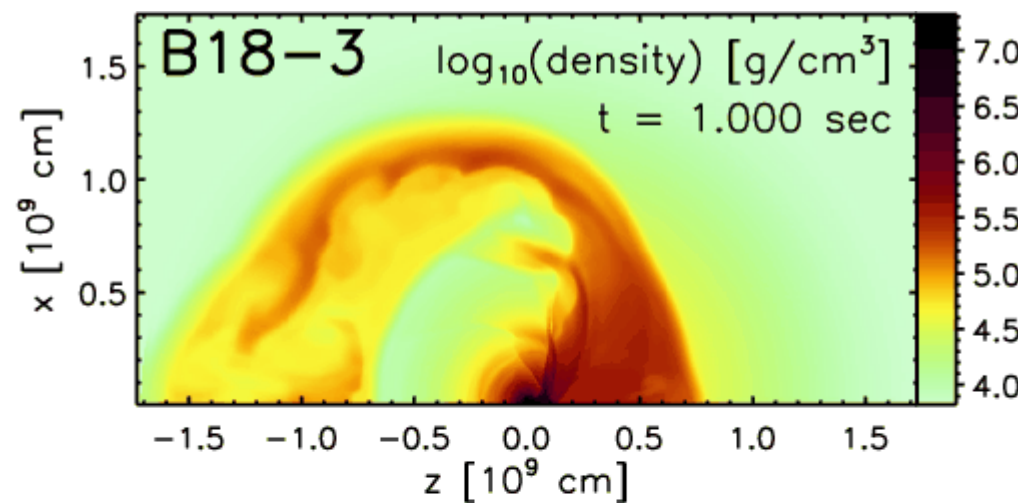
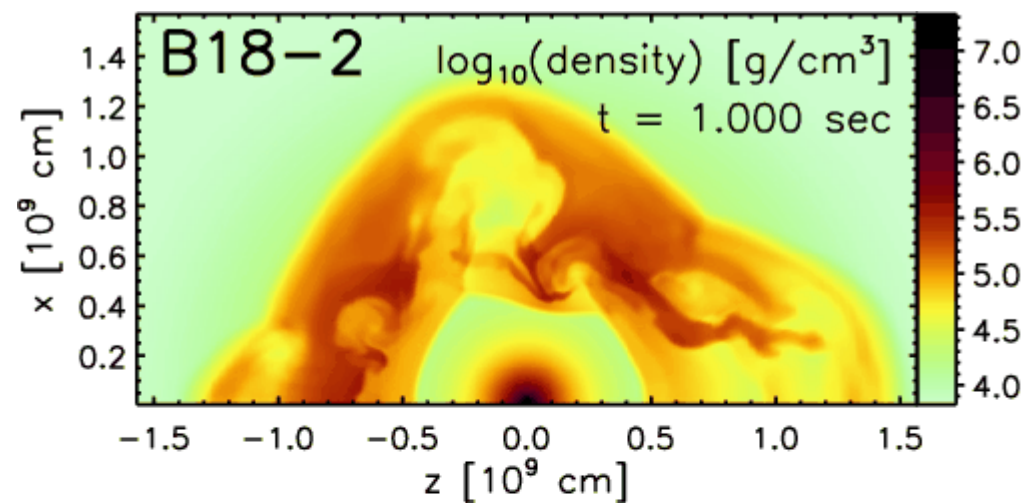
SASI mechanism

Standing Accretion
Shock Instability

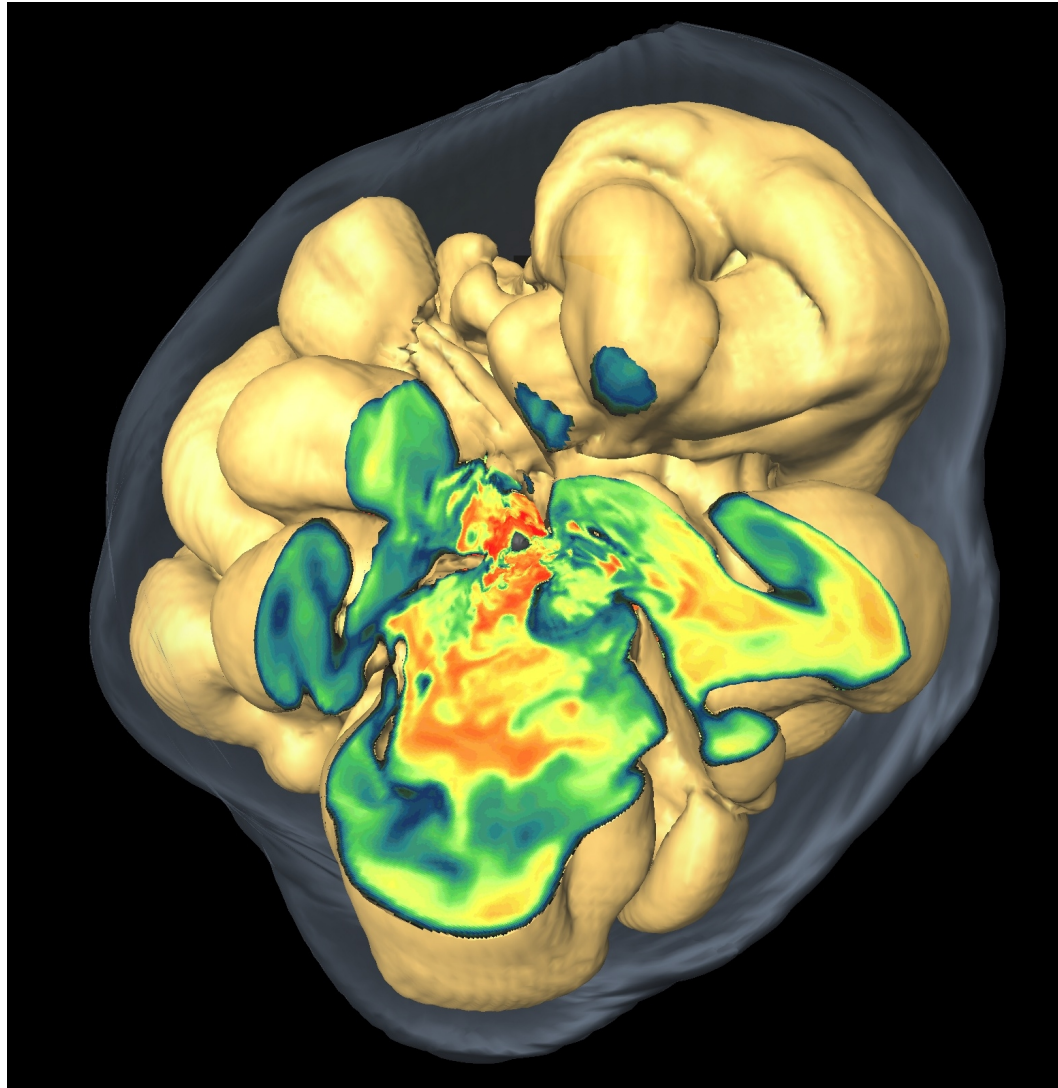
Proto-neutron star
oscillations excited
by accretion?

Scheck et al



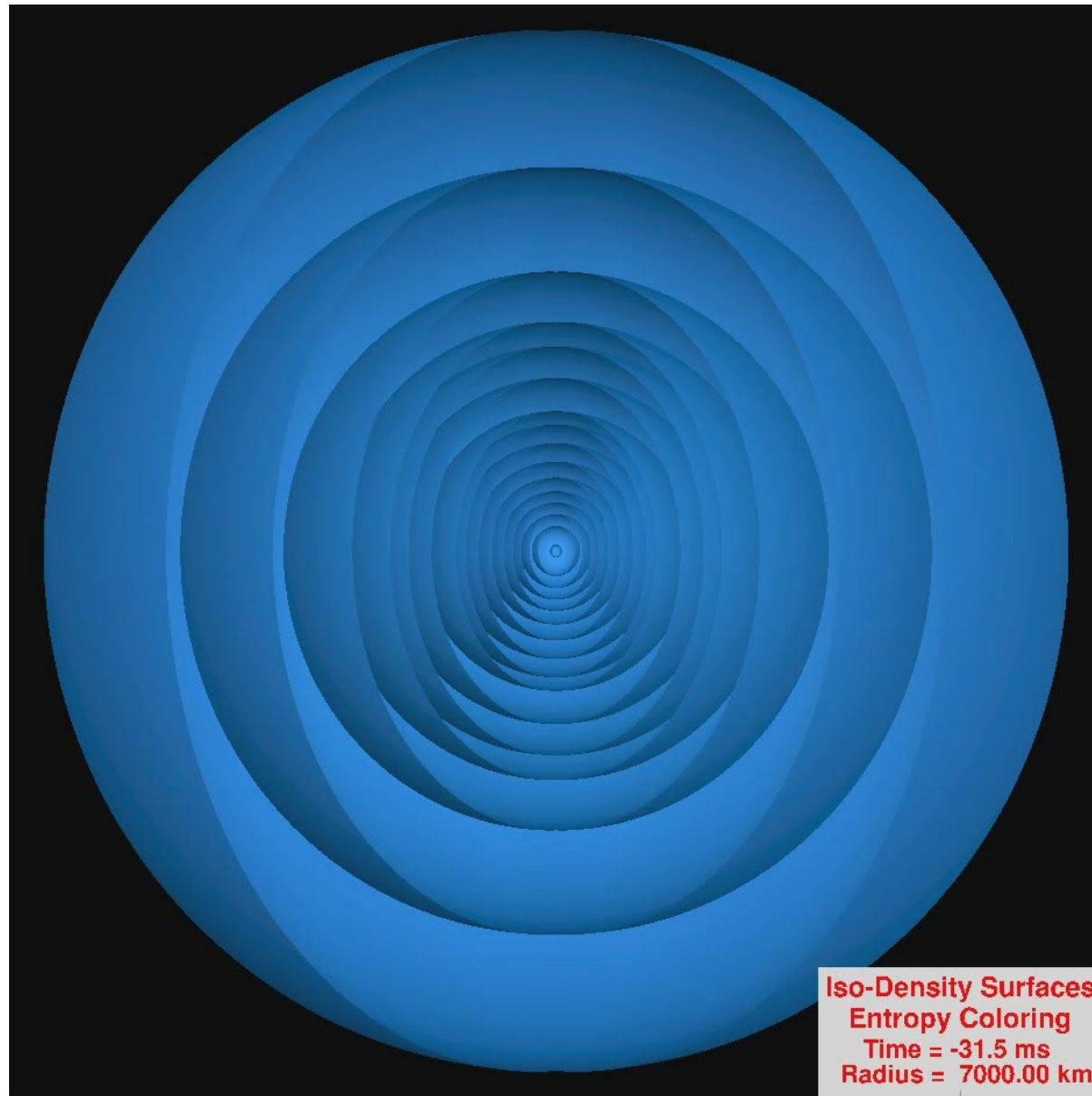


3 D simulation



Scheck et al 2006

Oscillations in proto-neutron star

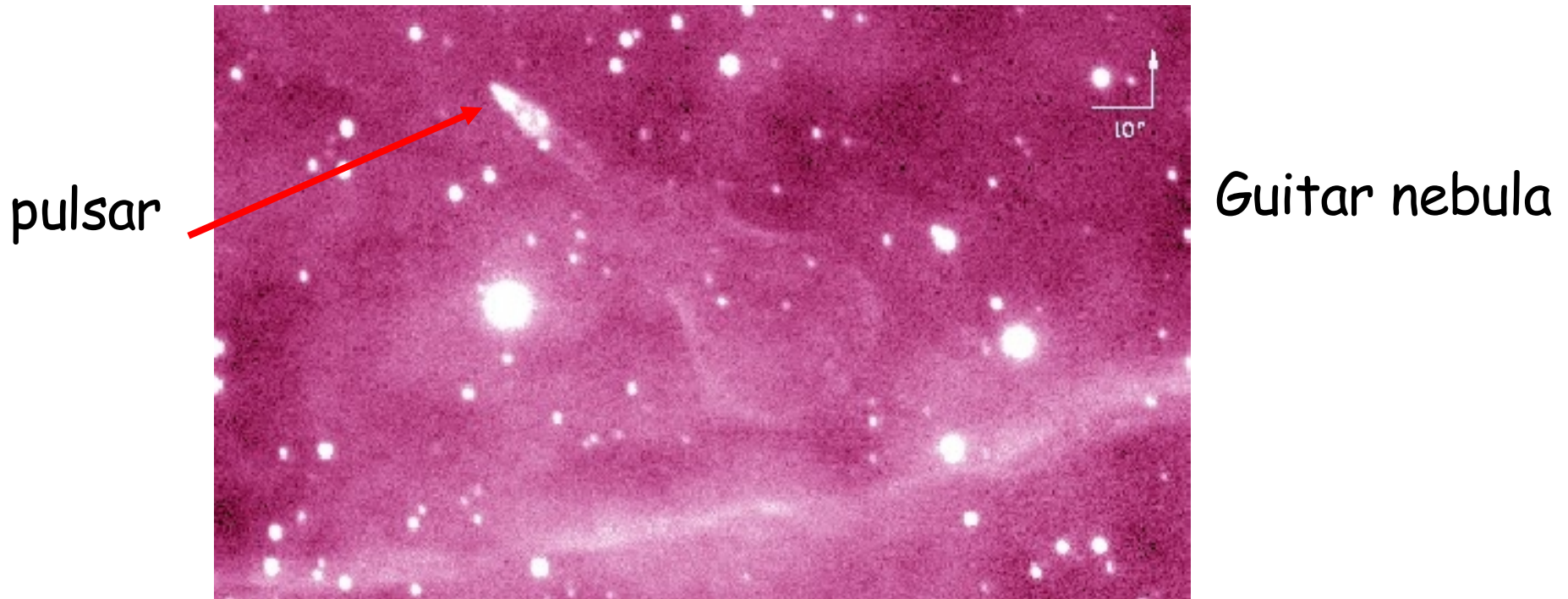


Burrows et al

Pulsar kicks

Pulsars = isolated neutron stars: Space velocities up to 1000 km/s.

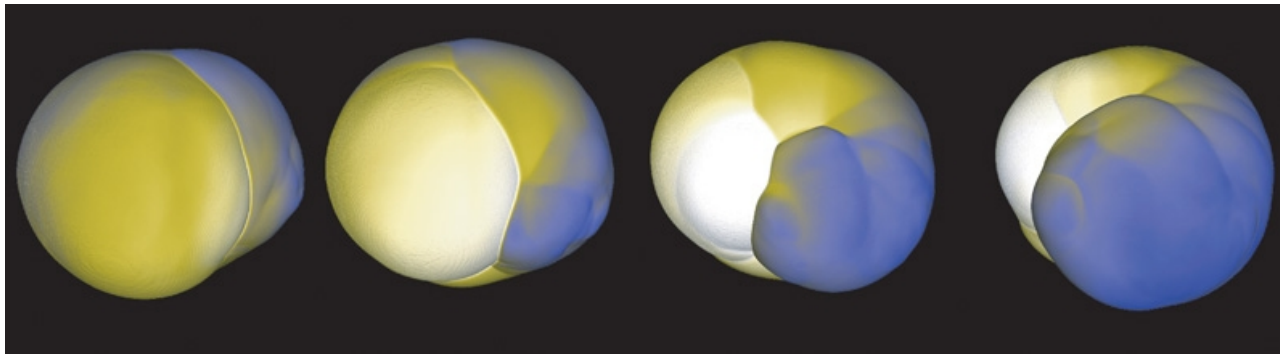
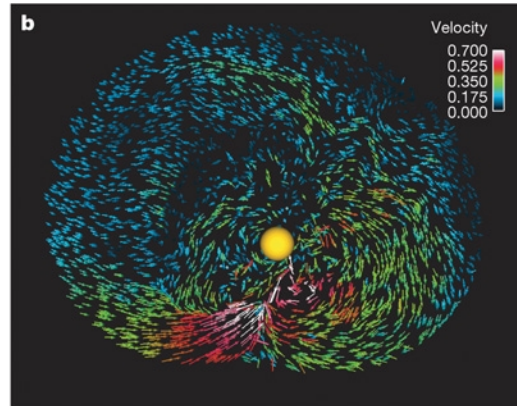
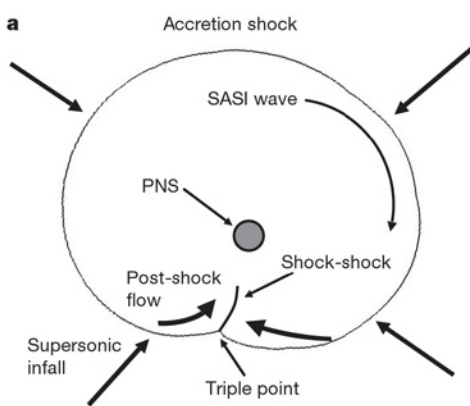
Large scale anisotropy $\Rightarrow$ 'kicks' $\Rightarrow$ high space velocities



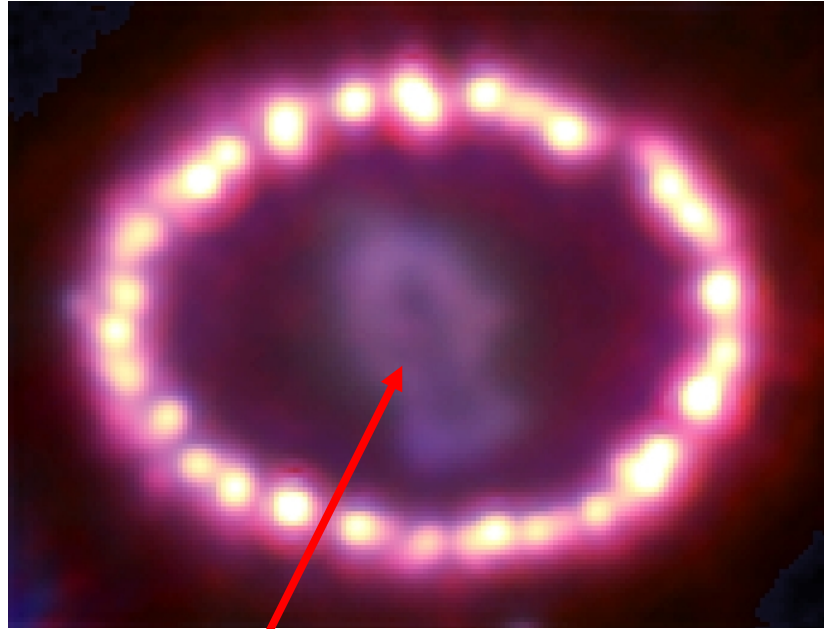
Pulsar spins

Pulsars: Rotation periods 20 ms to ~ 10 s

'Spiral' wave $m = 1 \Rightarrow$ pulsar spins



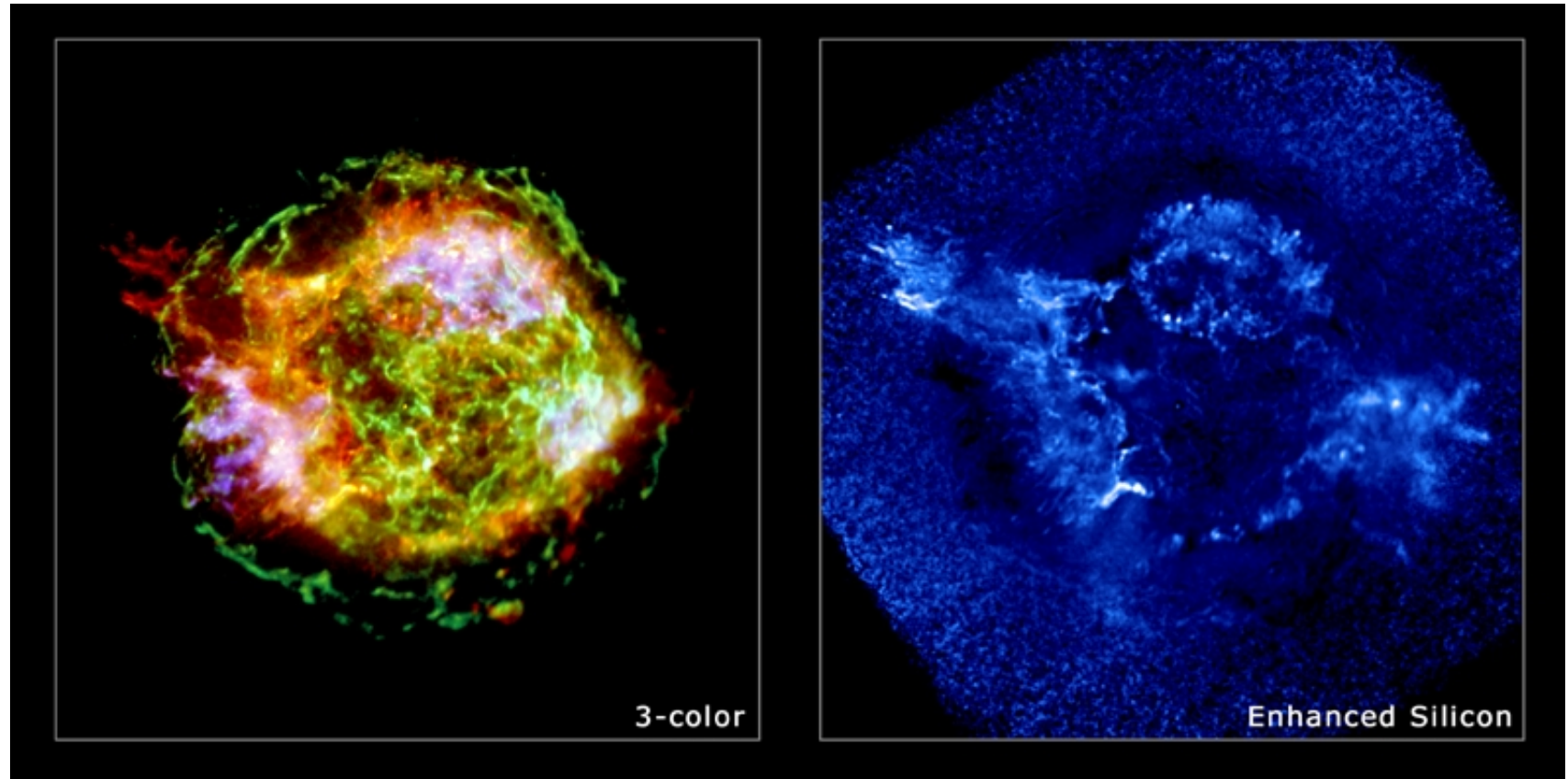
Asymmetries, element mixing common



SN ejecta

SN 1987A

Asymmetries, element mixing common



3-color

Enhanced Silicon

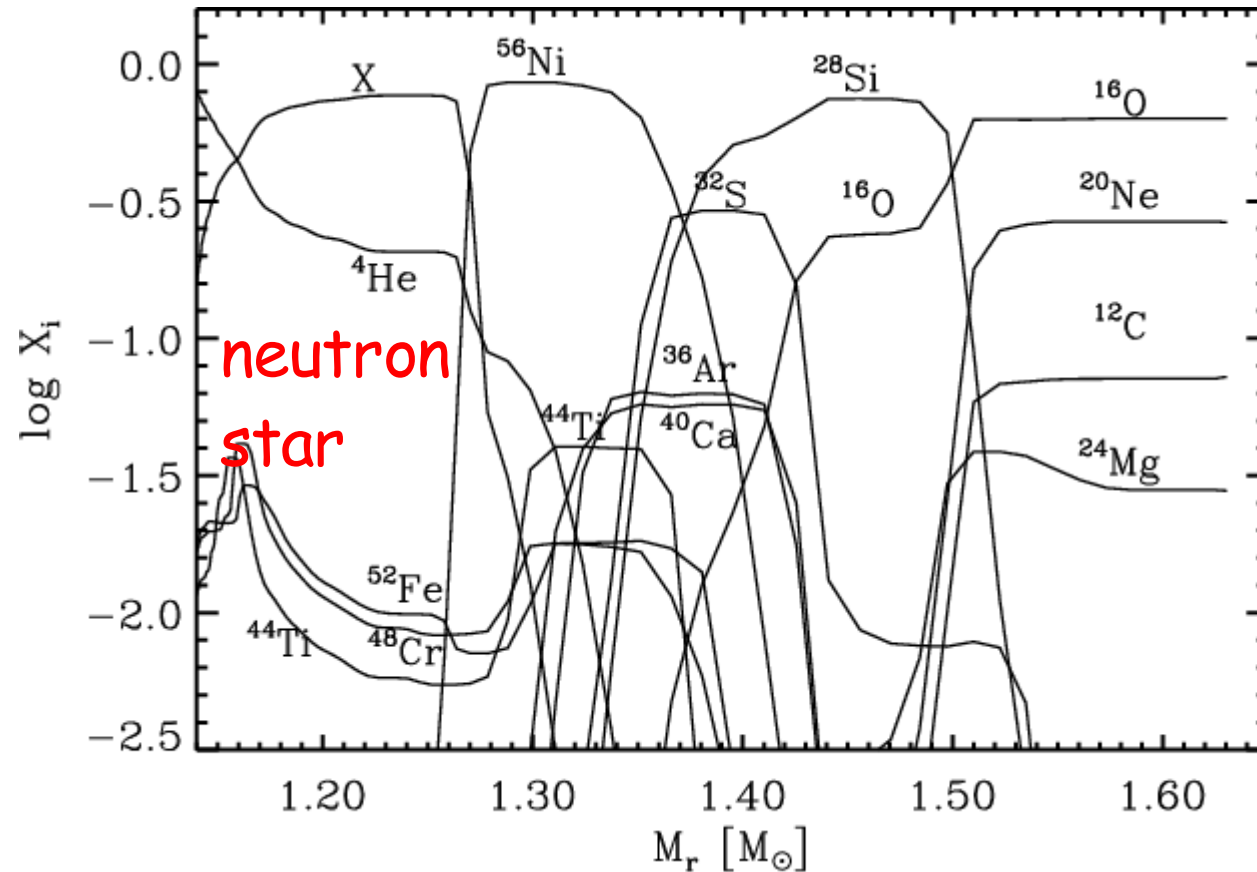
Red = Si

Chandra

Blue = Fe

Cas A (~ 340 years)

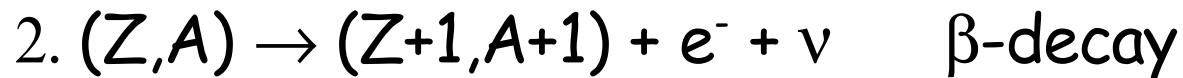
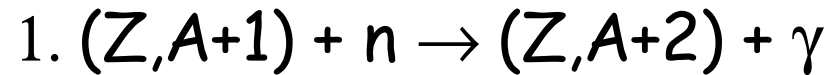
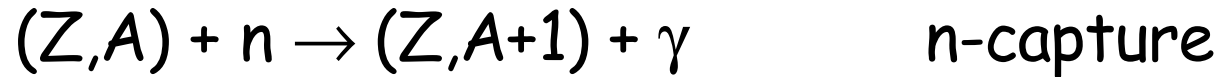
Explosive nucleosynthesis by shock wave



Kifonidis et al

r-process in neutrino driven wind during first seconds

n-capture

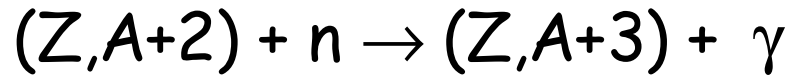
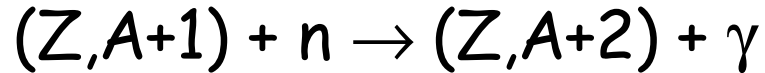
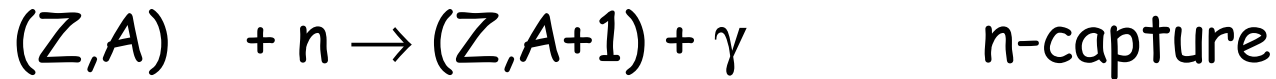


Time scale for β -decay seconds to days (short compared to evolutionary time scale)

s-process: β -decay before new n-capture

r-process: new n-capture before β -decay

r-process



.....

neutron capture cross section decreases with N

photodisintegration increases with N

n-capture continues until **equilibrium** between

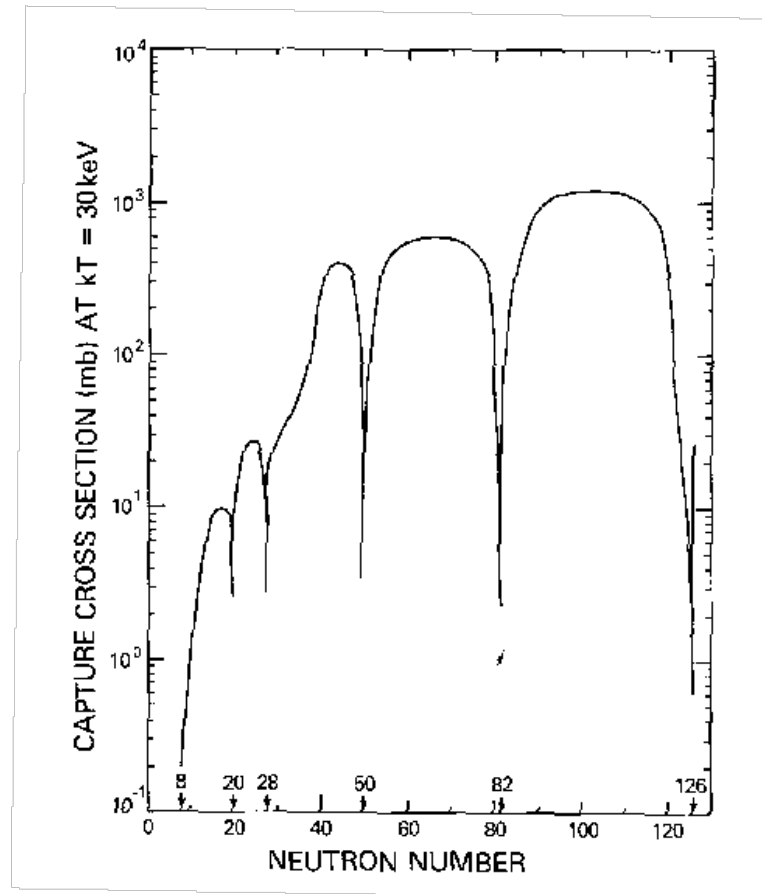
n-capture = photodis.

from this **β -decay** $\Rightarrow (Z+1,A)$

r-process

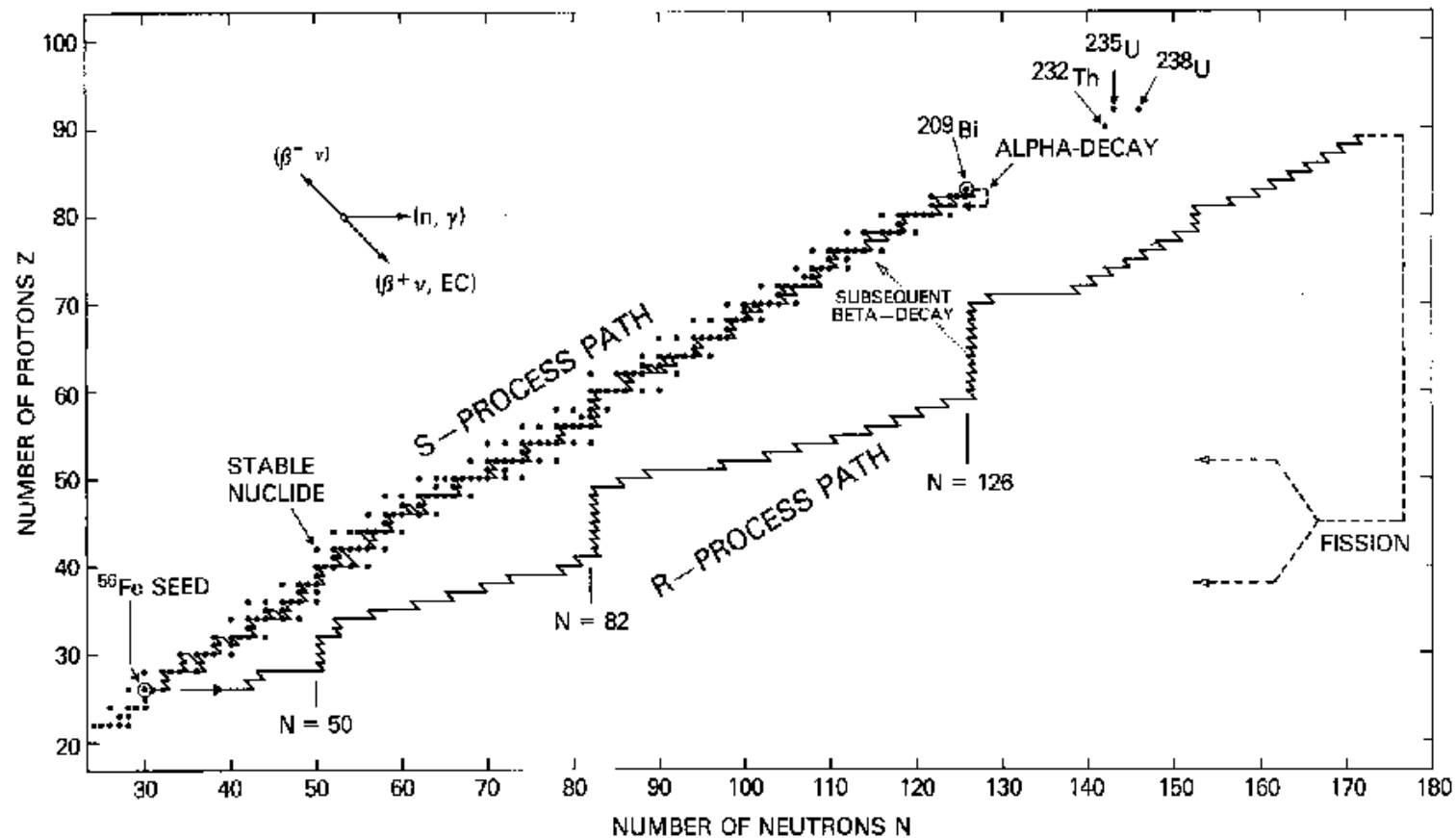
Photodisintegration cross section large above magic n-numbers

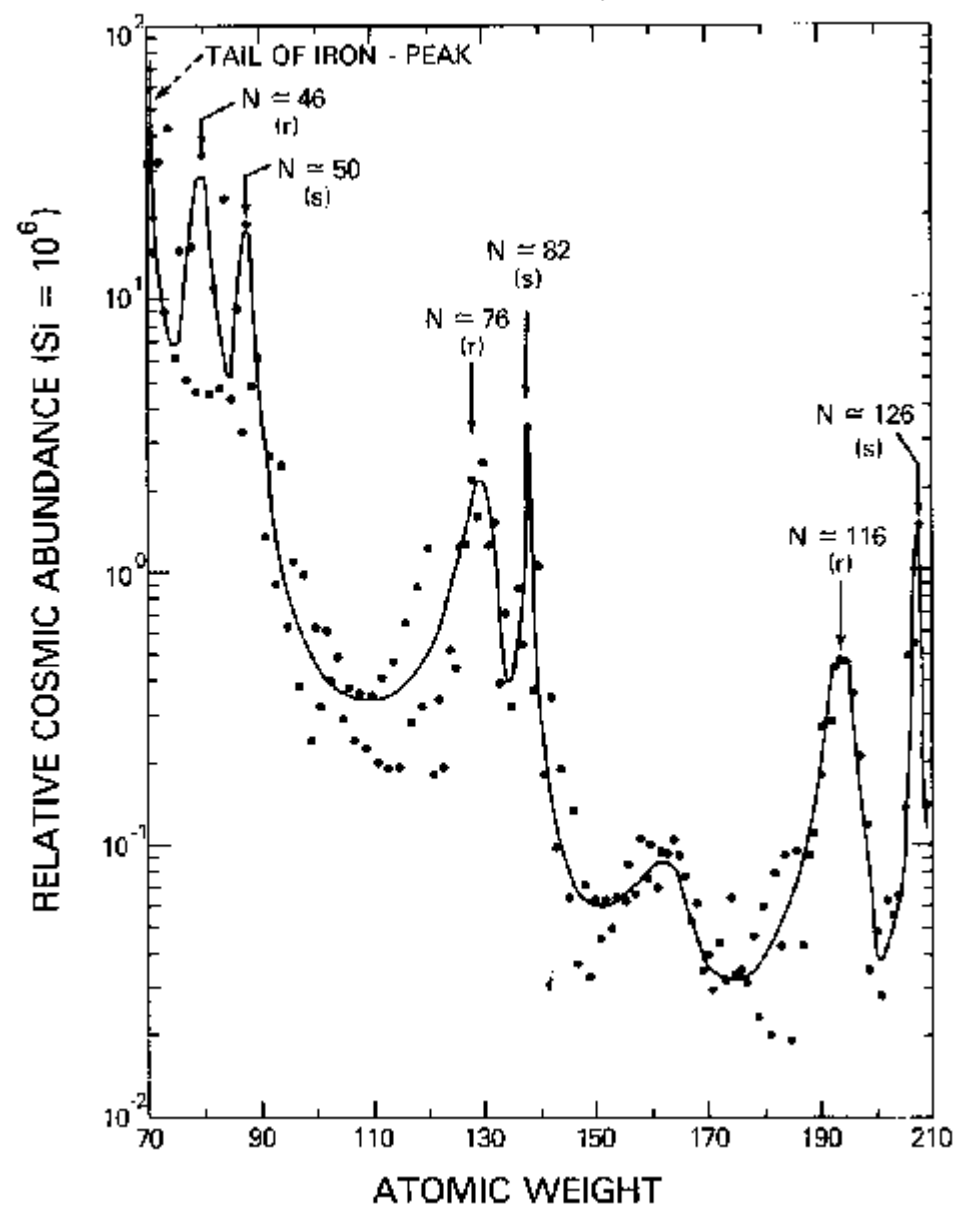
($N=8, 20, 28, 50, 82, 126$) $\Rightarrow$ pile up at magic n-numbers



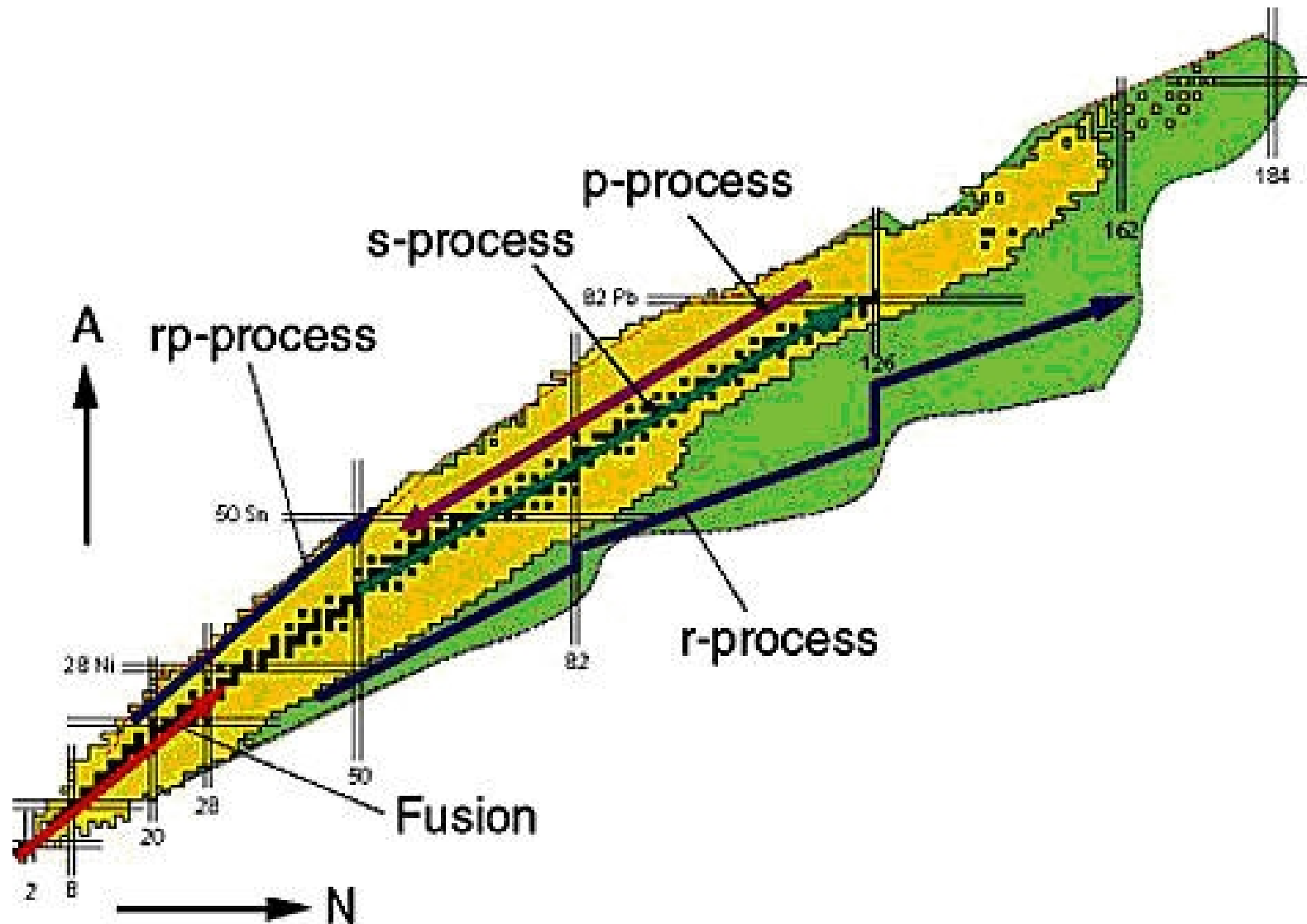
r-process

⇒ pile up at magic n-numbers





r-process



Site of r-process

Needed: High density of neutrons during a short period

Region close to neutron star during explosion ideal:

High neutron density from inverse beta decays (K-captures)

Many heavy seed nuclei from NSE (^{56}Ni , ^{56}Fe )

Correct abundance pattern? Not yet clear

