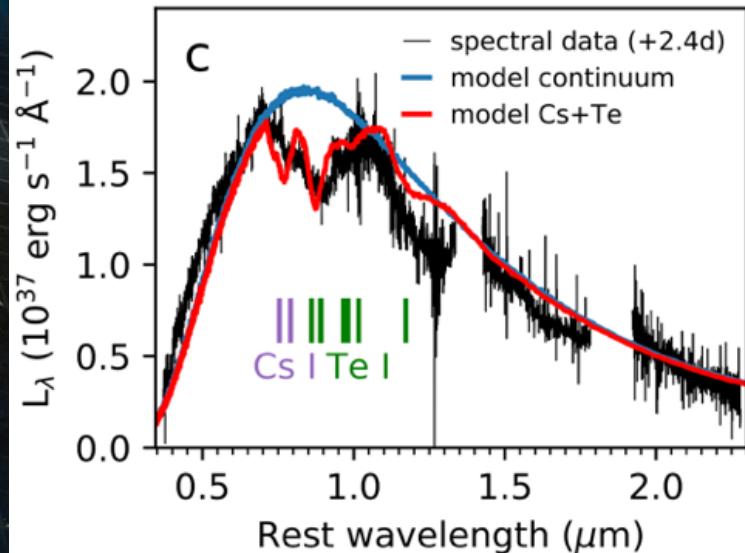
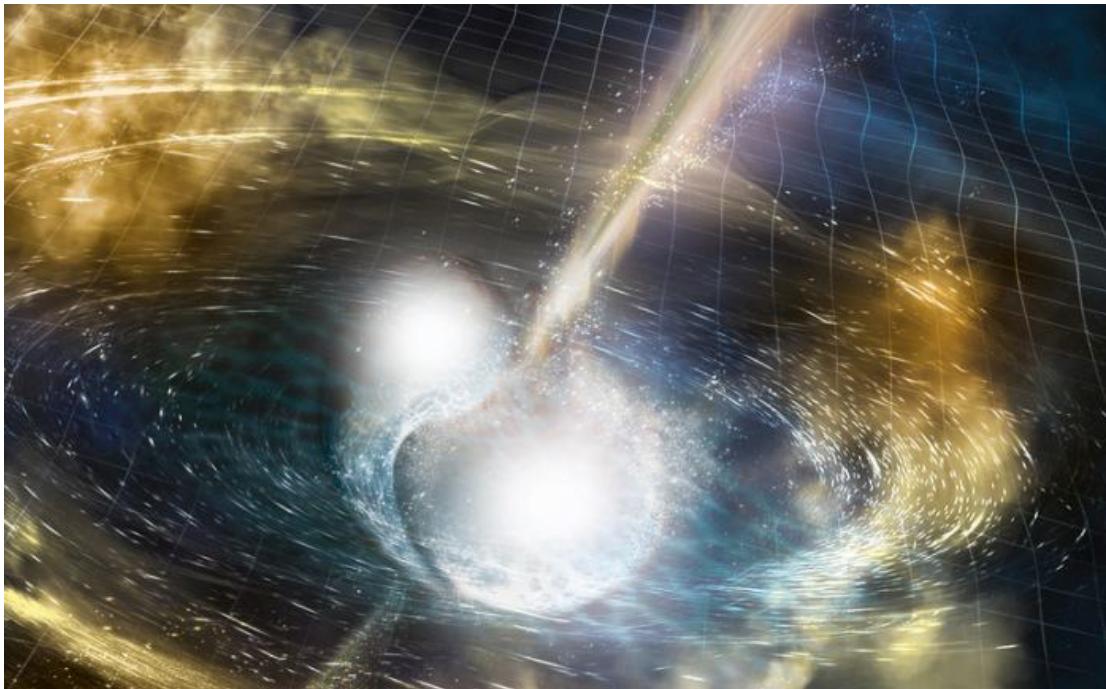


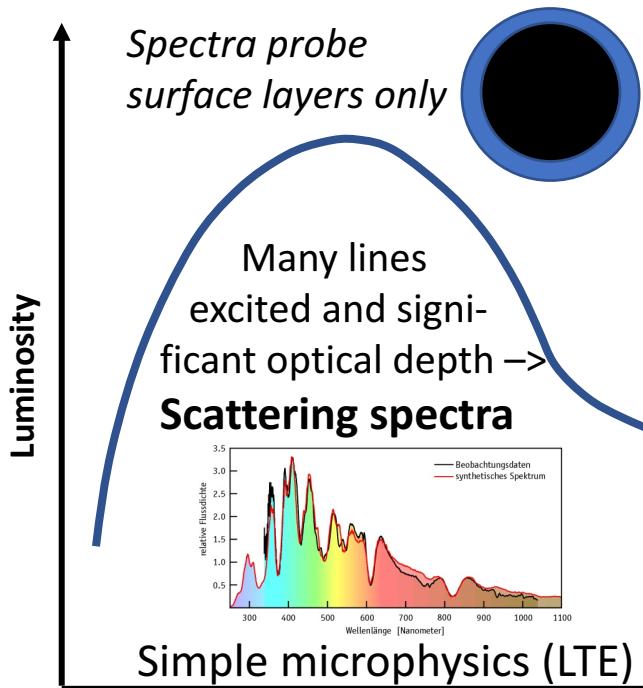
# Modelling light curves and spectra of supernovae and kilonovae



# Photospheric vs nebular phase

Long escape time for radiation

$$\rightarrow L_{\text{out}}(t) = \int_0^t K(t') L_{\text{in}}(t') t'$$



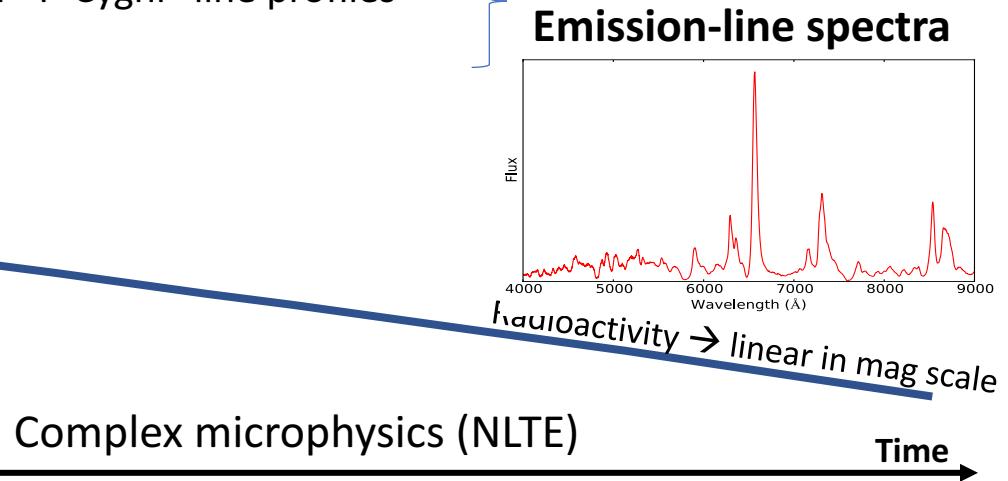
Short escape time for radiation

$$\rightarrow L_{\text{out}}(t) \sim L_{\text{in}}(t)$$

Few lines excited and reduced optical depth -->

- More variation in line emissivity
- Fewer "P-Cygni" line profiles

*Spectra probe all ejecta*



Complex microphysics (NLTE)

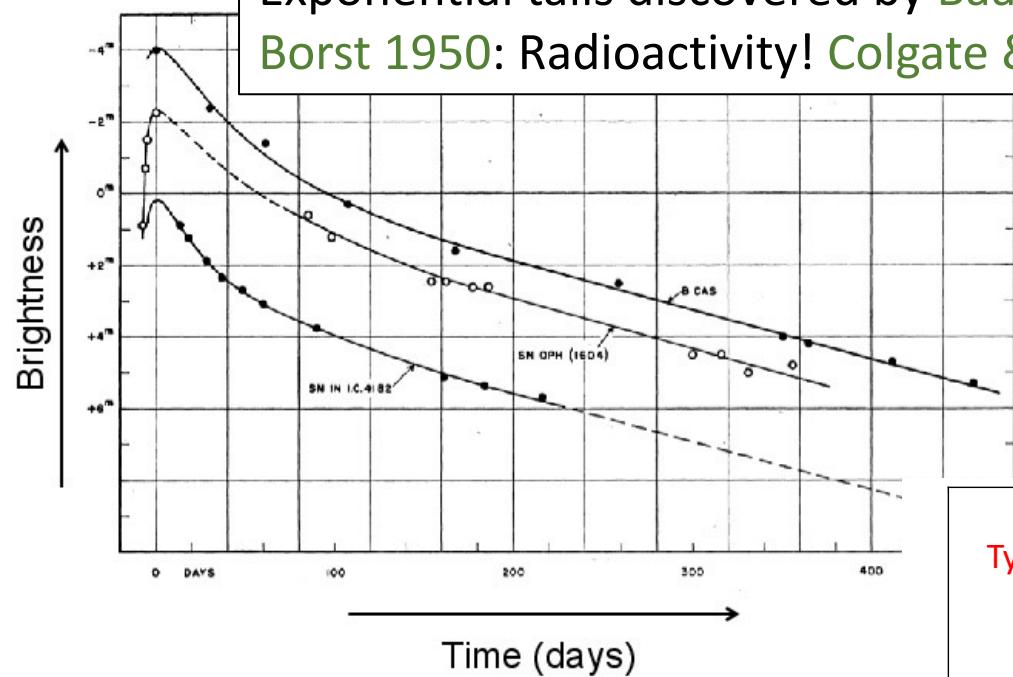
$$\text{Uniform ball: } t_{\text{thick}} = 80d \kappa_{0.1}^{1/2} M_{\text{Msun}} E_{51}^{-1/2}$$

Transition epochs: IIP SNe:  $\sim 140\text{d}$ , Ibc SNe:  $\sim 40\text{d}$ , KN:  $\sim 2\text{d}$

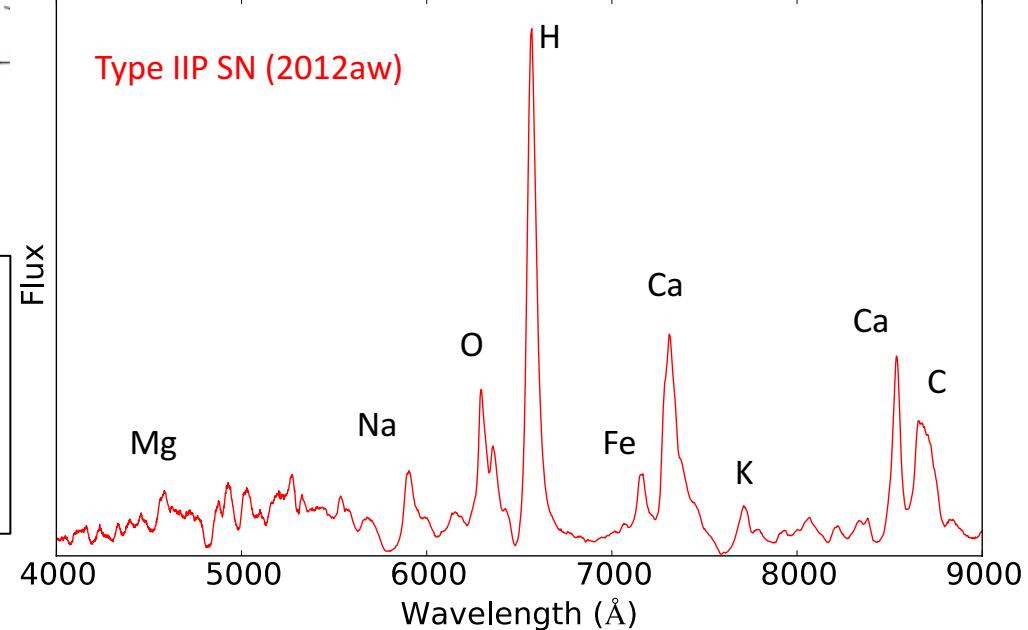
# The nebular phase

Exponential tails discovered by Baade+1945.

Borst 1950: Radioactivity! Colgate & McKee 1969:  $^{56}\text{Ni}/^{56}\text{Co}$ !



- $\sim 100\text{d} - 1000\text{d}$  post explosion
- Emission lines from all nuclear burning regions → window on nucleosynthesis and ejecta morphology.



- Data collection rate:  $\sim 5\text{-}10$  SNe per year (<1% of all discovered SNe).
- Current number of SNe with nebular spectra:  $\sim 50\text{-}100$

# The SUMO code (models nebular-phase spectra) AJ+2011, 2012

## Radioactive decay and gamma-ray thermalization

### Degradation of Compton electrons

- Spencer-Fano equation
- Ionization, excitation, heating

### NLTE statistical equilibrium

- 22 elements, 3 ion. stages
- 9,000 levels

### Temperature

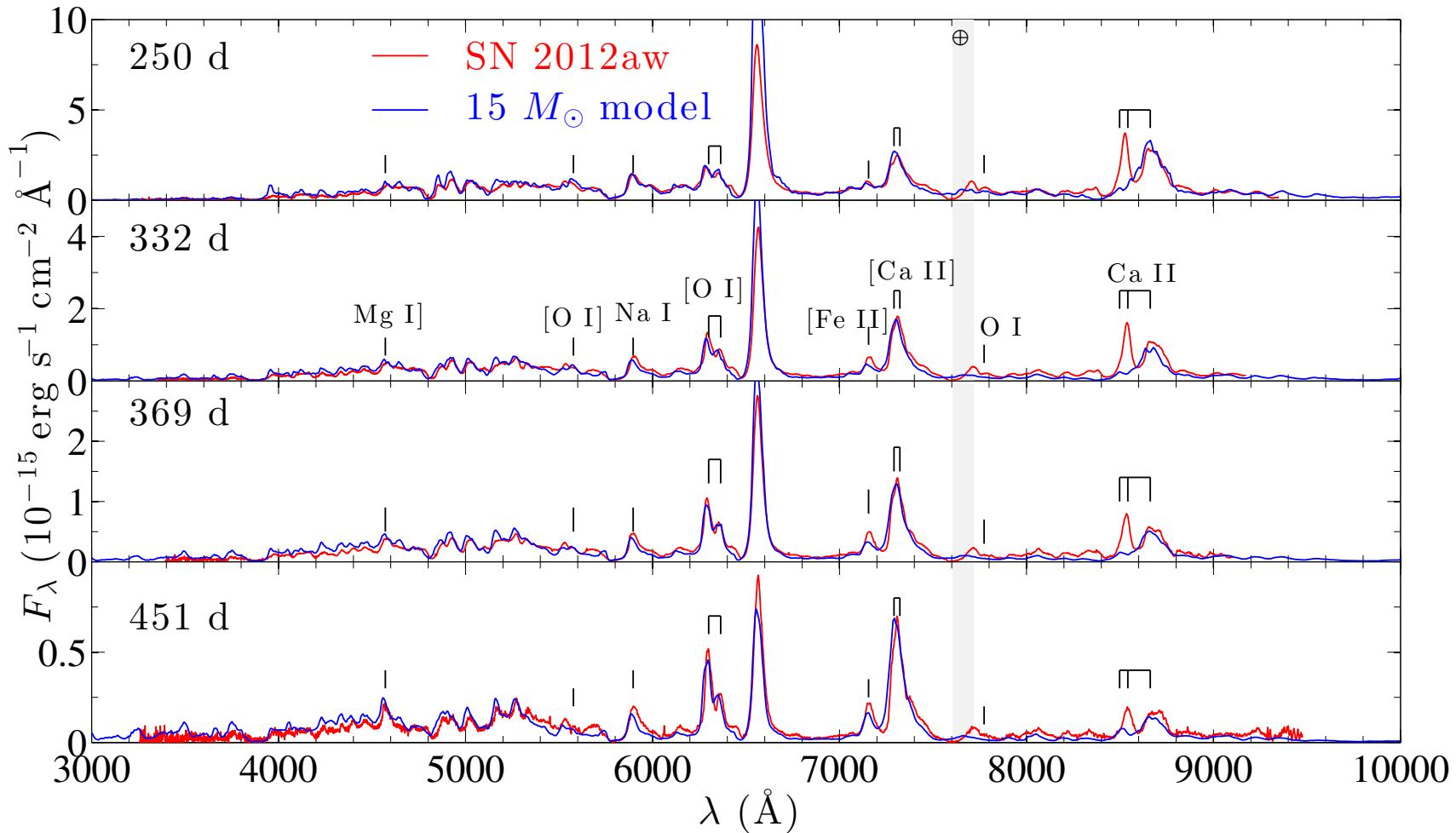
- Heating = cooling

### Radiative transfer

- Monte Carlo-based
- Sobolev approximation
- 300,000 lines

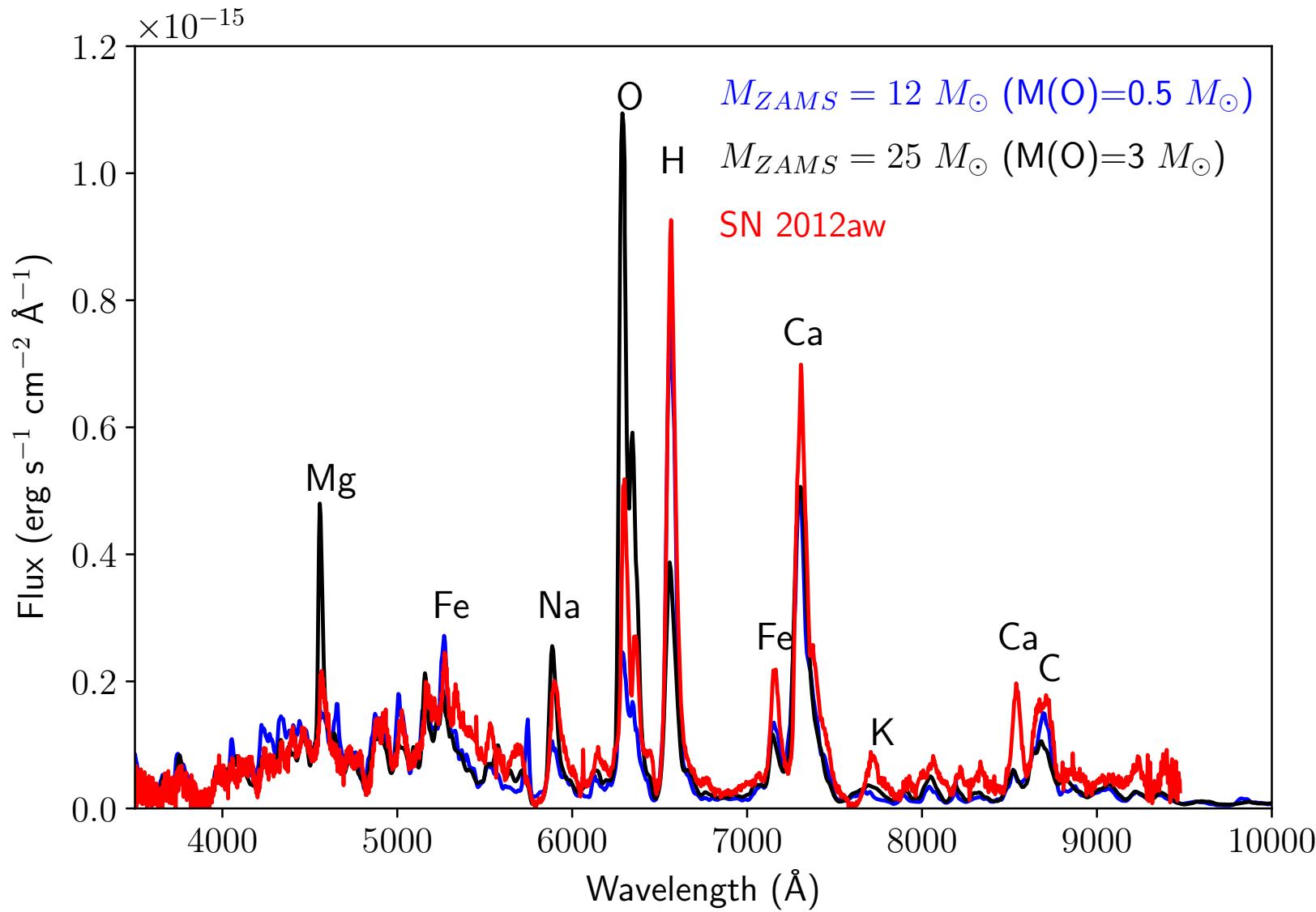
- Code is 1D but allows treatment of mixing by “virtual grid method”.

# Type II supernovae. Breakthrough a few year ago: *Model spectra start to agree quite well with observed spectra*

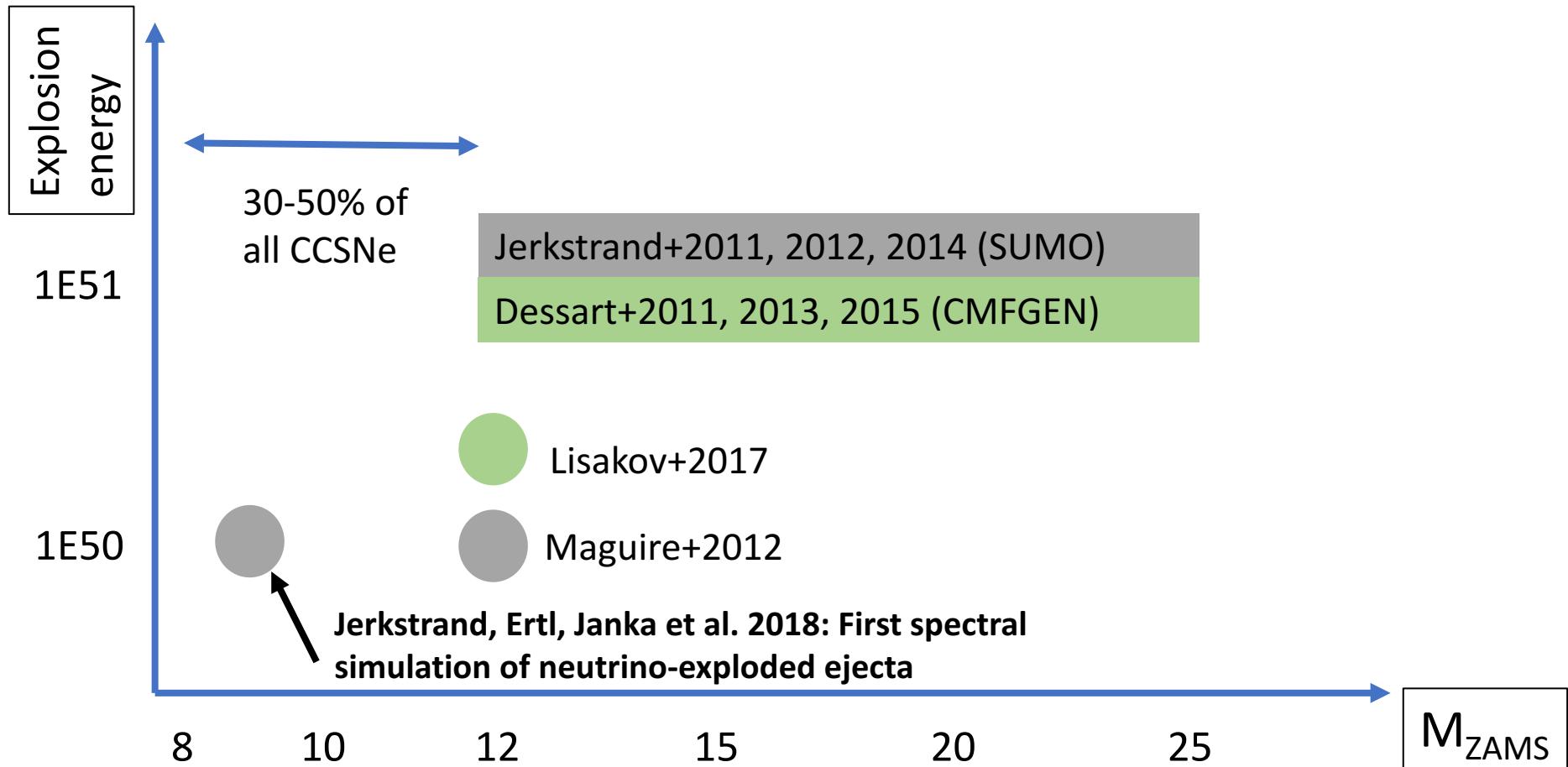


AJ+2014. See also Dessart+2013.

Can start to make detailed model comparisons, e.g. find best-fitting  $M_{ZAMS}$

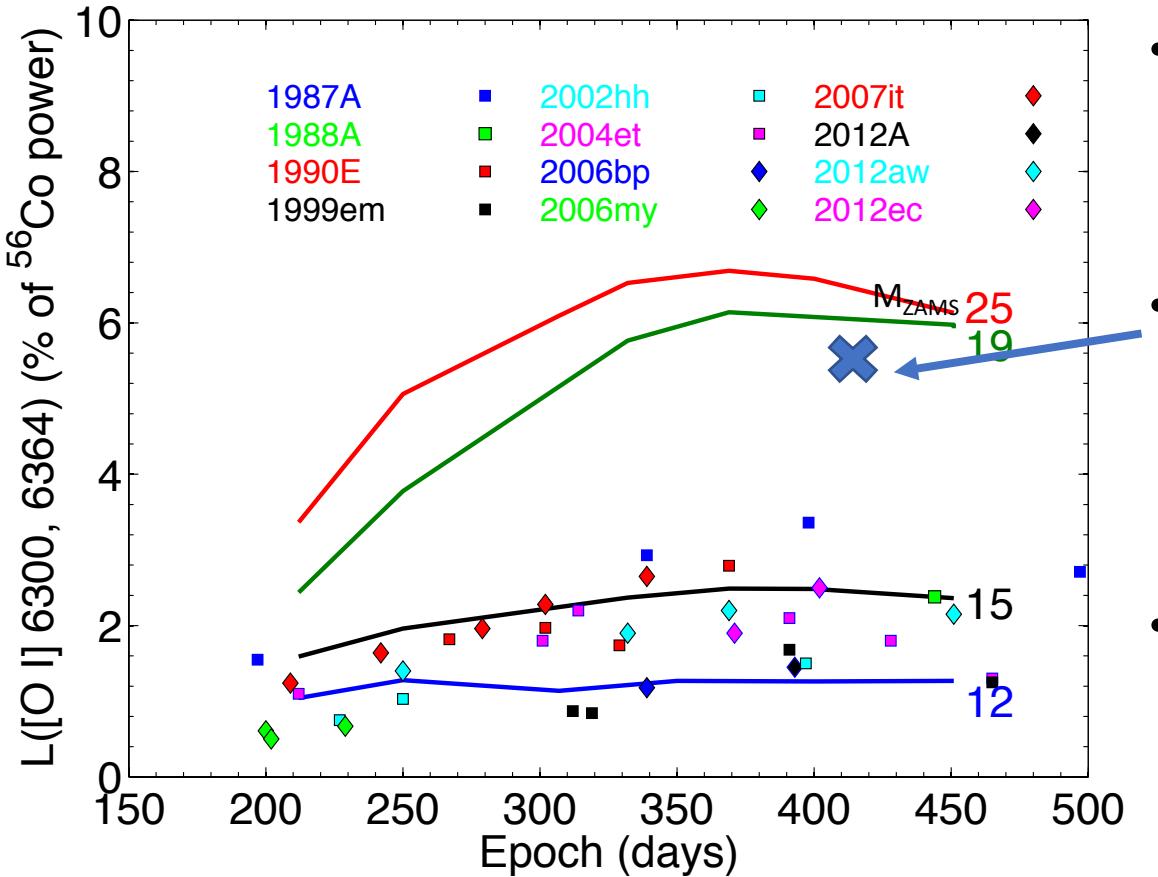


# Available nebular-phase models for Type II SNe



# Standard IIP supernovae: explosions of $M_{\text{ZAMS}} \sim 10\text{-}17 M_{\odot}$ stars

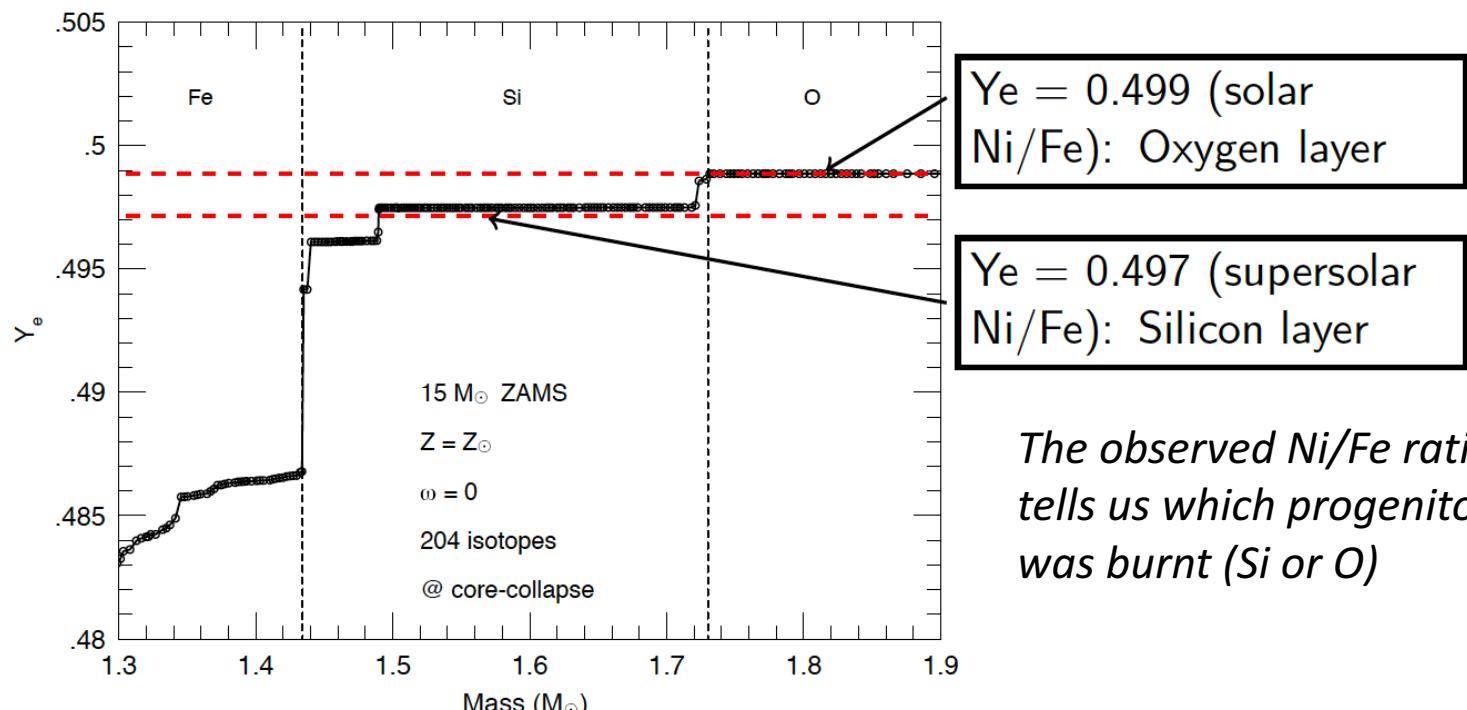
AJ+2015 (MNRAS), AJ in prep.



- “RSG problem” (Smartt 2009) is real: confirmed from two directions.
- However, first object with possibly  $M > 20 M_{\odot}$  now discovered (Anderson+2018): low metallicity.
- Same trend for Type IIb SNe (AJ+2015 (A&A))

# Diagnosing the explosive nucleosynthesis: Ni/Fe ratios

SN	Ni/Fe (times solar)	Reference
Crab	60 – 75	Macalpine 1989, Macalpine 2007
SN 1987A	0.5 – 1.5	Rank 1988, Wooden 1993, AJ+2015
SN 2004et	~1	AJ+2012
SN 2006aj	2 – 5	Maeda+2007, Mazzali+2007
SN 2012A	~ 0.5	AJ+2015
SN 2012aw	~ 1.5	AJ+2015
SN 2012ec	2.2 – 4.6	AJ+2015



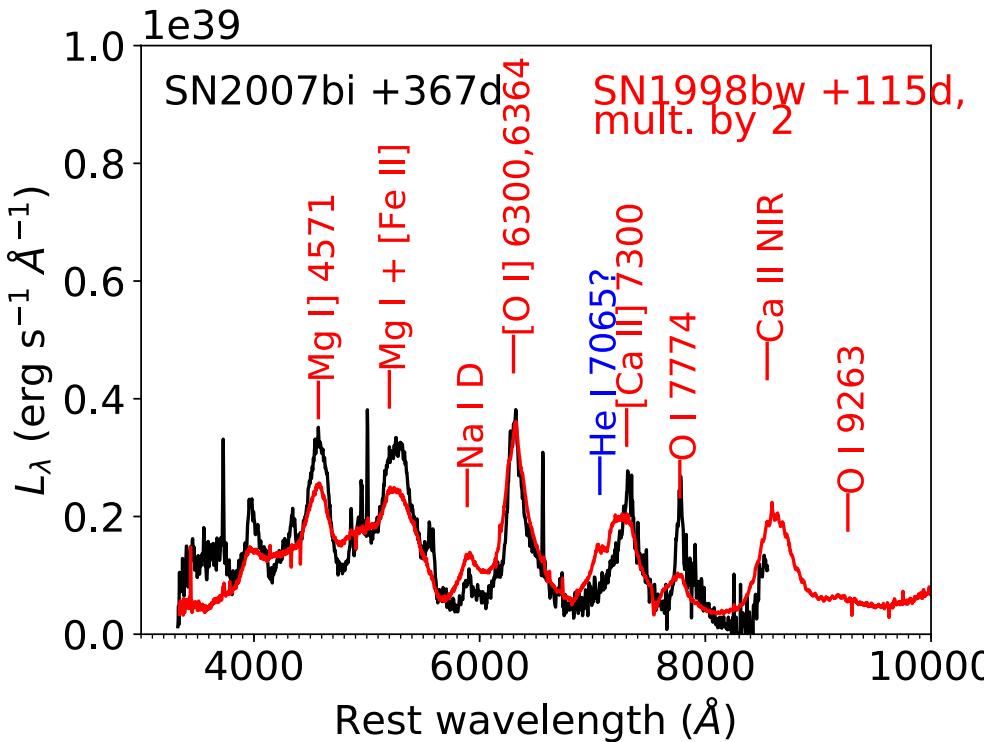
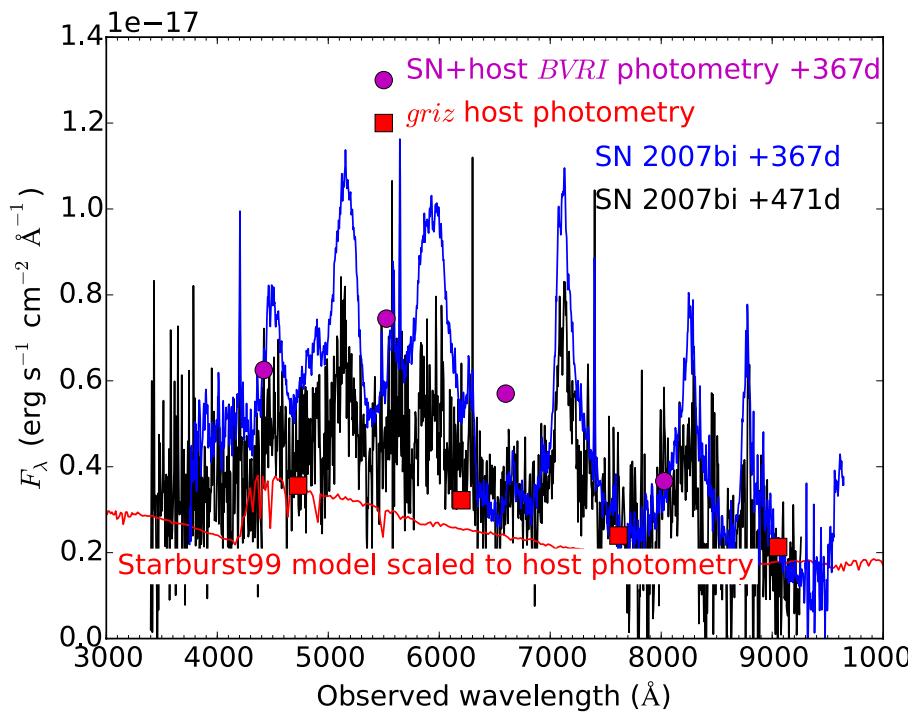
# The monsters

*Superluminous  
Type I supernovae*



# Nebular spectra of SLSN Ic: with galaxy subtraction, prototype SN 2007bi (Gal-Yam+2009) is similar to SN 1998bw

AJ+2017

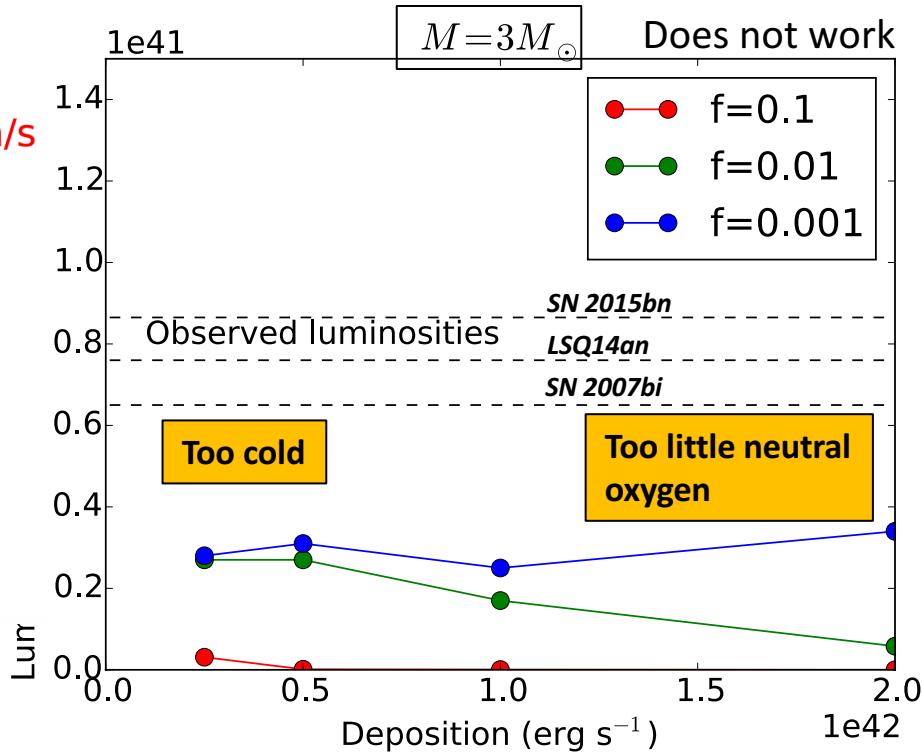
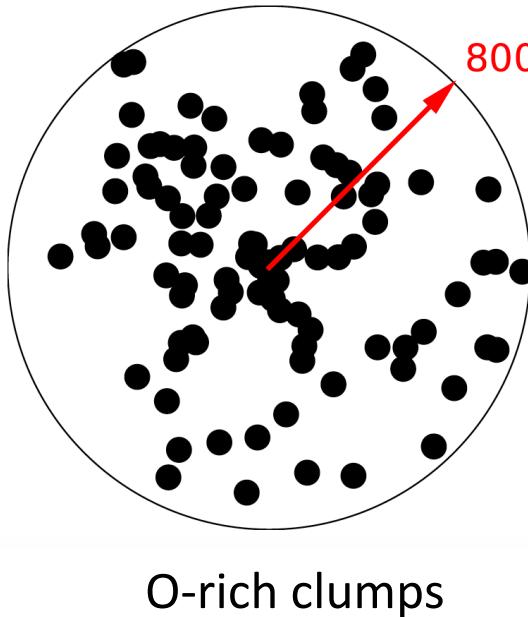


[O I] lines : Very large O masses required ( $\gtrsim 10 M_{\odot}$ )

→ These SNe come from very massive stars ( $M_{\text{ZAMS}} \gtrsim 40 M_{\odot}$ )

AJ+2017

- Three parameters:
- O mass
  - Powering level
  - Filling factor

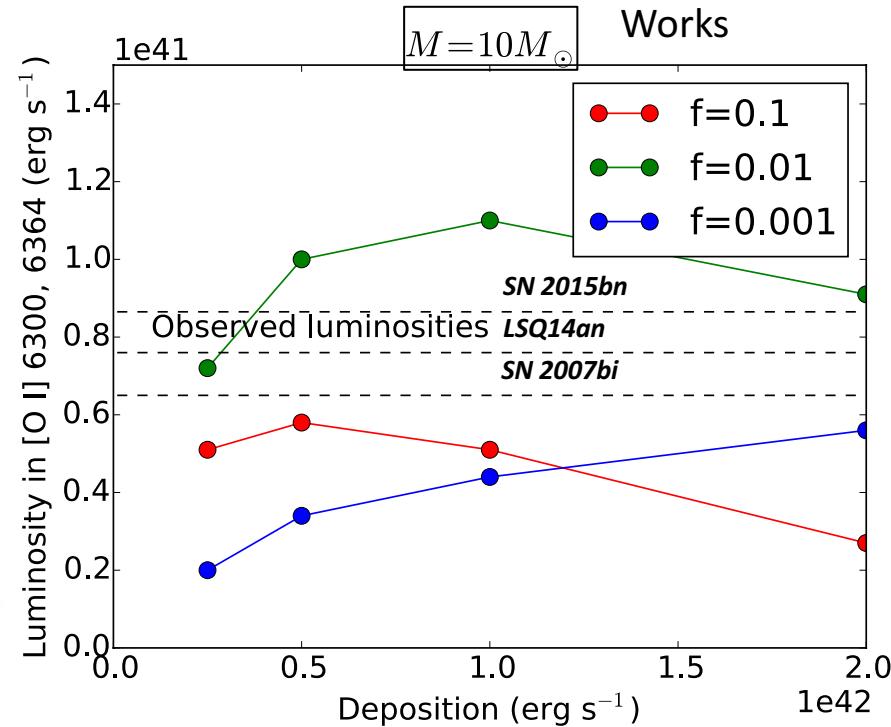
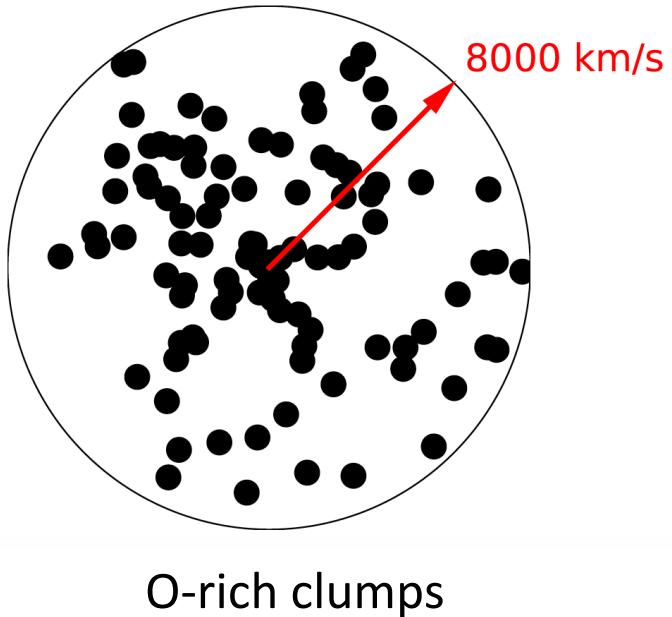


[O I] lines : Very large O masses required ( $\gtrsim 10 M_{\odot}$ )

→ These SNe come from very massive stars ( $M_{\text{ZAMS}} \gtrsim 40 M_{\odot}$ )

AJ+2017

- Three parameters:
- O mass
  - Powering level
  - Filling factor

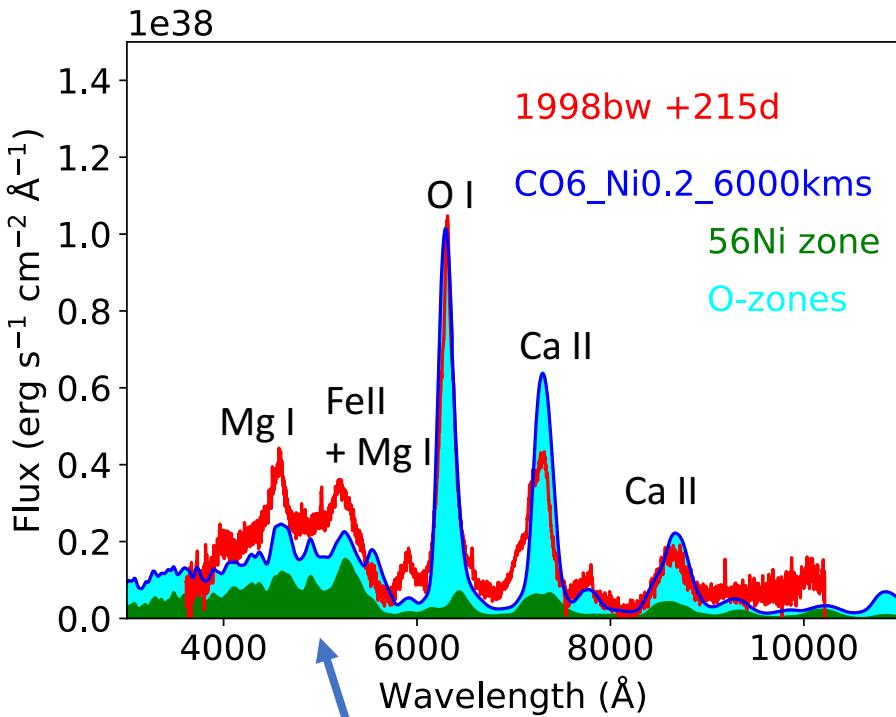


- Independent support from large inferred Mg masses ( $1.5-15 M_{\text{sun}}$ )
- Recombination lines suggest material is clumped or compressed in shells ( $f \lesssim 0.01$ ).

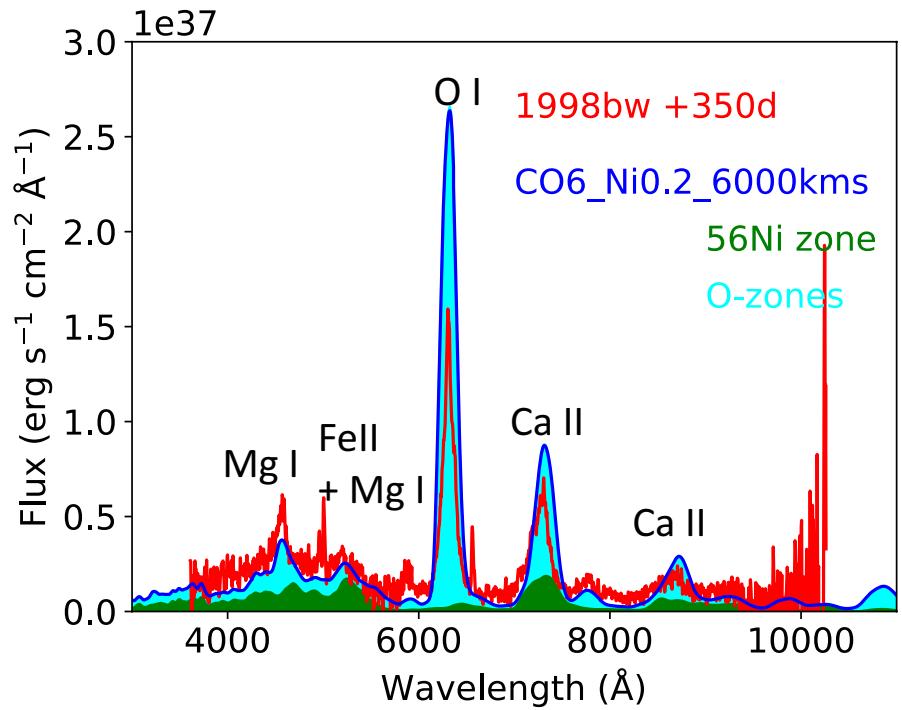
# SN 1998bw: Standard $^{56}\text{Ni}$ -powered models, powering 6-10 $\text{M}_{\text{sun}}$ CO cores fit well.

AJ+2018, in prep.

See also Mazzali+2001, Maeda+2006,  
Dessart+2018.



<5500 Å region dominated by complex radiative transfer effects



# Summary of Ic supernovae : view from late-time spectra

Broad-lined Ic  
(e.g. 1998bw)

Superluminous SN Ic fast

Superluminous SN Ic slow

$$\begin{aligned} M(CO) &\sim 6 M_{\text{sun}} \\ M_{\text{ZAMS}} &\sim 25 M_{\text{sun}} \end{aligned}$$

??  
No nebular  
data

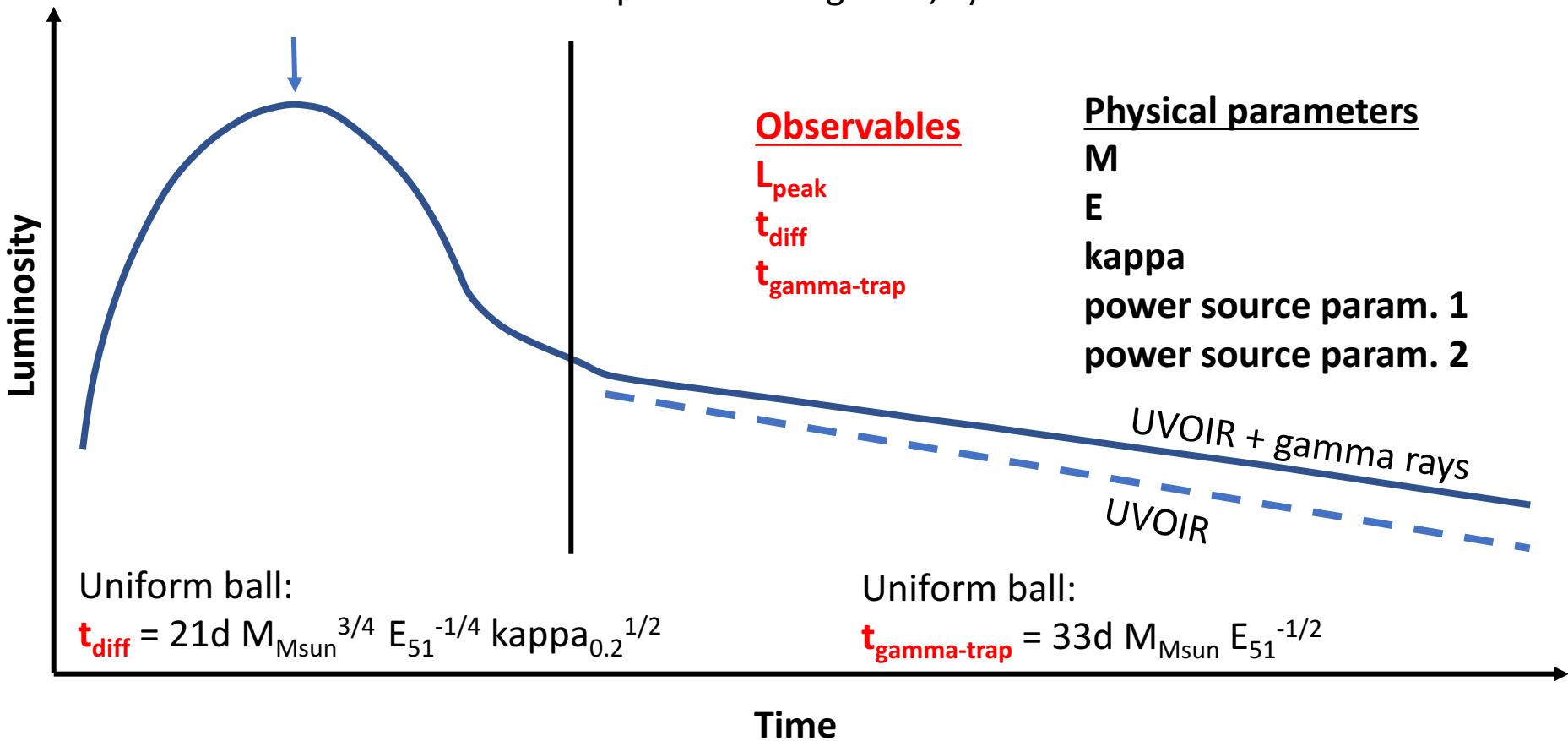
$$\begin{aligned} M(CO) &> \sim 15 M_{\text{sun}} \\ M_{\text{ZAMS}} &\sim 40-100^* M_{\text{sun}} \end{aligned}$$

\* Upper limit set by PPISN limit.  
Association with pair-instability SNe ( $>130 M_{\text{sun}}$ ) not likely (**AJ+2016**).

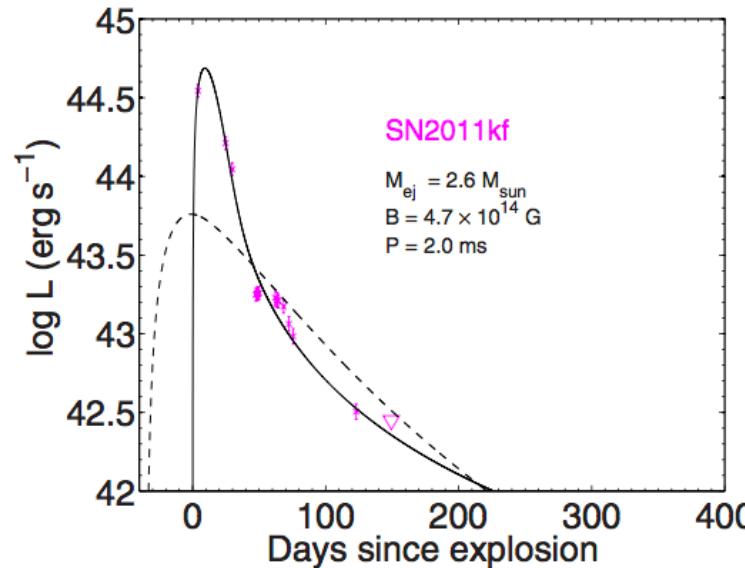
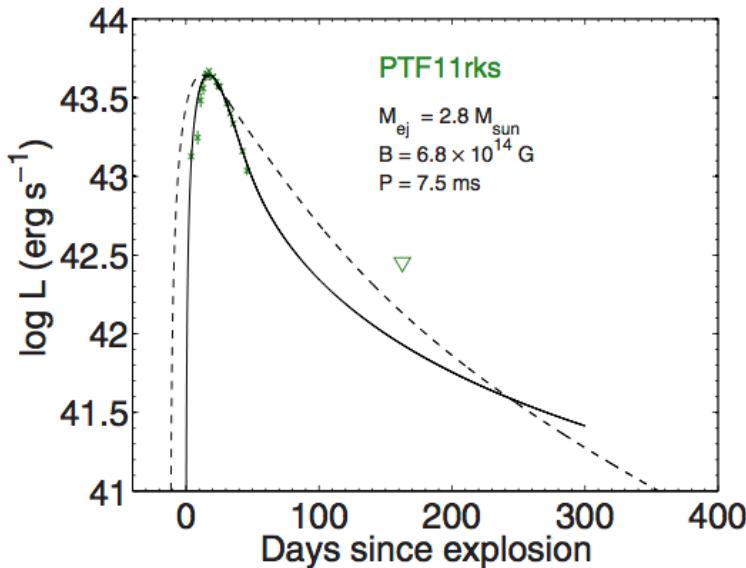
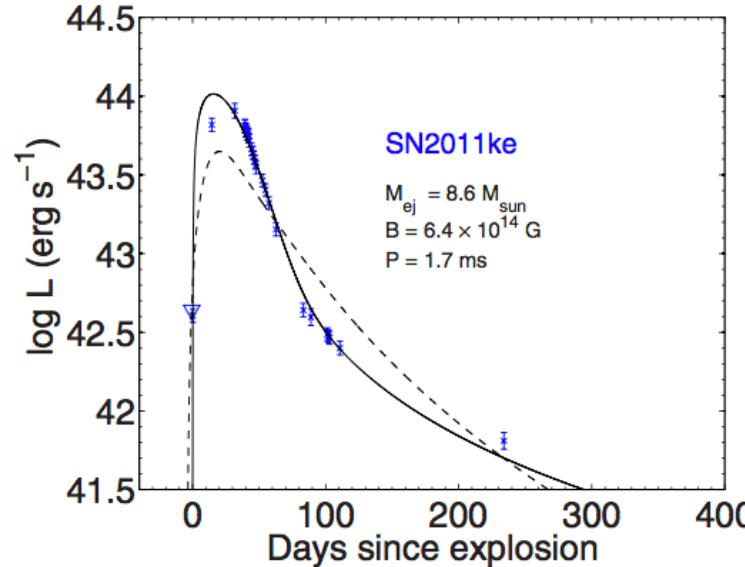
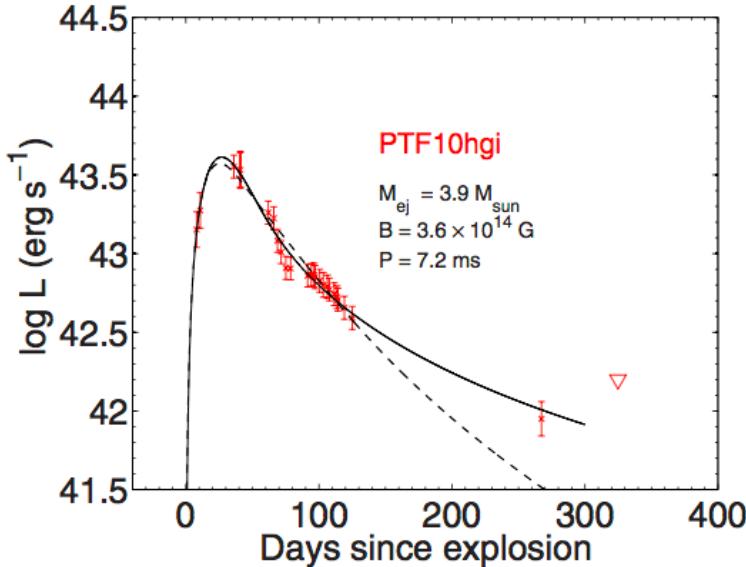
# Light curve modelling : searching for the power source of SLSNe

$$L_{\text{peak}} \sim L_{\text{in}}(t_{\text{peak}}) \text{ ("Arnett's law")}$$

More generally, "brightness" depends on strength of power source (amount of radioactivity, spin-down power of magnetar,...)



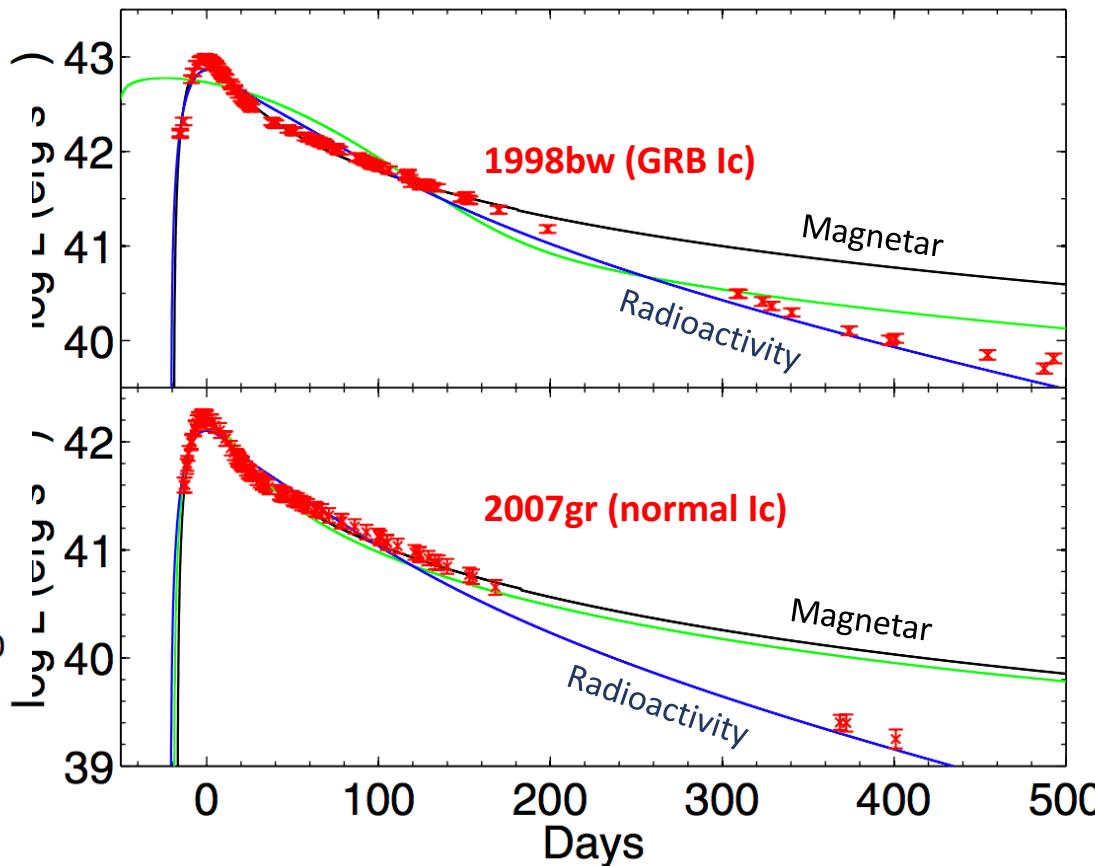
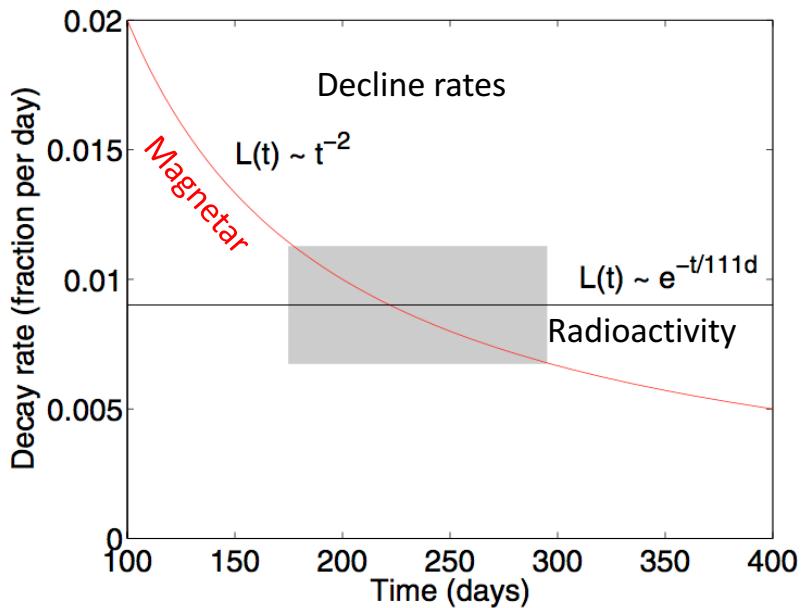
# Light curve modelling of SLSNe : evidence for magnetars?



Inserra, Smartt,  
Jerkstrand et al 2013

LC fitting code  
publicly available at  
<https://star.pst.qub.ac.uk/webdav/public/ajerkstrand/Codes/Genericarnett/>

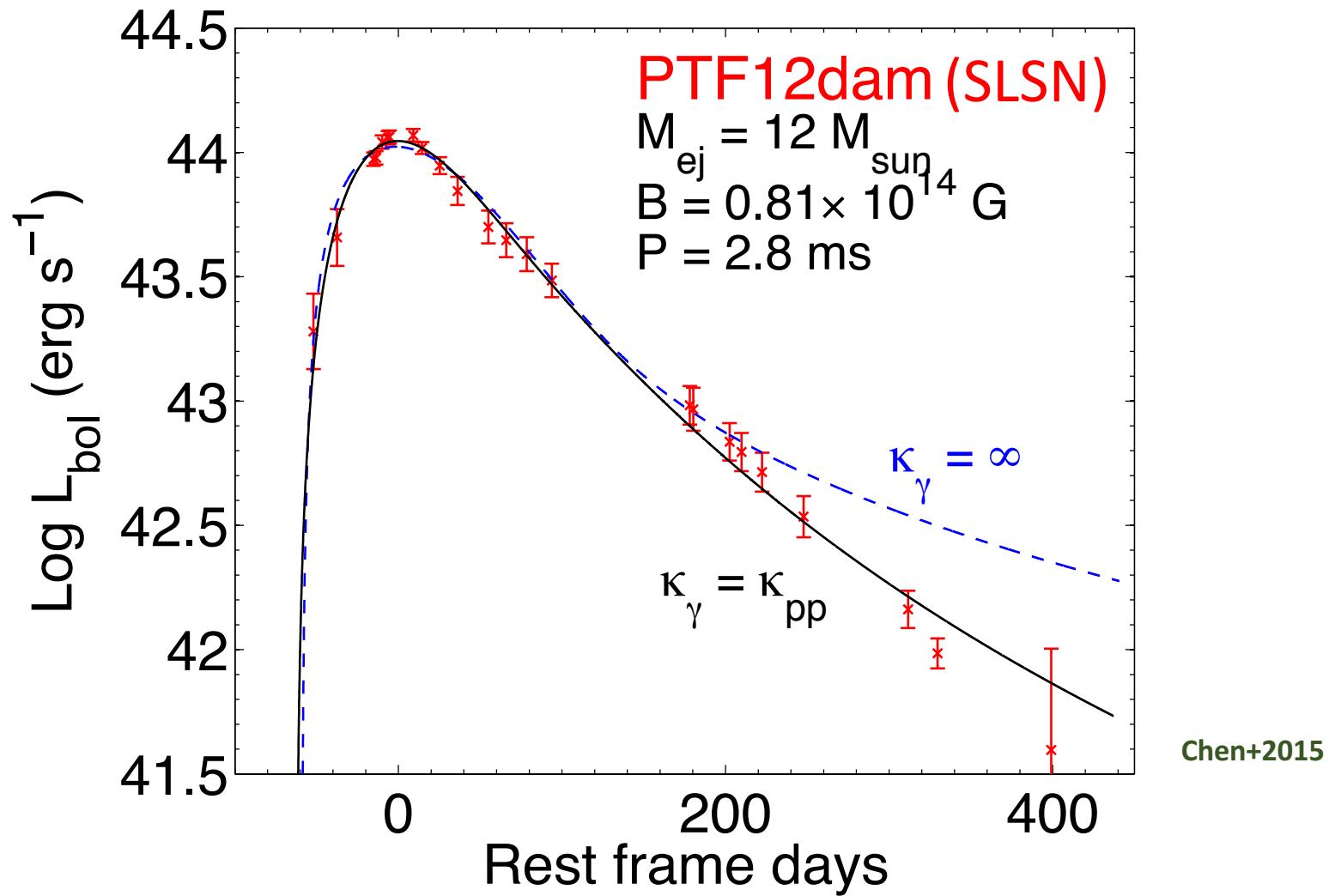
# Distinguishing magnetar powering from radioactivity



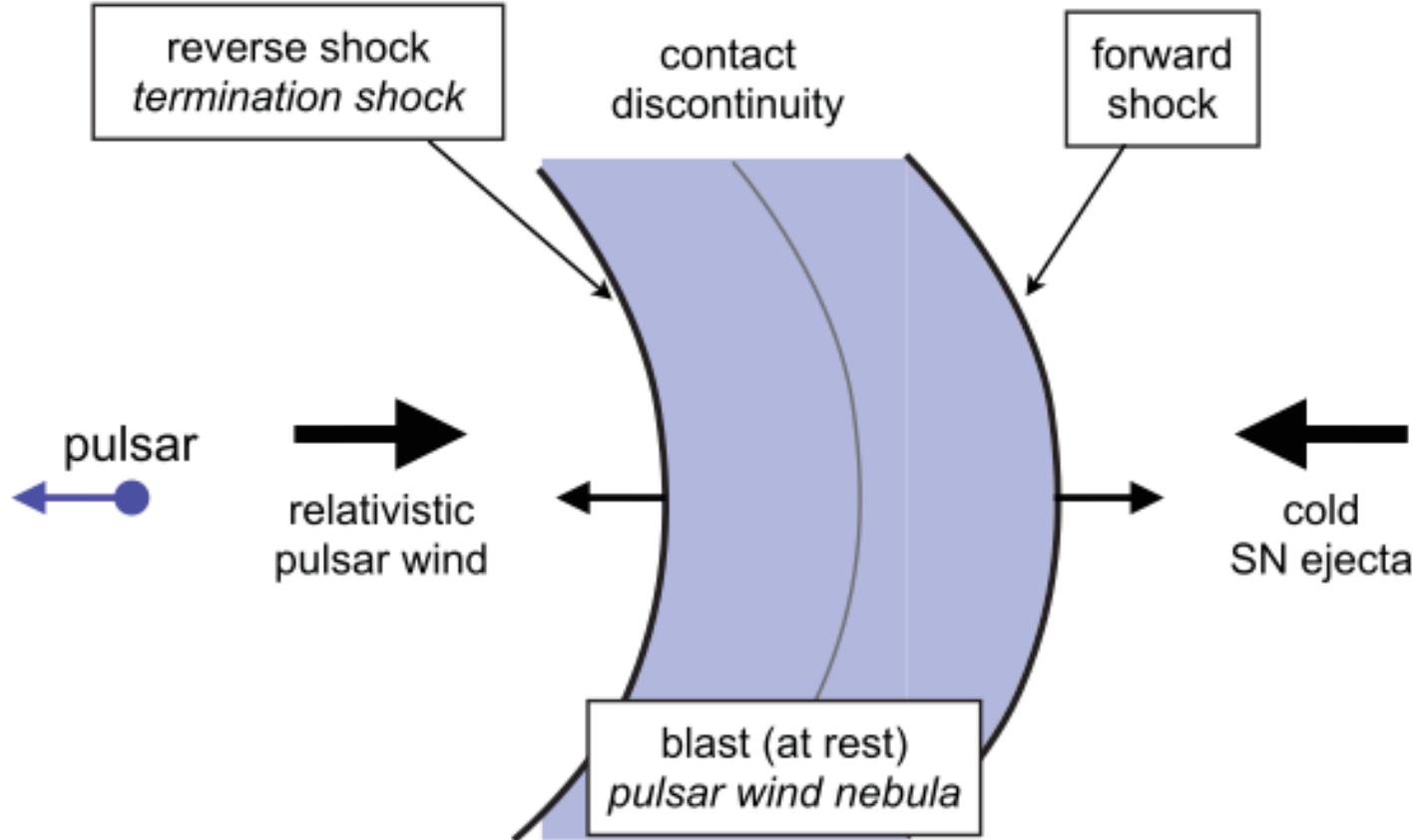
Inserra, Smartt, Jerkstrand et al 2013

*For non-superluminous Type Ibc SNe radioactivity fits better than magnetar powering*

However : allowing for escape of high-energy radiation from pulsar-wind region is an issue



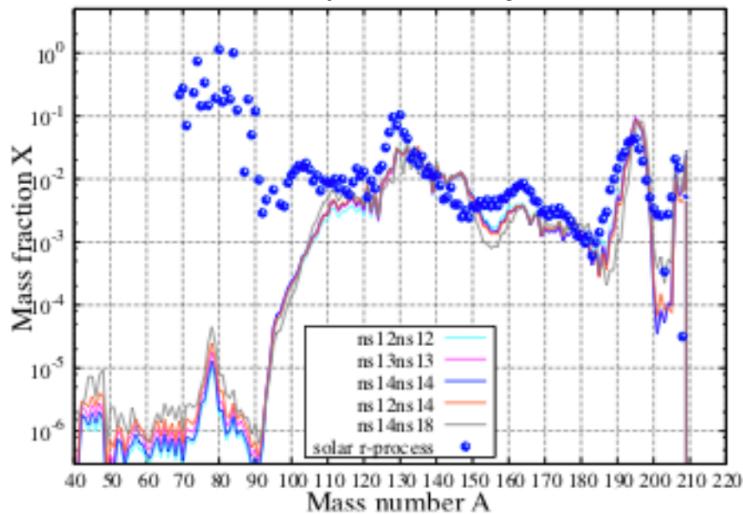
Modelling what's going on in the pulsar wind nebula is a formidable problem that noone has solved yet



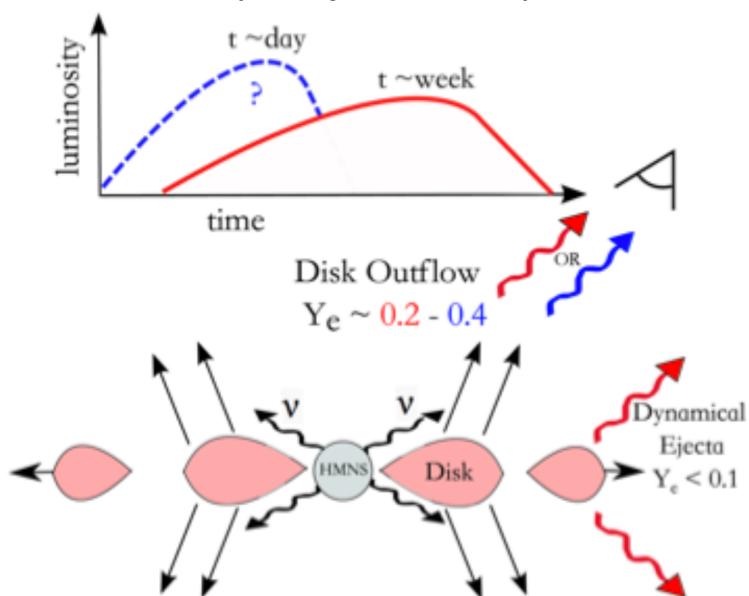
Kotera+2013

# Kilonovae

## Pure –process ejecta

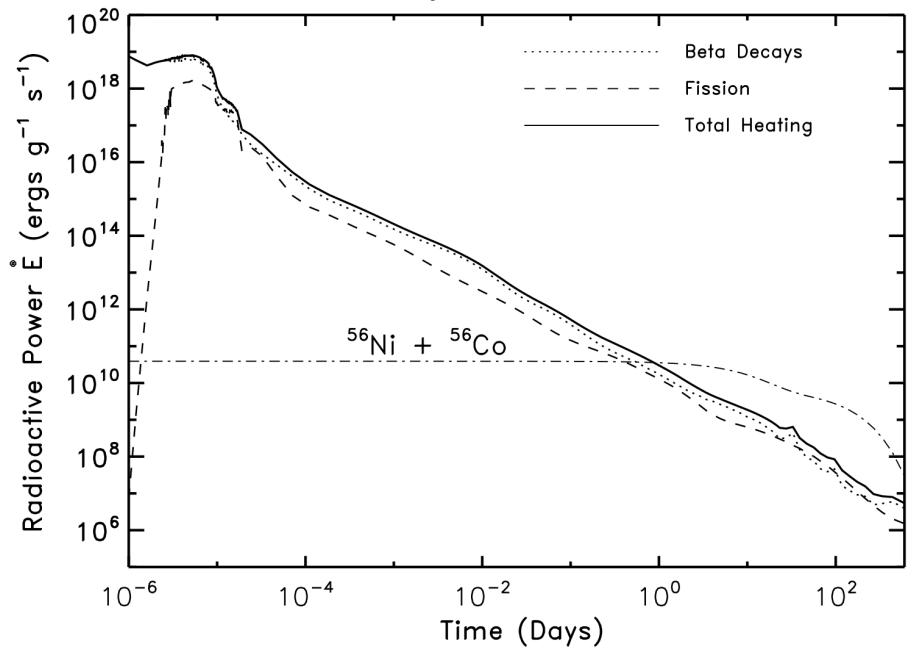


## Multiple ejecta components



Metzger+ 2014

## Radioactivity now well understood

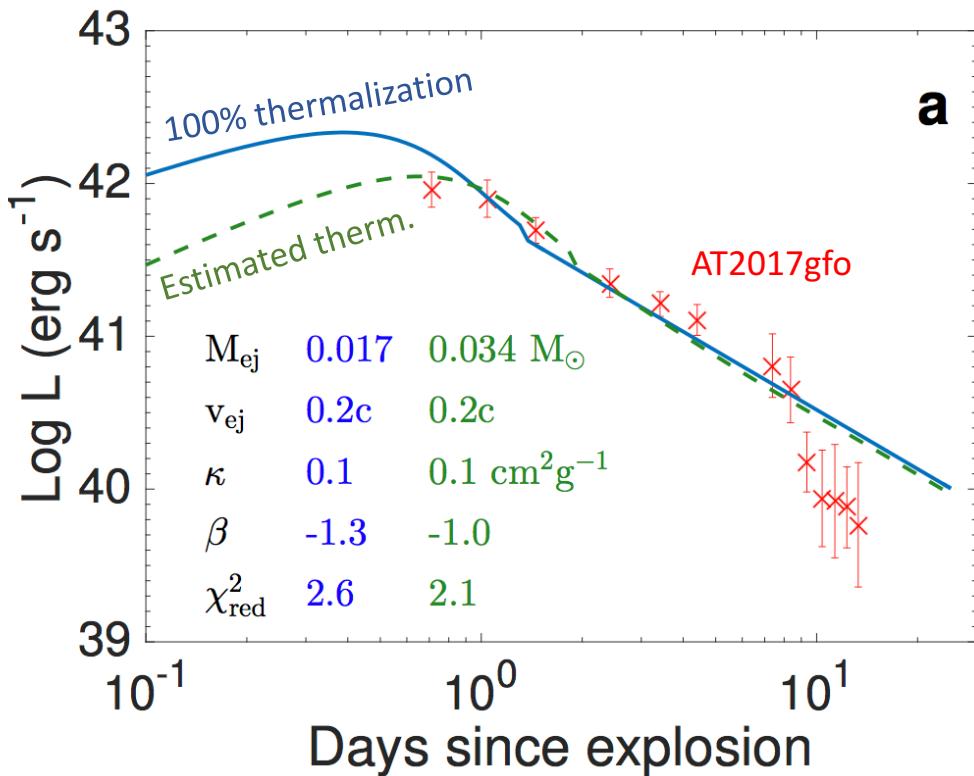
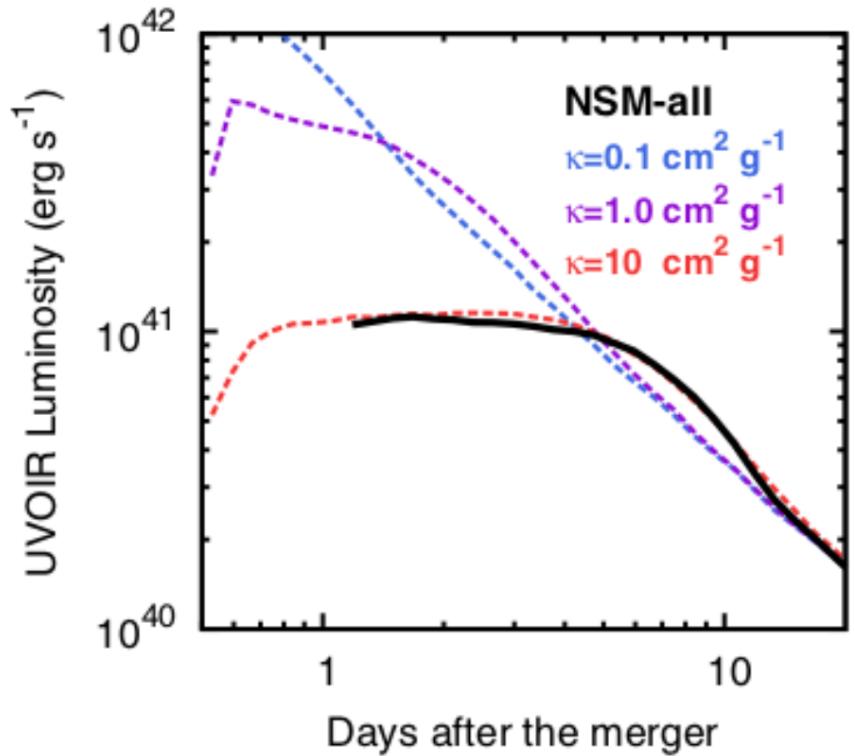


Metzger+ 2010

One parameter less than supernovae  
(all ejecta are radioactive, not some fraction  $X$  of it)

On the other hand more complex morphology and composition.

# Kilonovae : modelling the light curve



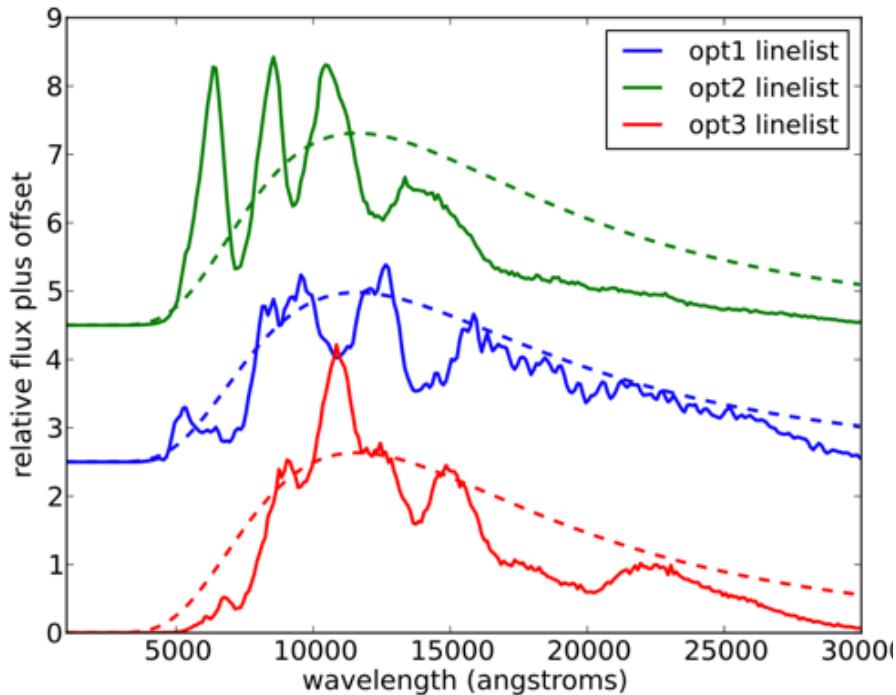
Tanaka+2013: Fixed opacity models do quite well

Smartt, Chen, Jerkstrand+2017, Nature

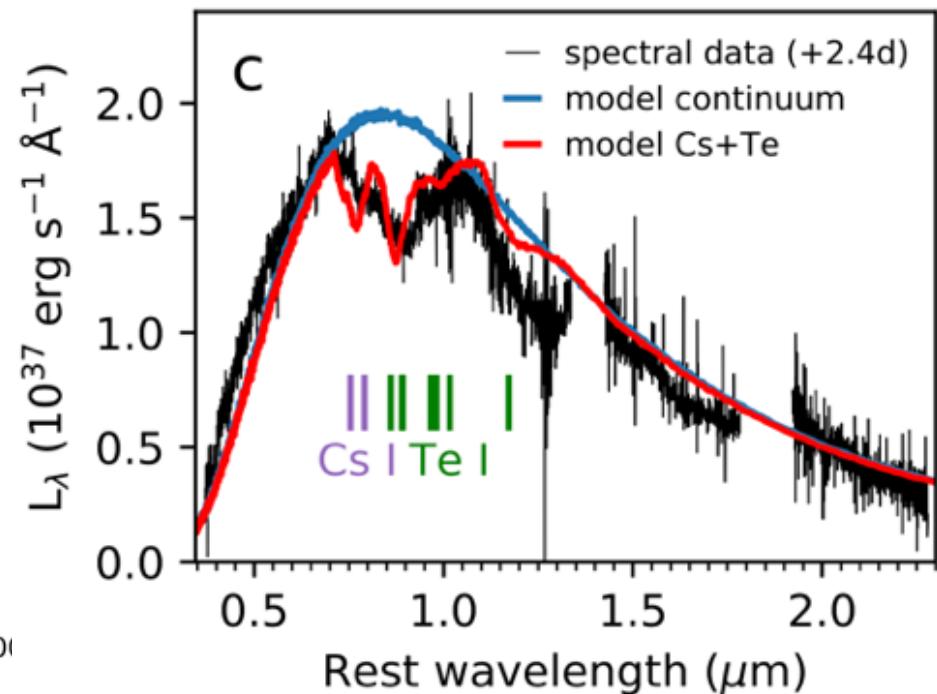
AT2017gfo ejected  $\sim 0.03 M_{\text{sun}}$  of ejecta at 20% speed of light.  
Powering consistent with predicted r-process radioactivity.

# Kilonovae : modelling the spectra

Kasen+2013: Issues with r-process atomic data: much work still to be done



Smartt+2017: A toy fit including only Cs and Te.



Kilonovae reach NLTE regime already after few days → NLTE codes like SUMO or CMFGEN are needed.

